

image retrieval

Computer Vision Methods 2025

CTU in Prague

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slide credits also to: Jiri Matas, Ondrej Chum, Andrej Mikulik, Filip Radenovic,

Michal Perdoch, James Pritts, Dmytro Mishkin, Jan Cech

- task formulation
- bag-of-words (BoW) model
- BoW generic point-of-view → other approaches
- fast spatial (geometric) matching
- special retrieval tasks

the task

image retrieval - example



query image

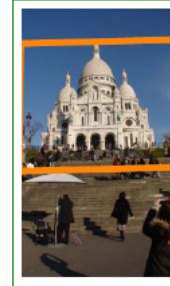
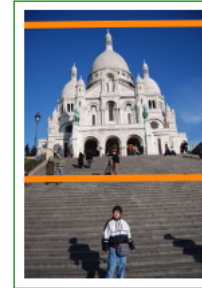
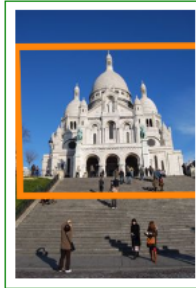


image retrieval



for image copy detection

image retrieval



for image copy detection

image retrieval



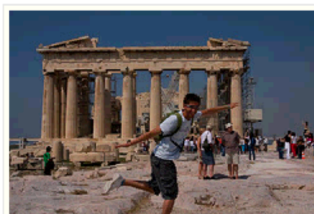
for image geo-localization

image retrieval



for image geo-localization

image retrieval



for image geo-localization

image retrieval



for image geo-localization

image retrieval



History [\[edit \]](#)

Originally a family business, the pub was founded in 1499,^[1] and therefore celebrated its 500th anniversary in 1999. It has been referred to as the **oldest brewery in Prague**. In 1762 the

for landmark recognition

image retrieval



for e-commerce

image retrieval



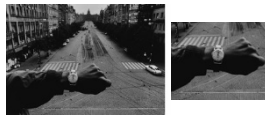
for logo infringement identification

image retrieval - task

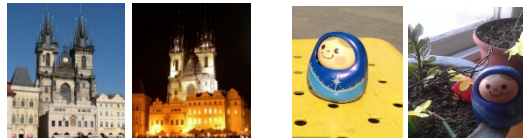
- given a **query image** and an **image collection (database)**



- retrieve database images according to their relevance to the query
 - rank all images
 - retrieve most relevant
- relevance defined in different ways, according to the task



identical photo



identical object



infringement

- retrieval approaches characterized by performance
 - quality: ability to retrieve relevant images first
 - speed: small query time
 - memory footprint: low memory requirements
 - scalability: applicability to large image collections

image retrieval - task

- retrieval is a ranking task for a given query “q”
- relevance is defined for pairs (q,a), “a” is a database image
- degree of relevance $s(q,a)$
 - estimate it to perform retrieval
 - need for ground-truth
- difficult to obtain continuous degree of relevance in ground-truth
 - binary approximation
 - 1: positive / matching / relevant pair
 - 0: negative / non-matching / non-relevant pair

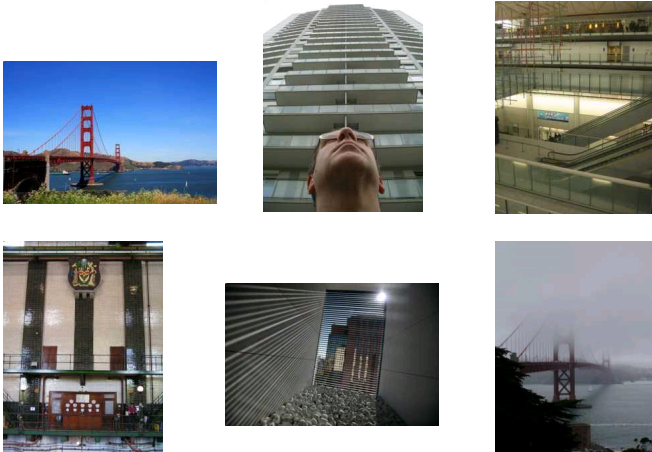
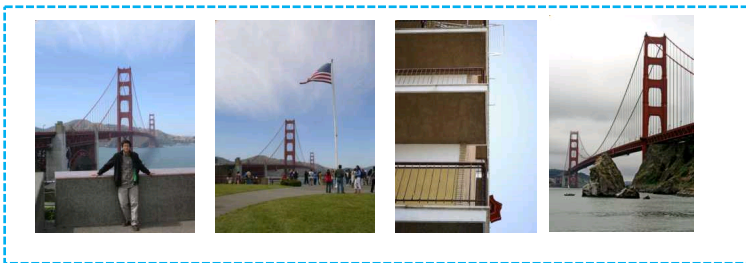
image retrieval - evaluation

query:

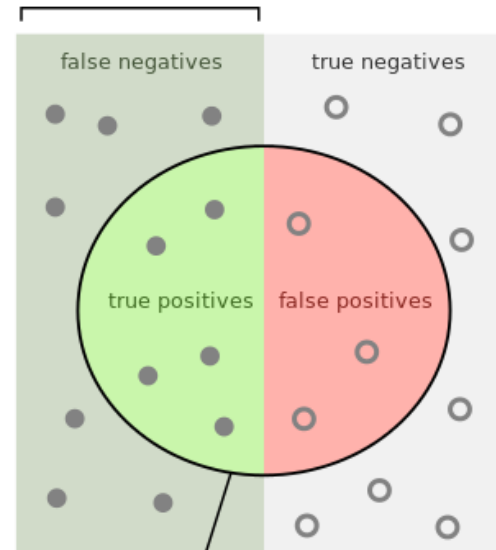


- 10 database images
- 5 relevant images, according to binary pairwise labels
- select a “window” of top-k images
- measure precision@k and recall@k
- what should k be? should we use only one window?

ranking:



relevant elements



How many selected items are relevant?

$$\text{Precision} = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

How many relevant items are selected?

$$\text{Recall} = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$

image retrieval - evaluation

query:



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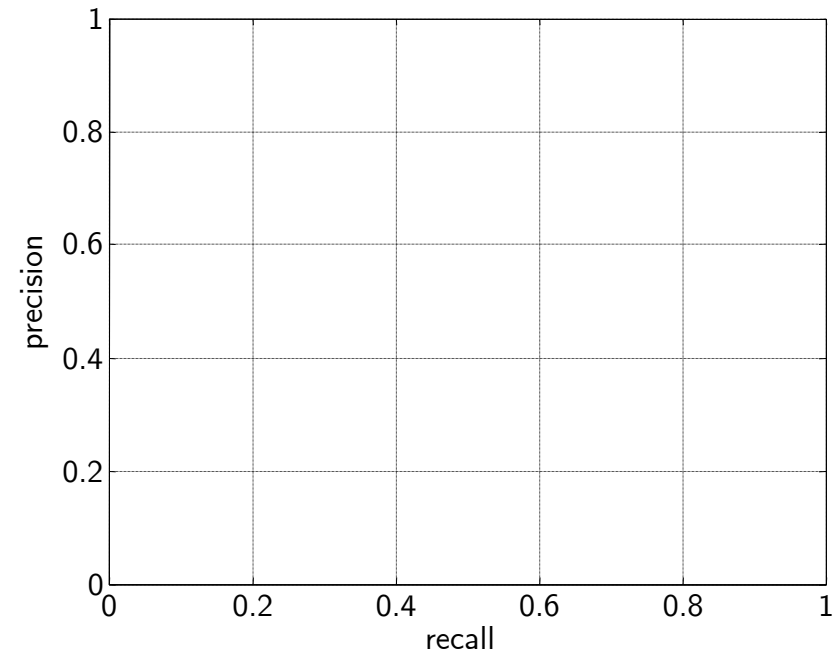


image retrieval - evaluation

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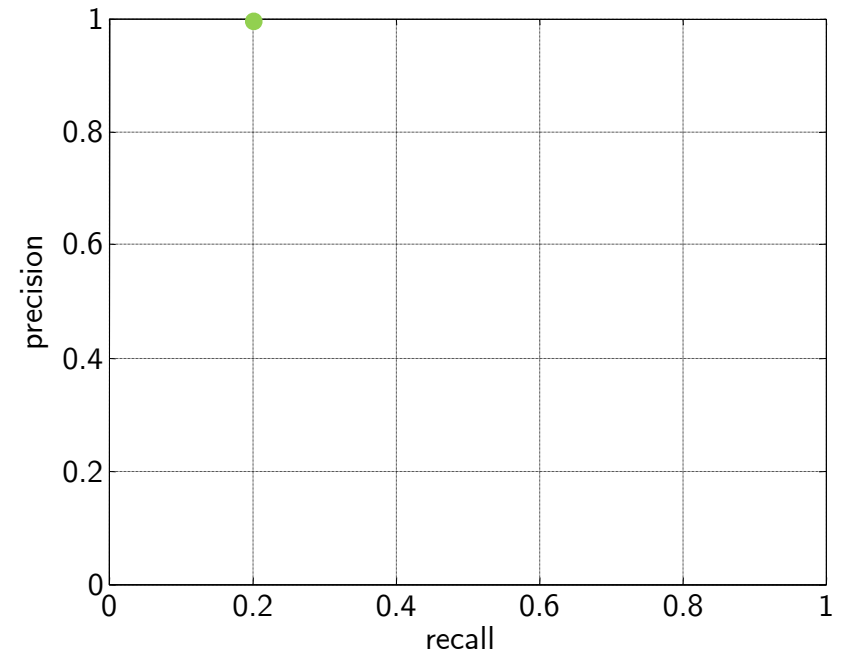
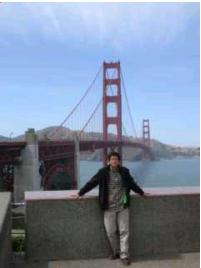


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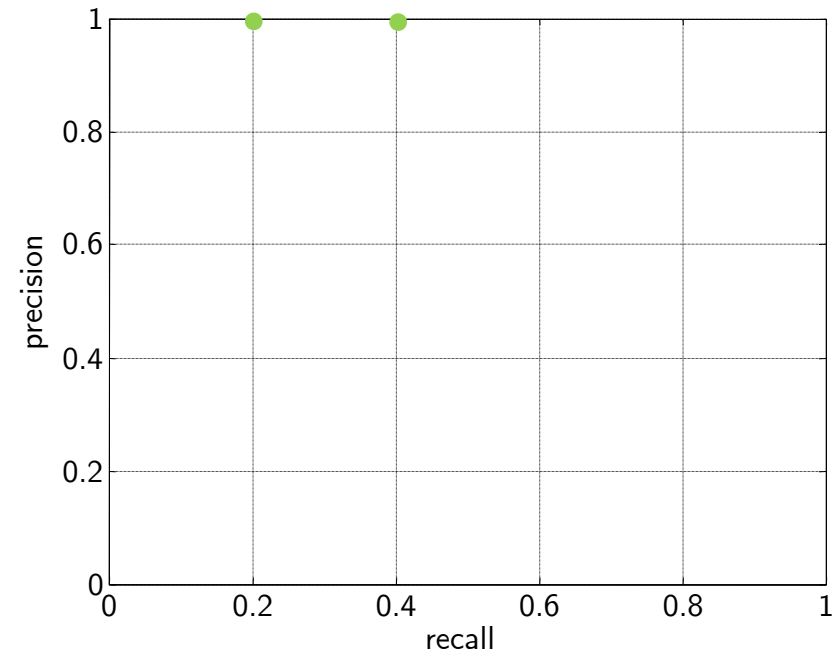


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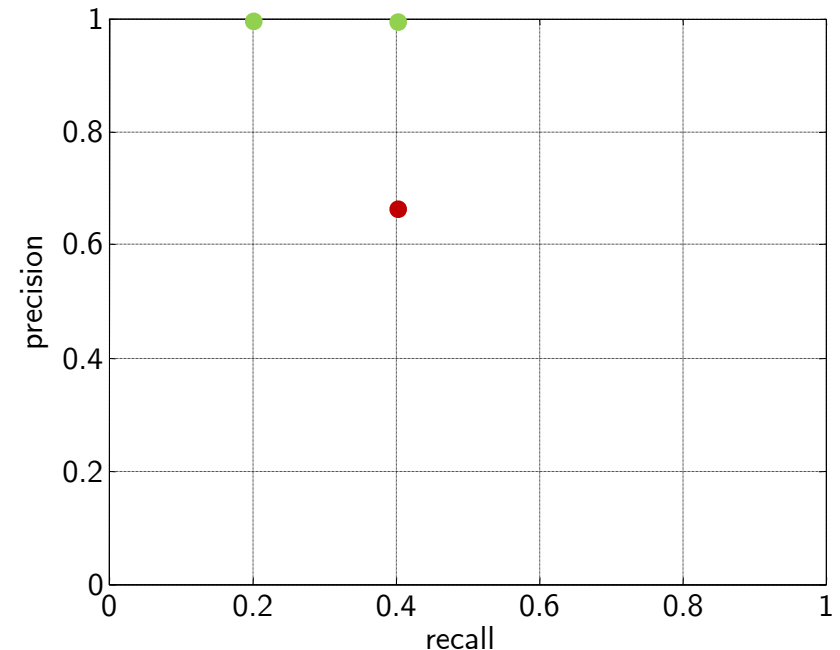
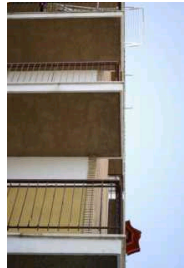


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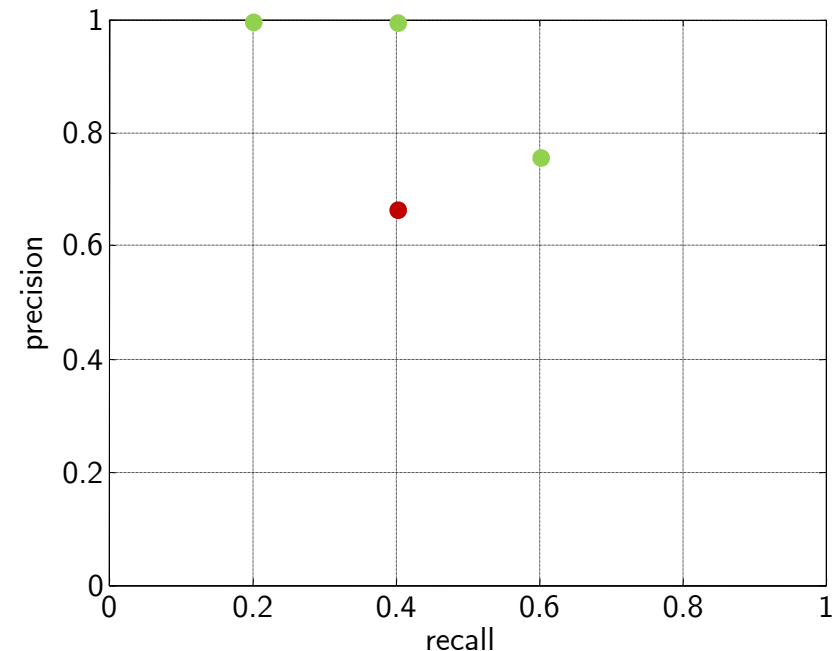
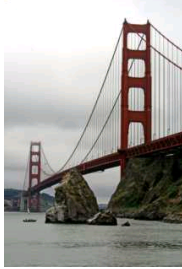
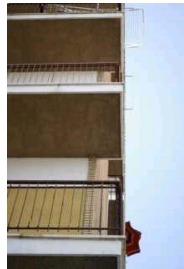
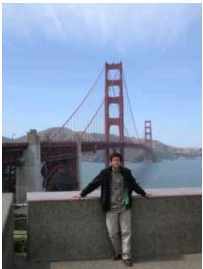


image retrieval - evaluation

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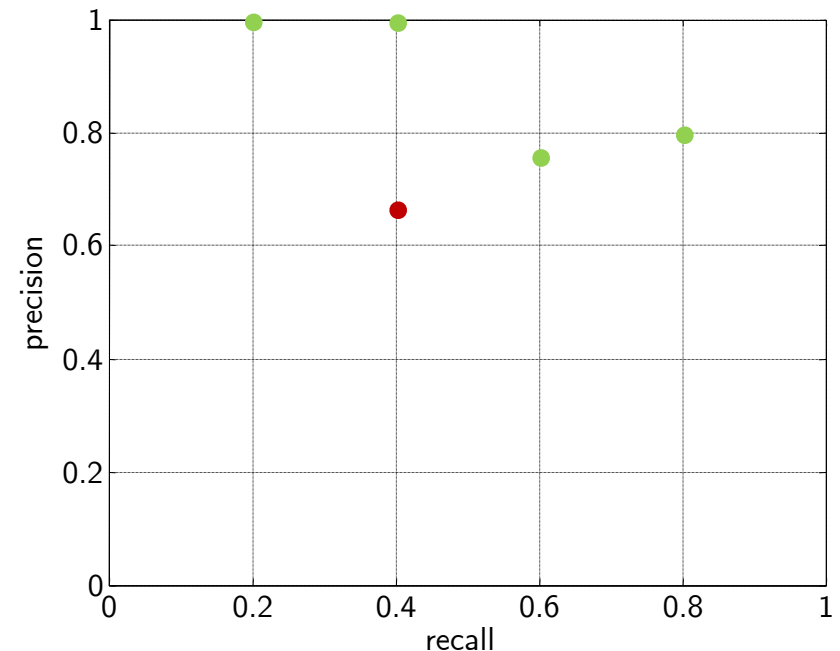
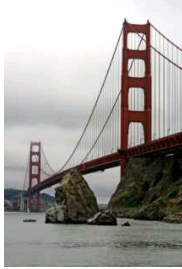
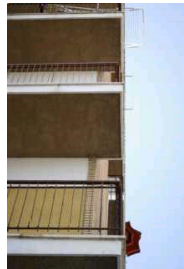
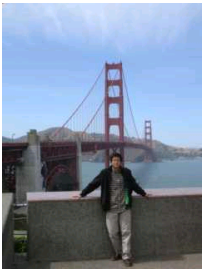


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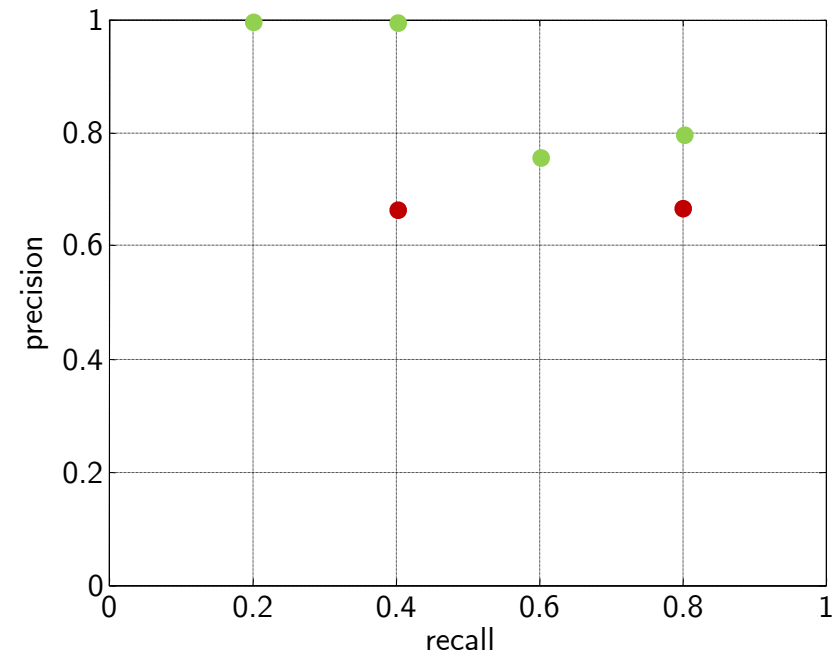
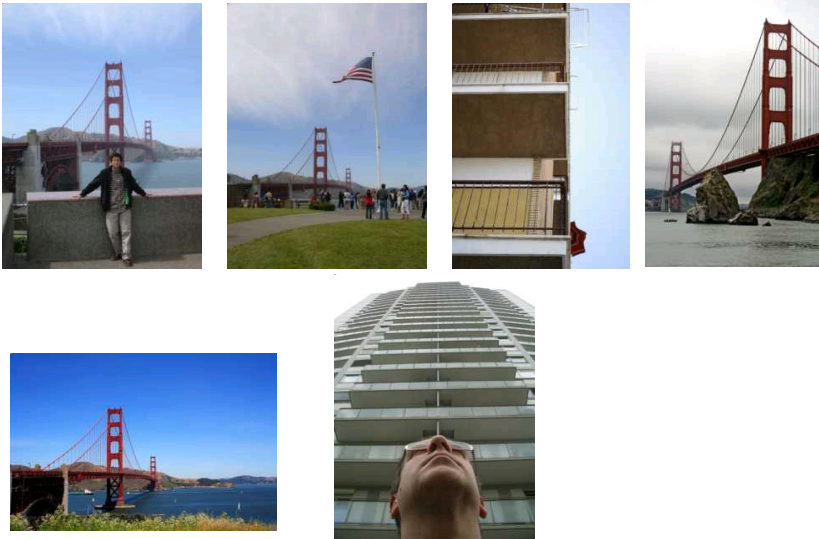


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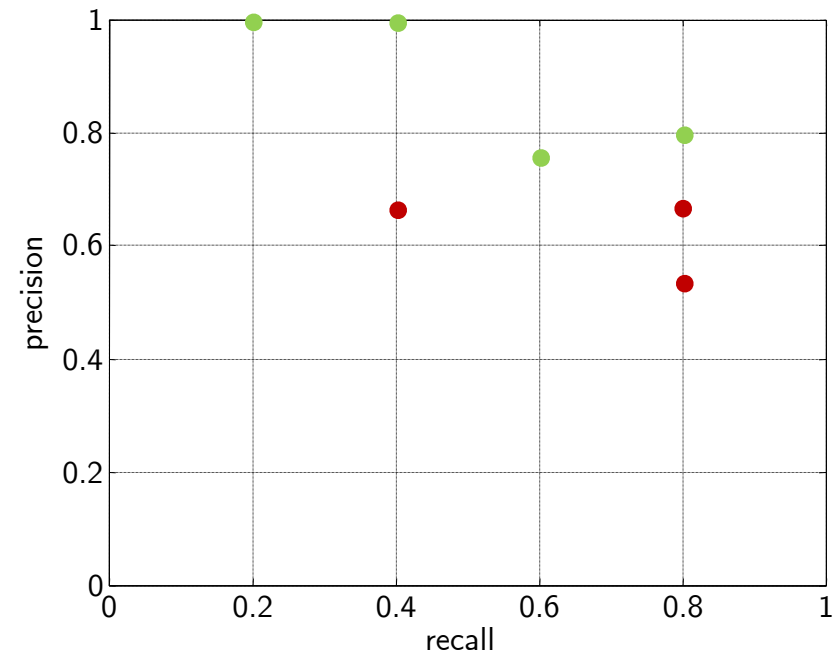
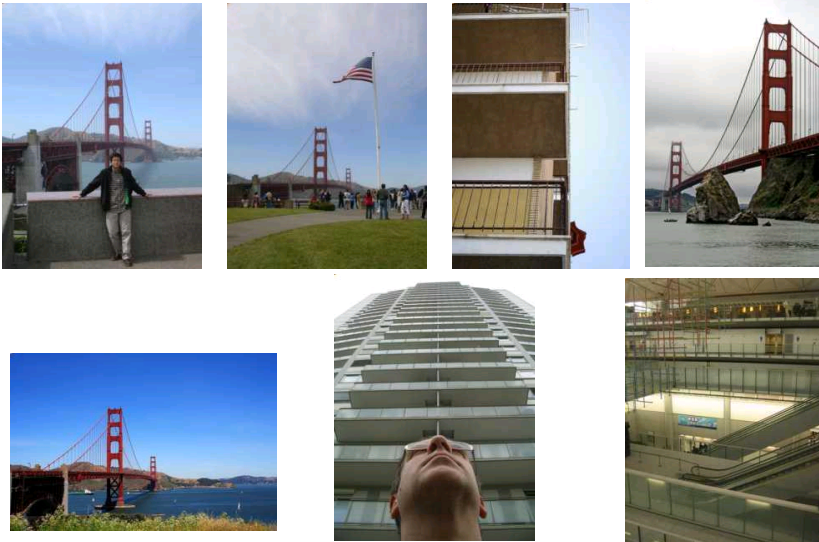


image retrieval - evaluation

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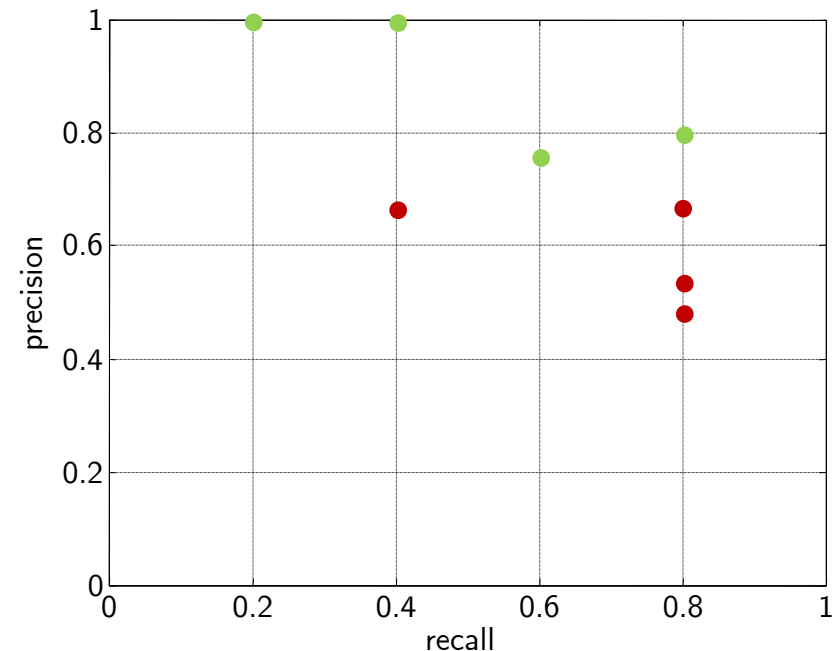
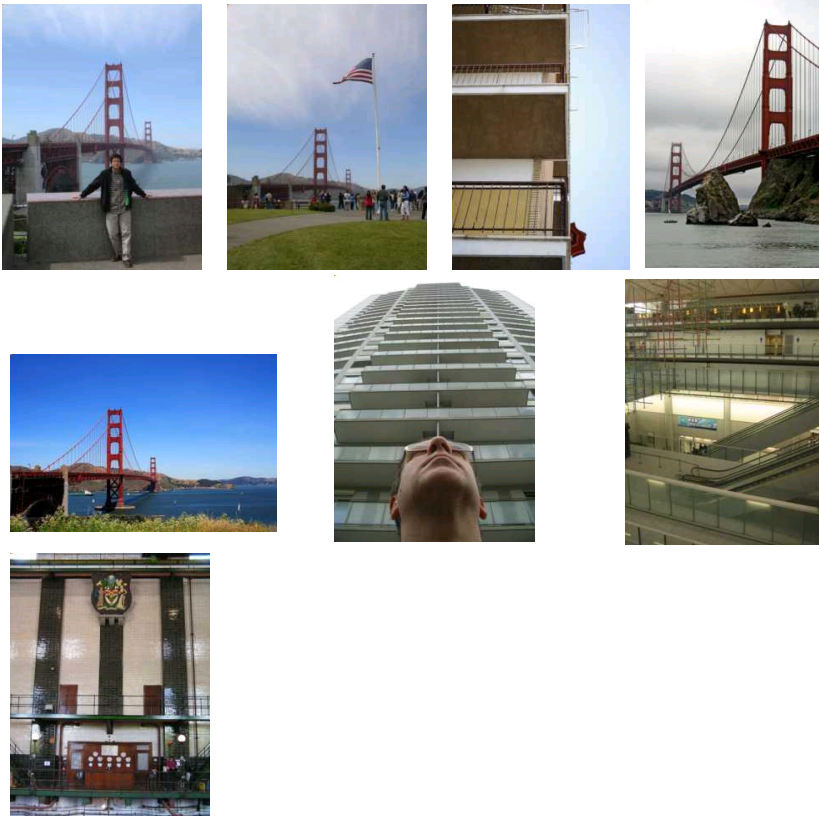


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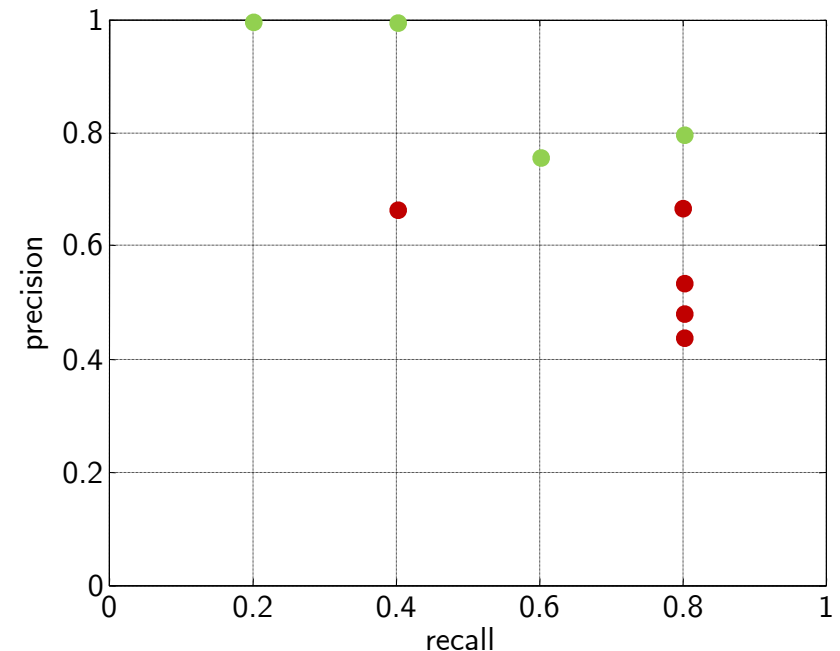
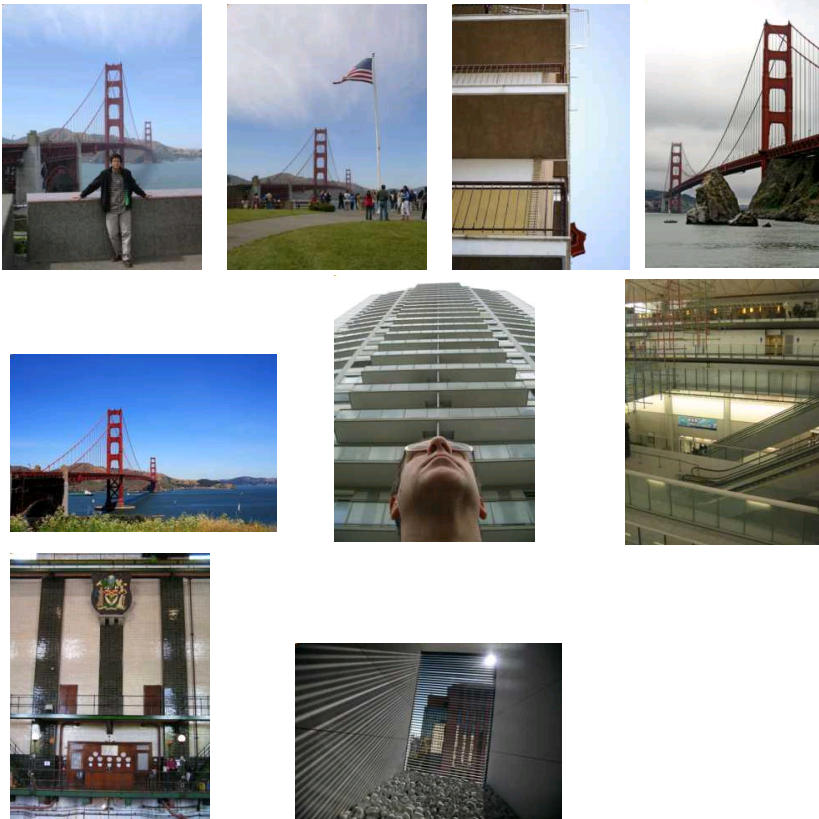


image retrieval - evaluation

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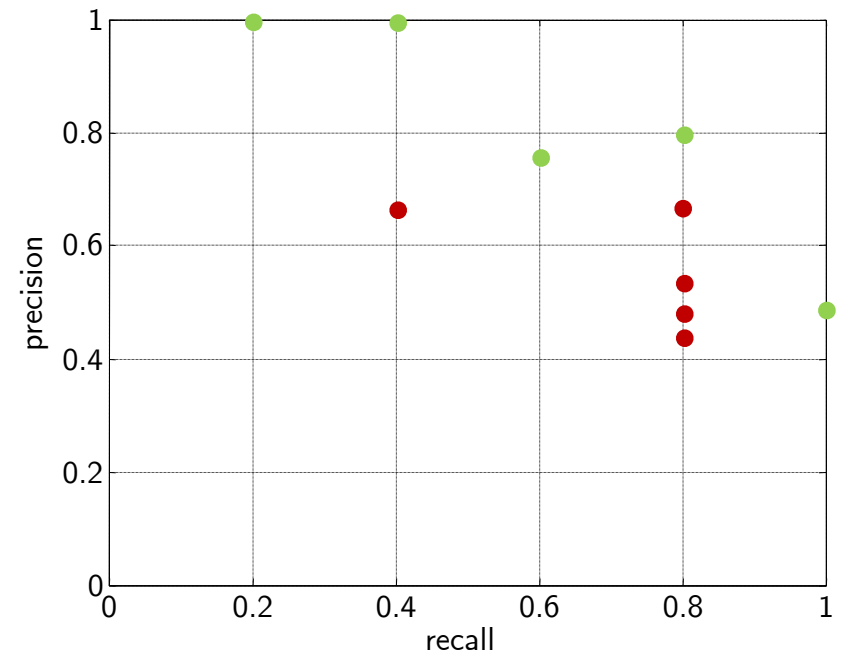
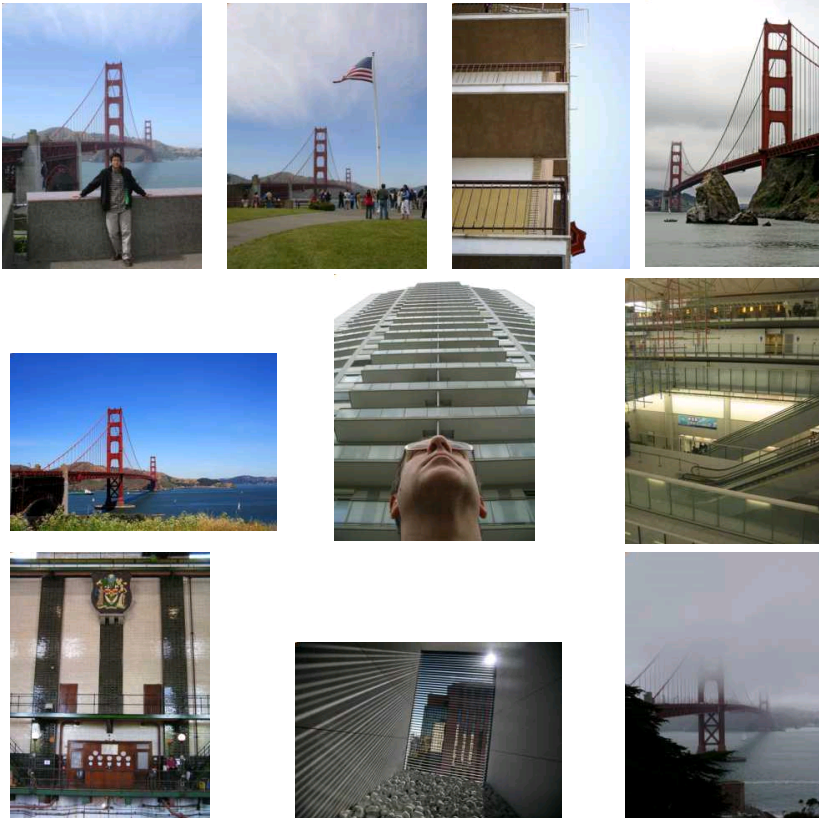


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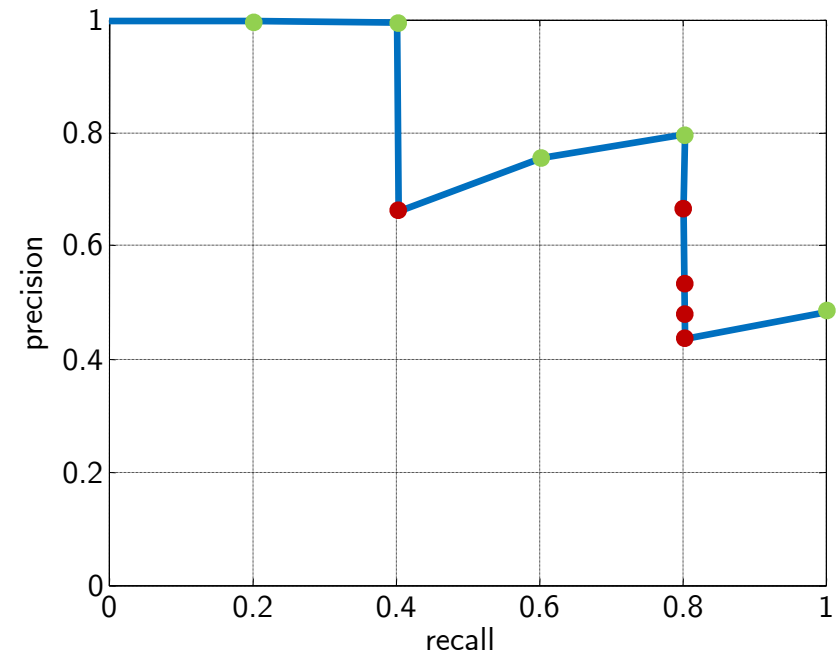
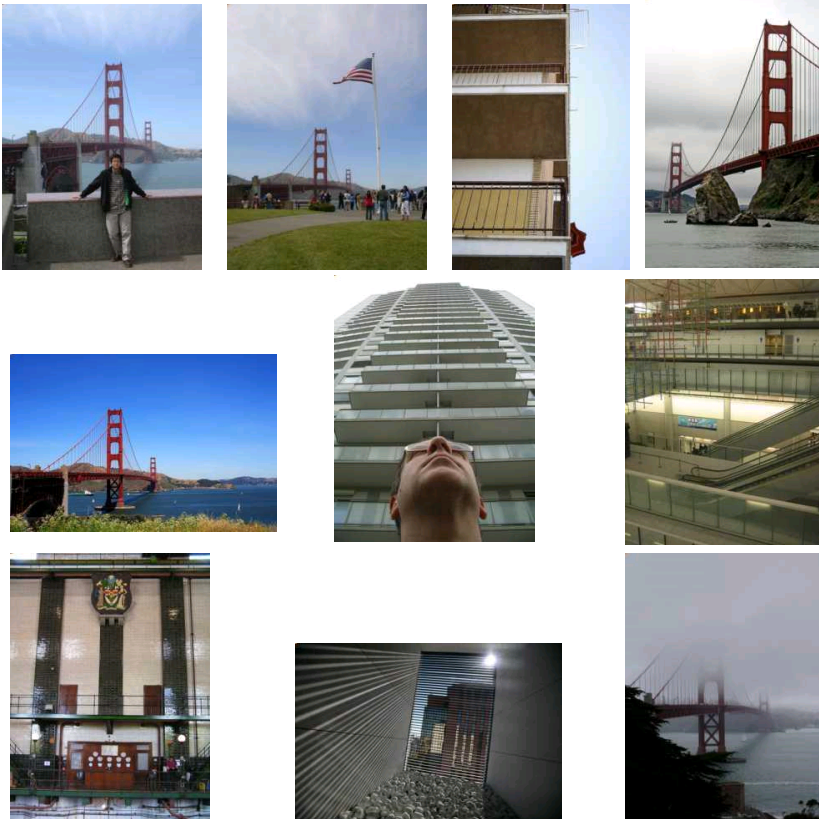


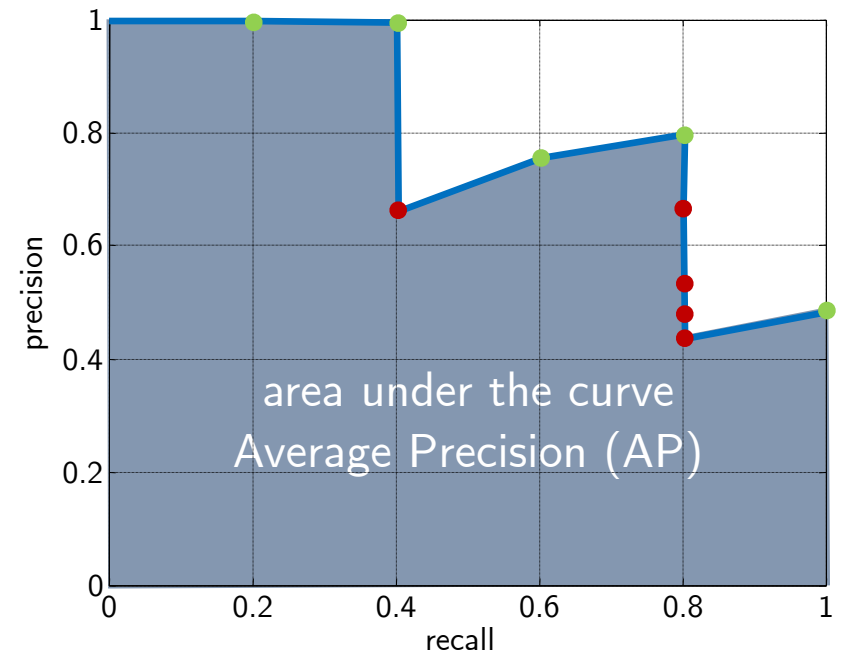
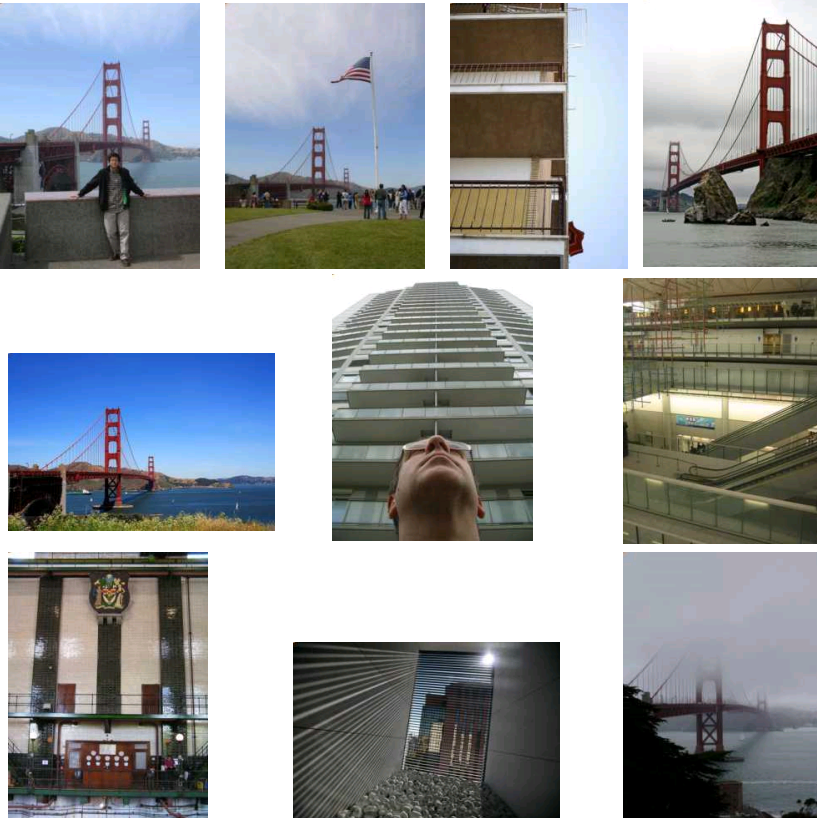
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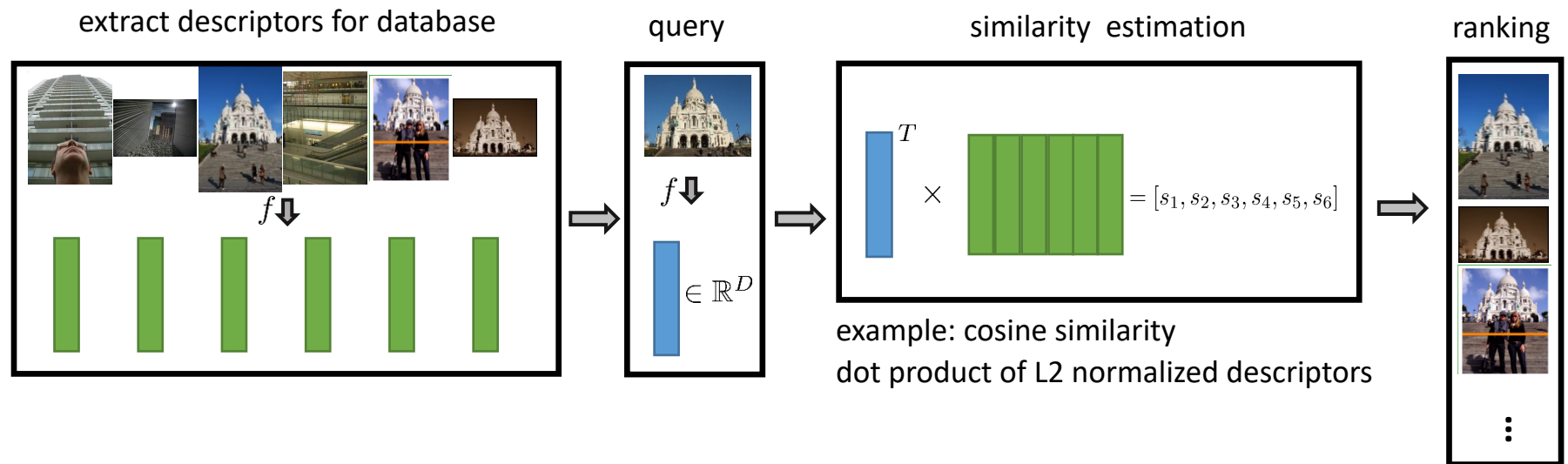
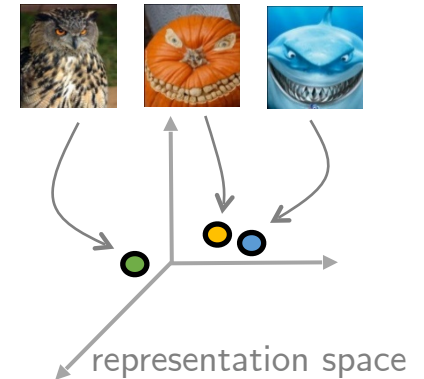
ranking:



visual representation

visual representation – vector space

- map images to a high dimensional representation space
- image descriptor $X = f(\text{image}) \in \mathbb{R}^D$
- function f is hand-crafted or learned
 - so that proximity reflects relevance
- retrieval is performed by nearest neighbor search

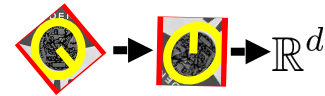


- how to obtain (global) image descriptors?
 - let's revisit local features & descriptors first...

visual representation – local descriptors

$$\mathcal{X} = g(\text{img})$$

$$\mathcal{X} = \{\mathbf{x}\}, \mathbf{x} \in \mathbb{R}^d$$



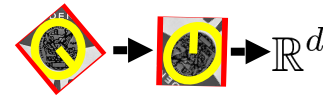
$$X = h(g(\text{img})) = h(\mathcal{X}) \in \mathbb{R}^D$$

visual representation – local descriptors

- represent an image by a set of local descriptors

$$\mathcal{X} = g(\text{image})$$

$$\mathcal{X} = \{\mathbf{x}\}, \mathbf{x} \in \mathbb{R}^d$$



- obtain global descriptor as a function of a local descriptor set

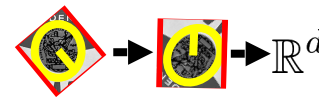
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visual representation – local descriptors

- represent an image by a set of local descriptors

$$\mathcal{X} = g(\text{img})$$

$$\mathcal{X} = \{\mathbf{x}\}, \mathbf{x} \in \mathbb{R}^d$$



- obtain global descriptor as a function of a local descriptor set

$$X = h(g(\text{img})) = h(\mathcal{X}) \in \mathbb{R}^D$$

- inherit their invariance properties
- robustness to occlusions and background clutter

local features

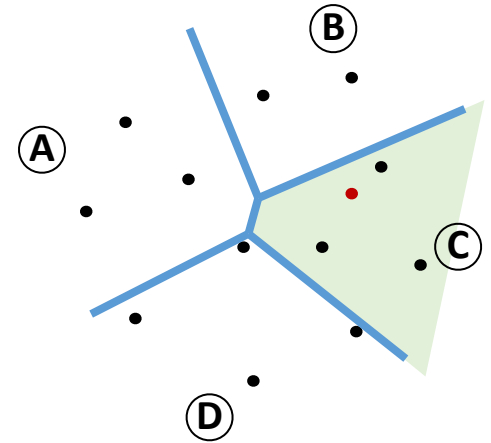


bag-of-words

BoW

bag-of-words - representation

- inspired by natural language processing
 - text document represented by the set of words in it
- quantize the space of local descriptors
 - eg. with k-means clustering
 - each cluster is a visual word
- visual codebook: set of visual words (centroids)

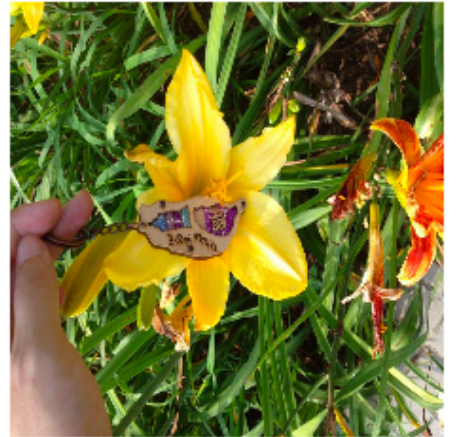


[Sivic & Zisserman. ICCV'03]

[Csurka et al. ECCVW'04]

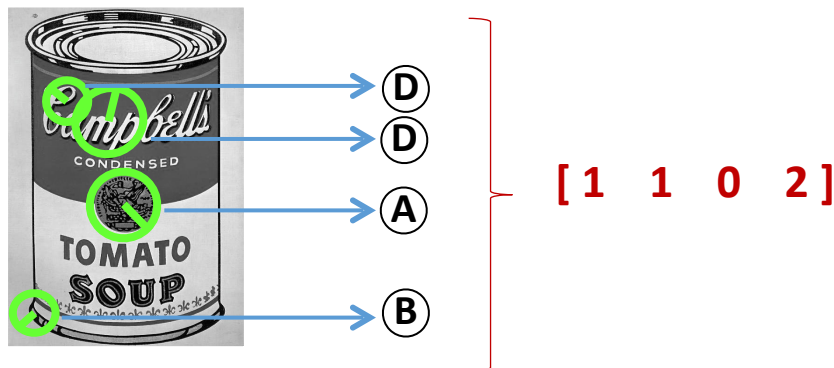
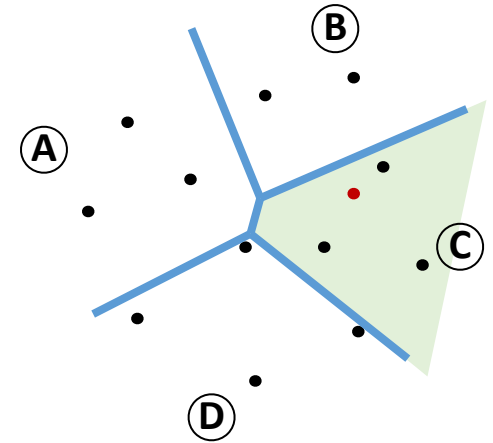
features (patches) in the same cluster





bag-of-words - representation

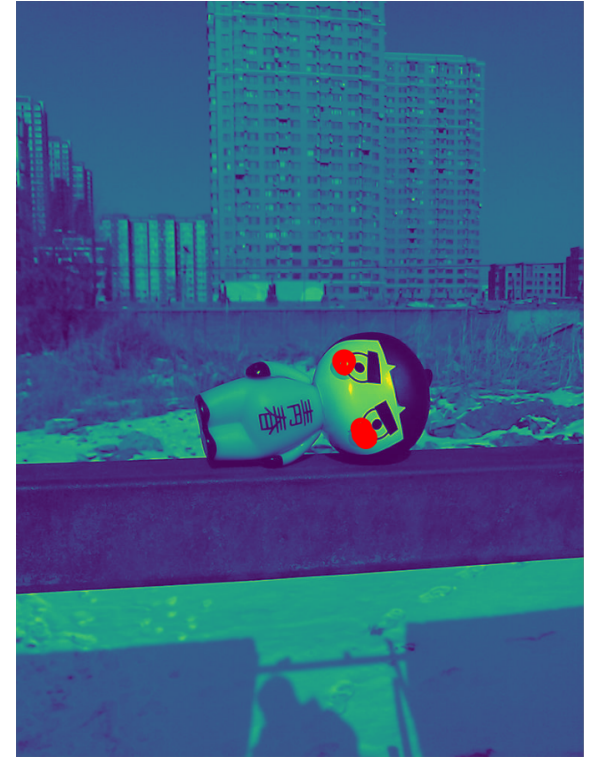
- inspired by natural language processing
 - text document represented by the set of words in it
- quantize the space of local descriptors
 - eg. with k-means clustering
 - each cell (cluster) is a visual word
- visual codebook: set of visual words (centroids)
- assign local descriptors to visual words
 - according to the nearest centroid
- histogram of visual word occurrences (term-frequency) per image



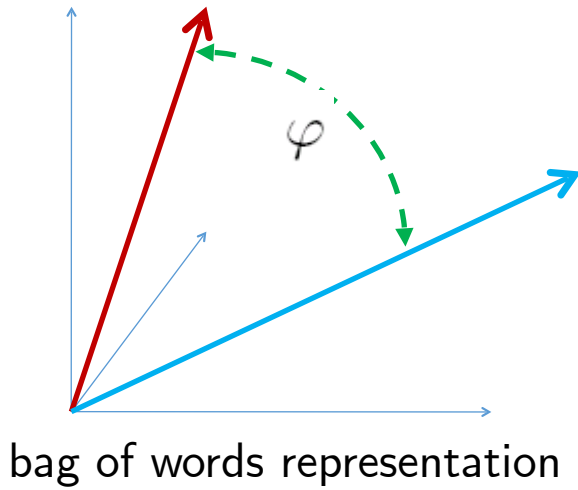
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local features with the same visual word

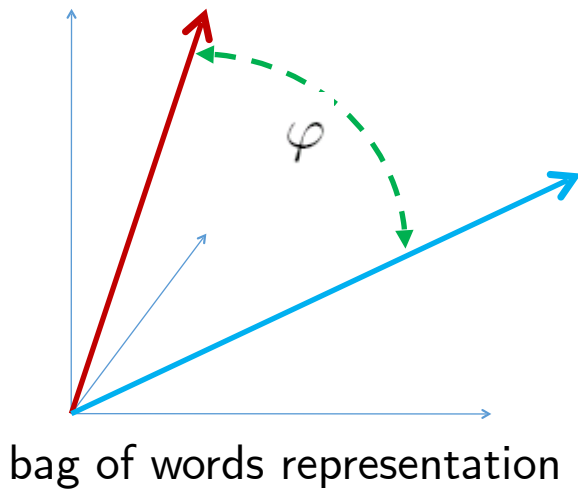


bag-of-words - similarity



$$\cos \varphi = \frac{X^\top Y}{\|X\| \|Y\|} = \frac{1}{\|X\|} \frac{1}{\|Y\|} \sum_{i=1}^K X(i)Y(i)$$

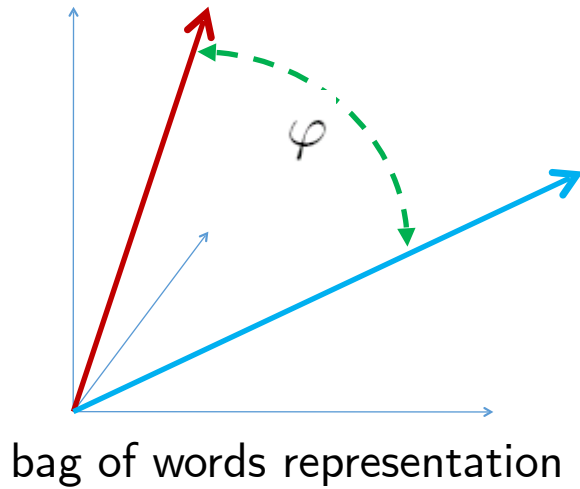
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database	query	score
Ⓐ Ⓑ Ⓒ Ⓓ Y_1 (1002)	Ⓐ Ⓑ Ⓒ Ⓓ 0301	s_1
	• X_q	=

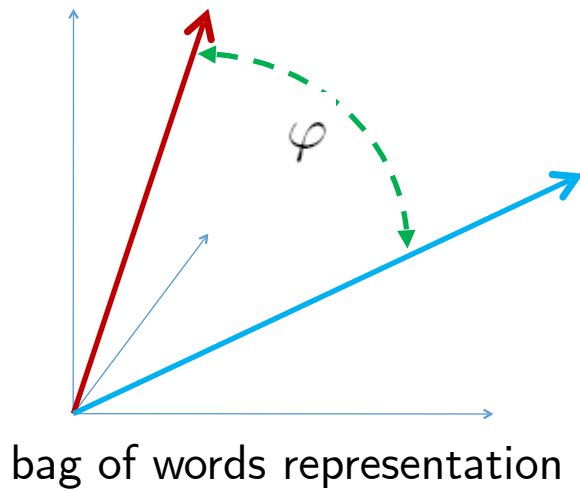
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database	query	score
Y_1 (A) (B) (C) (D)	(A) (B) (C) (D)	
(1) (0) (0) (2)	(0) (3) (0) (1)	s_1
	$\bullet X_q$	

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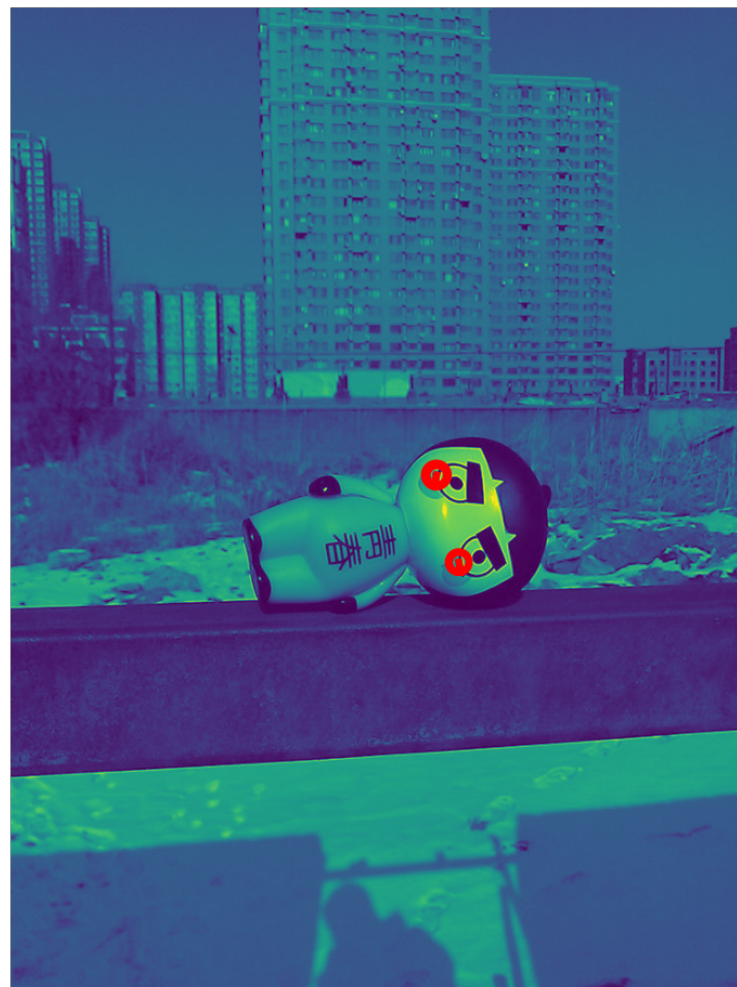
database					query	score
	(A)	(B)	(C)	(D)		
Y_1	(1	0	0	2)	(A) 0	s_1
Y_2	(0	2	0	1)	(B) 3	s_2
Y_3	(1	0	0	0)	(C) 0	s_3
	⋮				(D) 1	⋮

• X_q

local features with the same visual word



local features with the same visual word



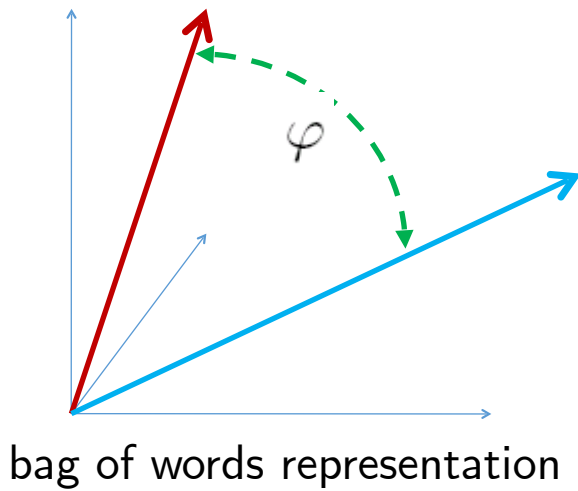
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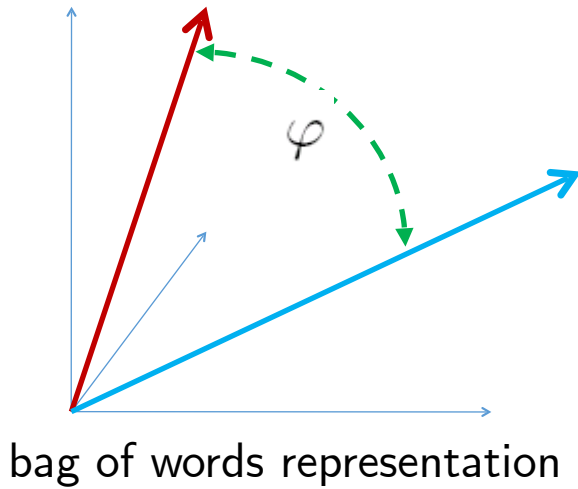


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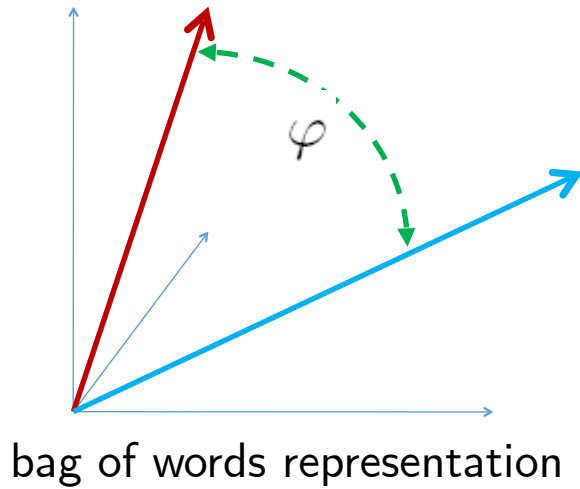
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database	query	score
Ⓐ Ⓑ Ⓒ Ⓓ Y_1 (1 0 0 2)	Ⓐ • X_q Ⓑ Ⓒ Ⓓ 0 3 0 1	s_1 =

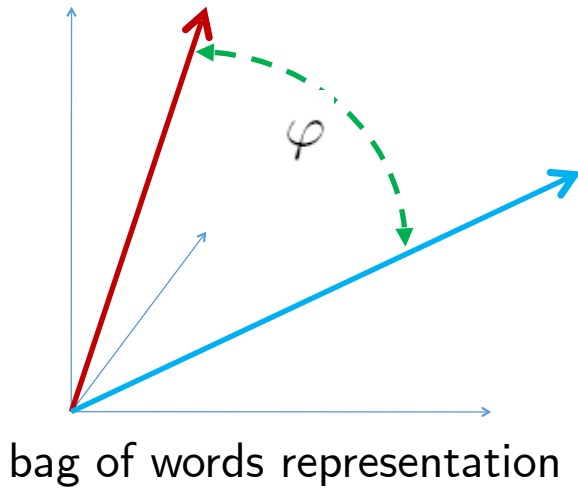
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database	query	score
Y_1 (A) (B) (C) (D)	(A) (B) (C) (D)	
(1) (0) (0) (2)	(0) (3) (0) (1)	s_1
	• X_q	

bag-of-words - similarity

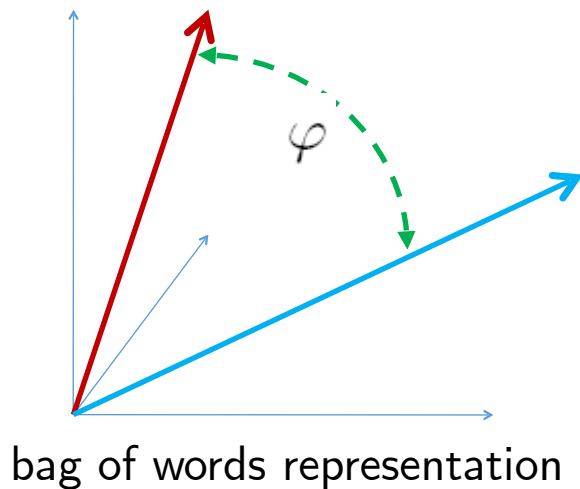


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database					query	score
	(A)	(B)	(C)	(D)		
Y_1	(1	0	0	2)	(A) 0	s_1
Y_2	(0	2	0	1)	(B) 3	s_2
Y_3	(1	0	0	0)	(C) 0	s_3
	⋮				(D) 1	⋮

• X_q

bag-of-words - similarity

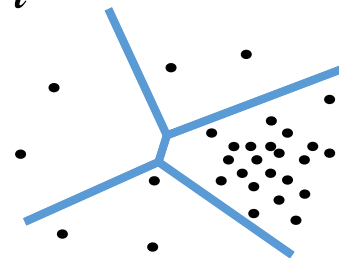


$$\cos \varphi = \frac{X^T Y}{\|X\| \|Y\|} = \frac{1}{\|X\|} \frac{1}{\|Y\|} \sum_{i=1}^K X(i) Y(i)$$

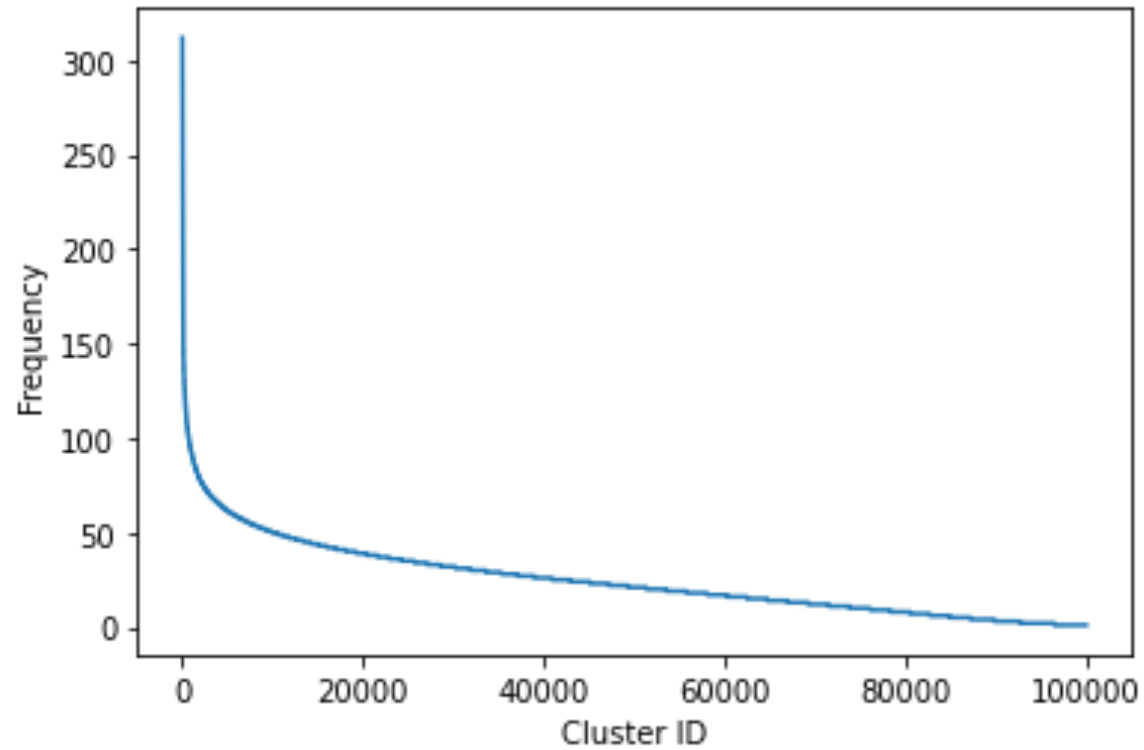
database	query	score
Ⓐ Ⓑ Ⓒ Ⓓ Y_1 (1 0 0 2) Y_2 (0 2 0 1) Y_3 (1 0 0 0) ⋮	Ⓐ Ⓑ Ⓒ Ⓓ X_q	s_1 s_2 s_3 ⋮

■ inverse-document-frequency (idf):

- multiply dimension i with $w_i = \log \frac{\# \text{ images}}{\# \text{ images with word } i}$
- down-weights highly populated visual words



cluster sizes



cluster size = 312



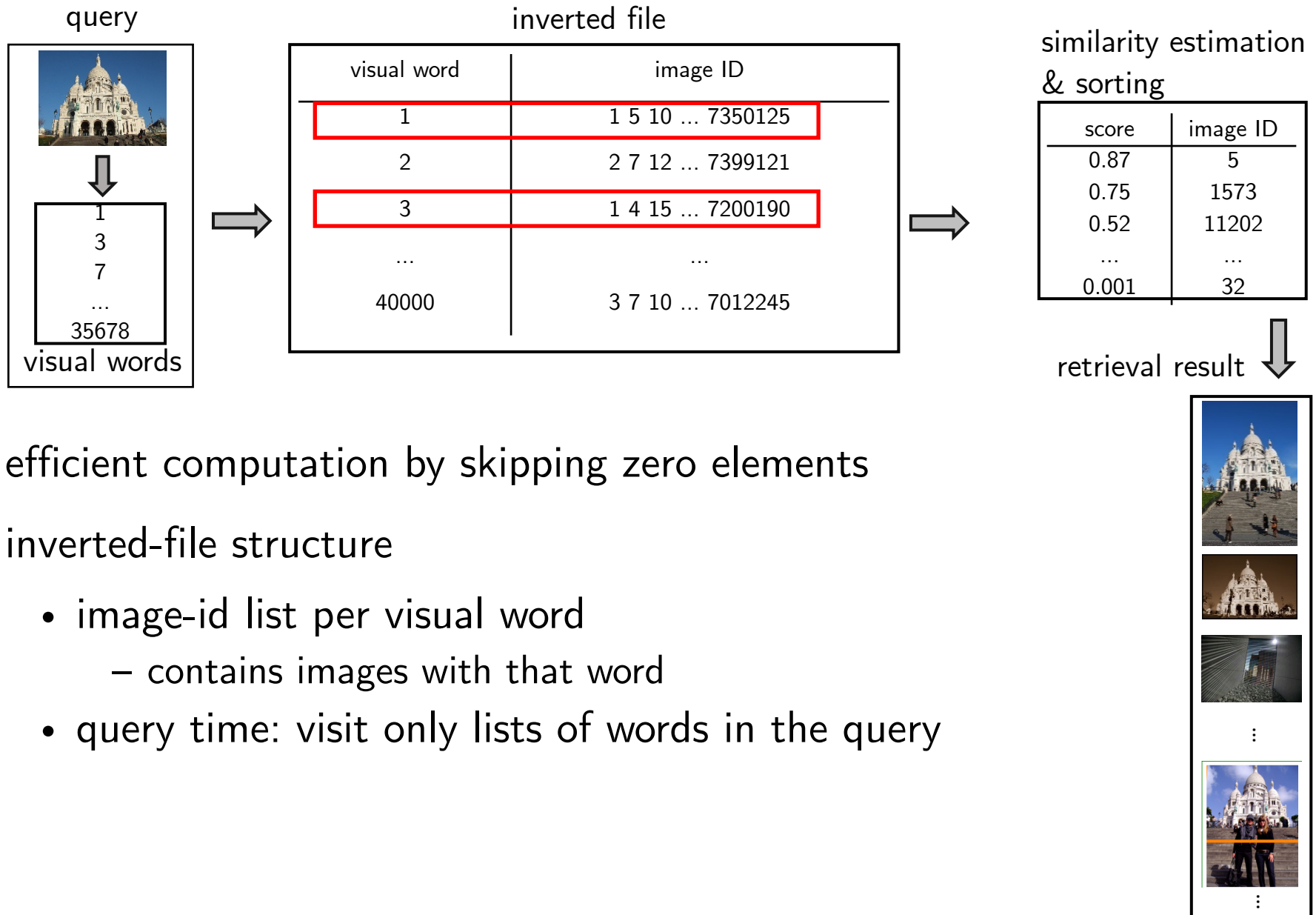
cluster size = 92



cluster size = 92



bag-of-words – retrieval

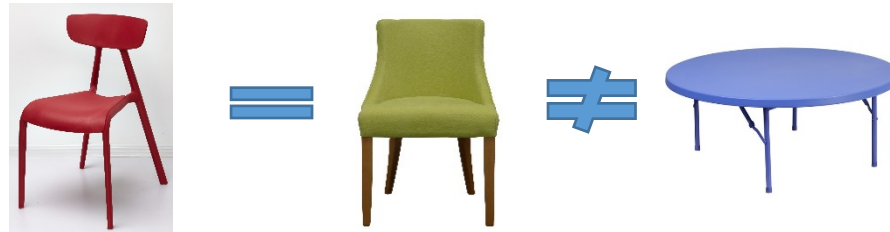


- efficient computation by skipping zero elements
- inverted-file structure
 - image-id list per visual word
 - contains images with that word
 - query time: visit only lists of words in the query

impact of codebook size

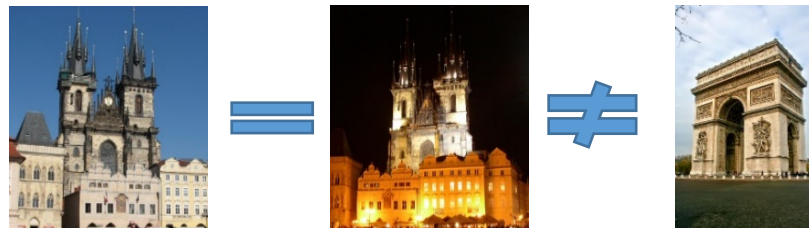
■ small (eg. 128)

- dense representation: compatible with approximate NN search
- memory: $\# \text{images} \times \text{codebook-size} \times \text{descriptor-element-footprint}$
- appropriate for category-level matching



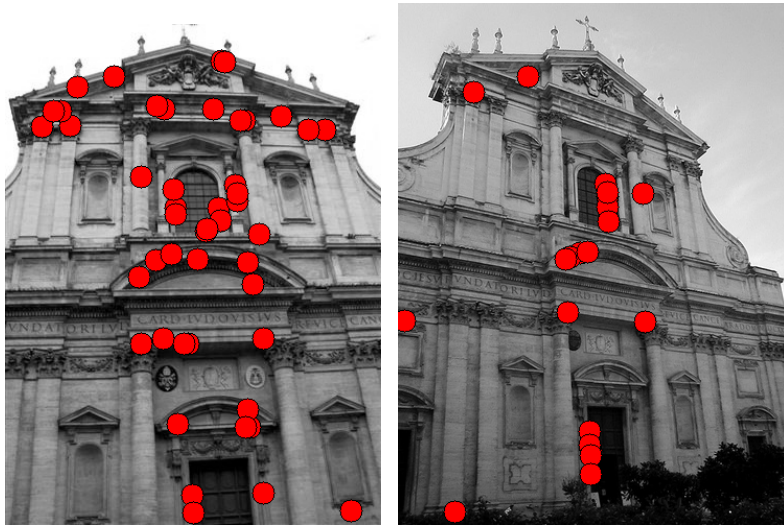
■ very large (eg. 10^6)

- sparse representation: use of inverted-file
- memory: $\text{total-number-of-features} \times \text{image-id-footprint}$
- appropriate for instance-level matching

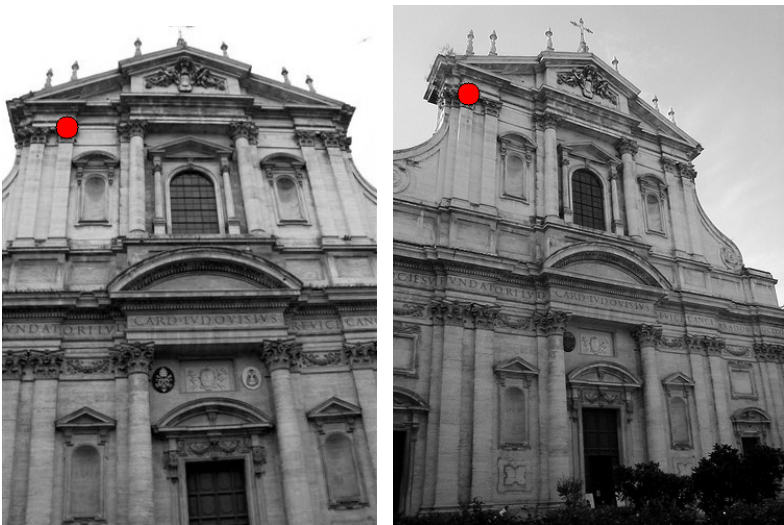


bag-of-words - example

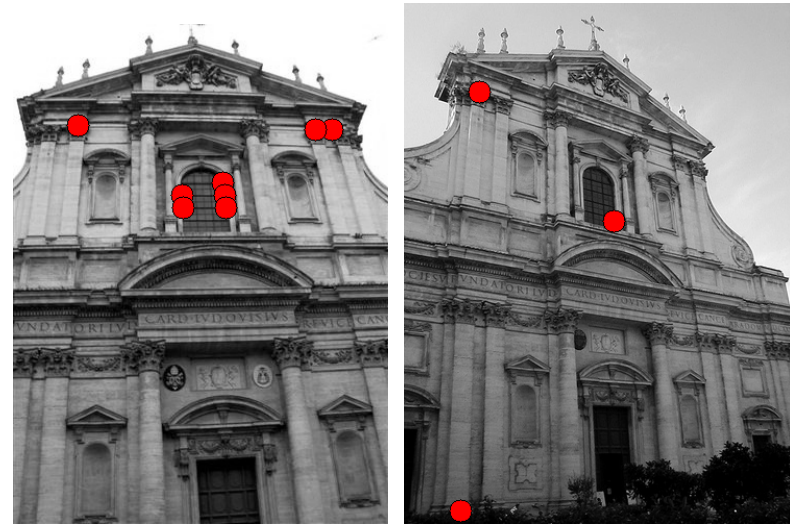
- local descriptors mapped to the same visual word for different codebook size



64 visual words



10^6 visual words



10^3 visual words

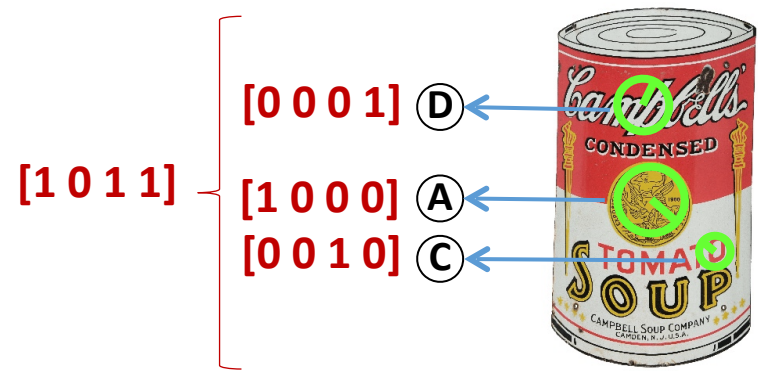
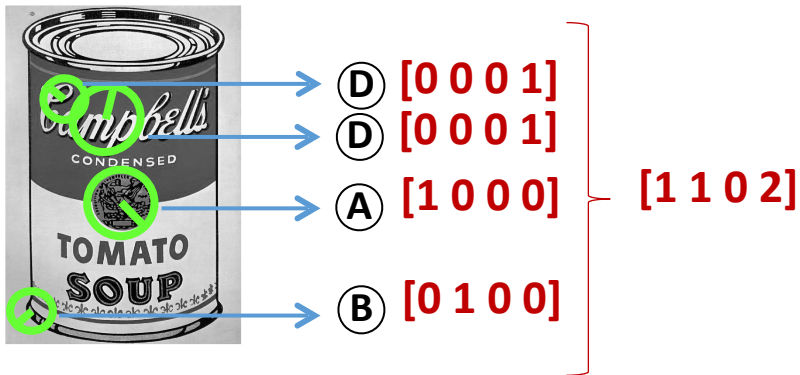
BoW & other approaches

from a different point of view

bag-of-words

$$S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$$

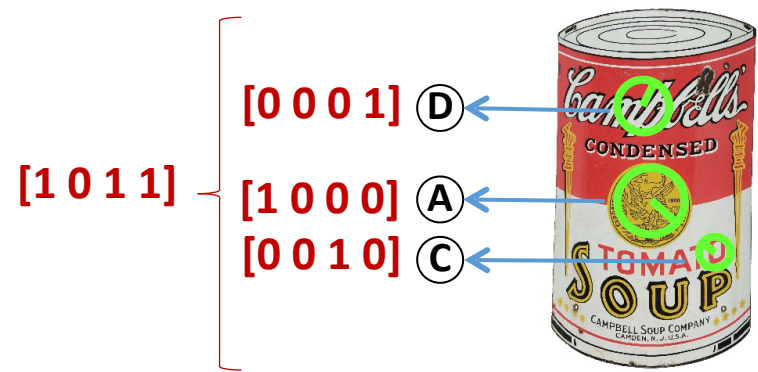
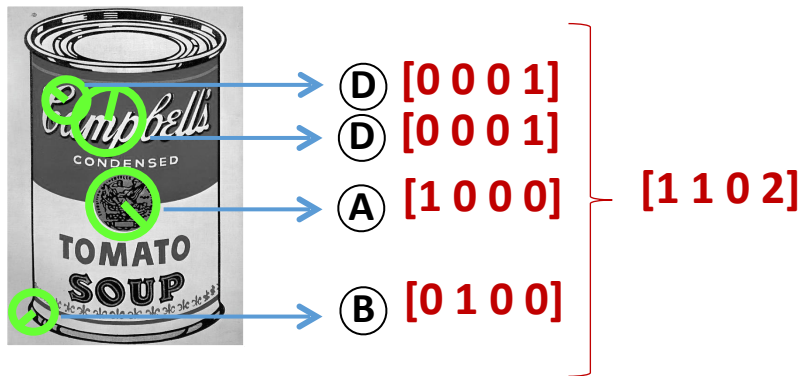
- local embedding: $\phi(\mathbf{x}) = [0, \dots, 1, \dots, 0]^\top$, $\mathbf{x}$ assigned to word $q(\mathbf{x})$
 $q(\mathbf{x})$ -th element



bag-of-words

image similarity $\rightarrow S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$

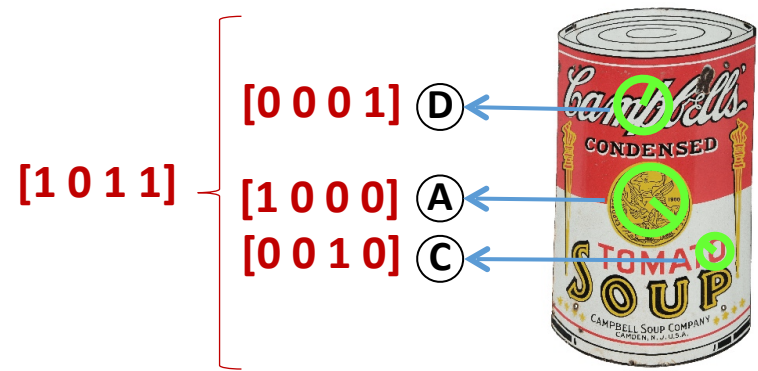
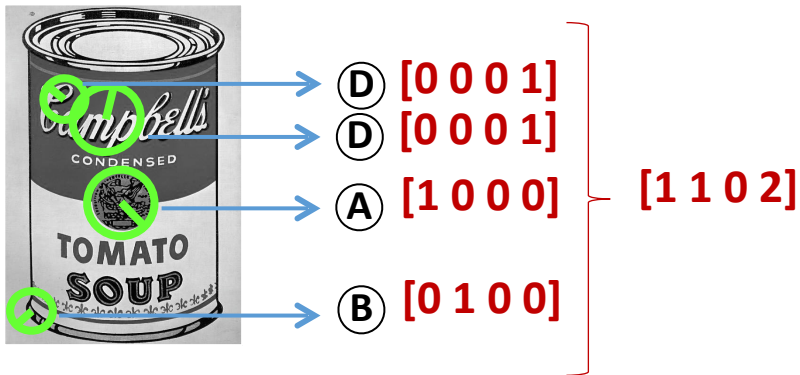
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bag-of-words

image similarity $\rightarrow S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$ global descriptor

- local embedding: $\phi(\mathbf{x}) = [0, \dots, 1, \dots, 0]^\top$, $\mathbf{x}$ assigned to word $q(\mathbf{x})$
 $q(\mathbf{x})$ -th element

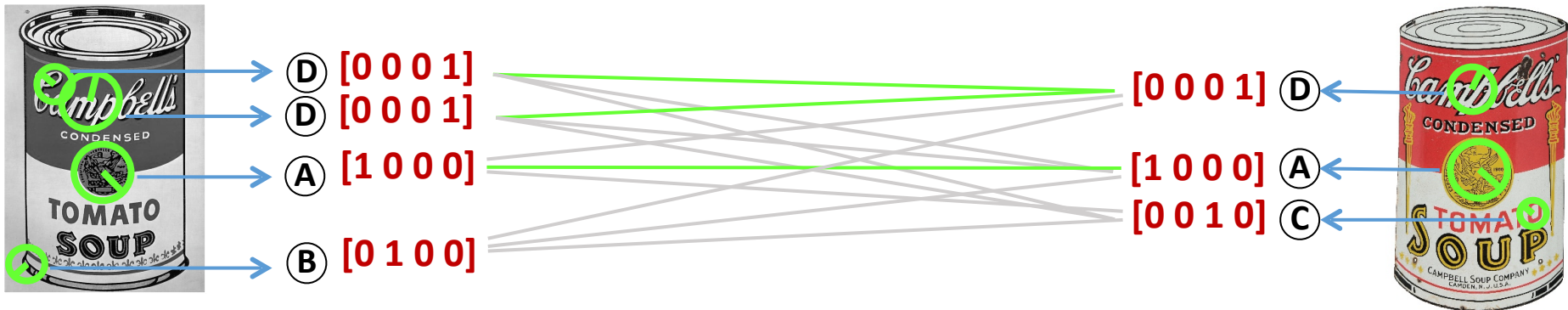


bag-of-words

image similarity $\rightarrow$ $S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$ global descriptor

$= \sum_{\mathbf{x} \in \mathcal{X}} \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{x})^\top \phi(\mathbf{y})$ voting approach

- local embedding: $\phi(\mathbf{x}) = [0, \dots, 1, \dots, 0]^\top$, $\mathbf{x}$ assigned to word $q(\mathbf{x})$
 $q(\mathbf{x})$ -th element



bag-of-words

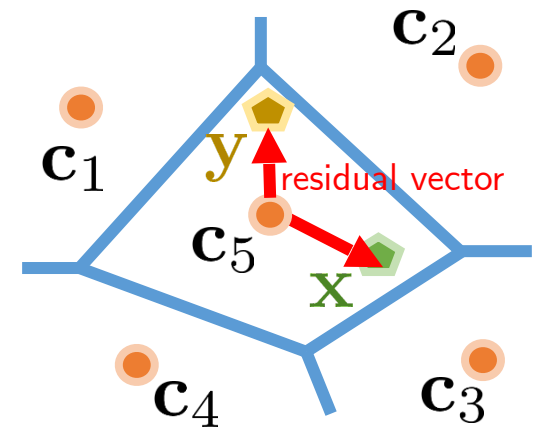
image similarity $\rightarrow$ $S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$ global descriptor

$= \sum_{\mathbf{x} \in \mathcal{X}} \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{x})^\top \phi(\mathbf{y})$ voting approach

- local embedding: $\phi(\mathbf{x}) = [0, \dots, \mathbf{1}, \dots, 0]^\top$, $\mathbf{x}$ assigned to word $q(\mathbf{x})$
 $q(\mathbf{x})$ -th element
- same result achieved in two ways:
 - voting approach: accumulate local similarity of all pairs
 - dot product of two vectors (efficient)
- accumulate 0 if different visual word, 1 (or idf) if same visual word
 - what about more fine-grained votes?

vector of locally aggregated descriptors (VLAD)

- fine-grained votes equal to
 - 0, if $q(\mathbf{x}) \neq q(\mathbf{y})$ (different visual words)
 - $r(\mathbf{x})^\top r(\mathbf{y})$, if $q(\mathbf{x}) = q(\mathbf{y})$ (same visual word)
- residual vector $r(\mathbf{x}) = \mathbf{x} - \mathbf{c}_{q(\mathbf{x})}$
- local embedding $\phi(\mathbf{x}) = [\mathbf{0}^\top, \dots, r(\mathbf{x})^\top, \dots, \mathbf{0}^\top]^\top$
 $q(\mathbf{x})$ -th sub-vector



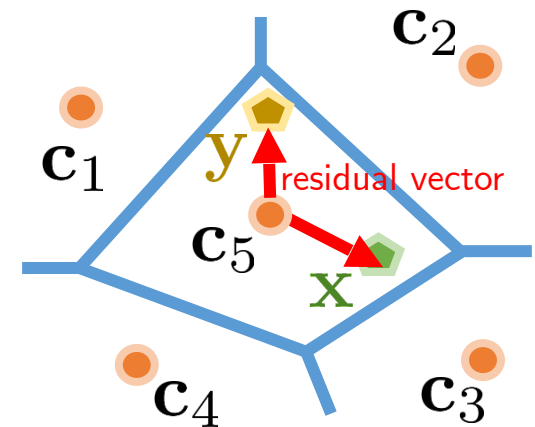
vector of locally aggregated descriptors (VLAD)

- voting approach
 - intuitive but inefficient

$$S(\mathcal{X}, \mathcal{Y}) \propto \sum_{\mathbf{x} \in \mathcal{X}} \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{x})^\top \phi(\mathbf{y})$$

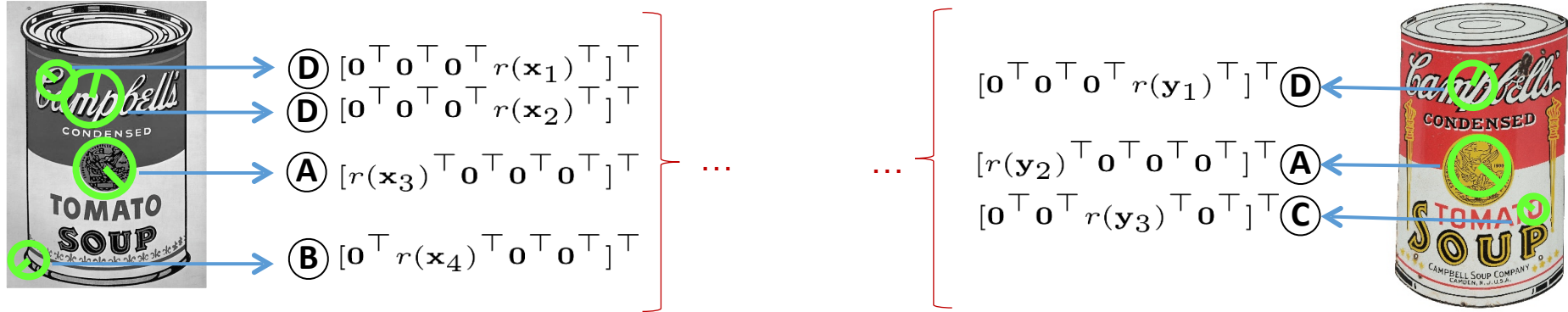
- global descriptor similarity
 - efficient via dot product (dK dimensions)

$$S(\mathcal{X}, \mathcal{Y}) \propto \left(\sum_{\mathbf{x} \in \mathcal{X}} \phi(\mathbf{x}) \right)^\top \sum_{\mathbf{y} \in \mathcal{Y}} \phi(\mathbf{y})$$



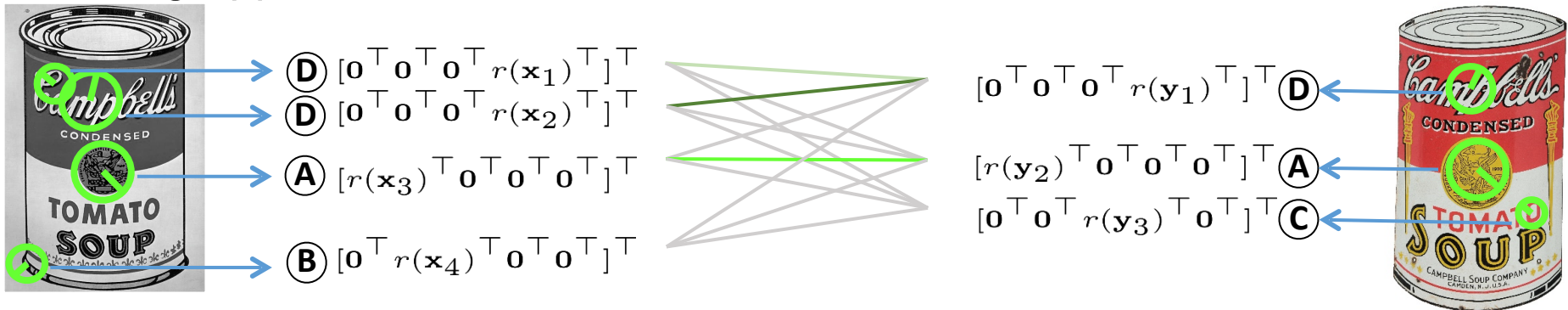
vector of locally aggregated descriptors (VLAD)

■ global descriptor similarity



- sum to obtain global descriptors
- dot product for similarity

■ voting approach



- non-binary votes
- according to descriptor similarity

VLAD and related approaches

■ VLAD variations

- use L2 normalized residuals [Delhumeau et al. ACMMM'13]
 - only angles matter
- L2 normalization of each d-dimensional VLAD sub-vector
 - handles features from repeating patterns
 - [Arandjelovic & Zisserman, CVPR'13]

■ Fisher vectors [Perronnin et al. CVPR'10]

- Gaussian-Mixture-Model instead of k-means
- different derivation: gradient log-likelihood of local descriptors
- soft-assign to all visual words
- residual vectors normalized (divided) by cluster variance

selective match kernel (SMK)

- use a local similarity function to estimate votes

$$S(\mathcal{X}, \mathcal{Y}) \propto \sum_{\mathbf{x} \in \mathcal{X}} \sum_{\mathbf{y} \in \mathcal{Y}} \hat{s}(\phi(\mathbf{x})^\top \phi(\mathbf{y}))$$

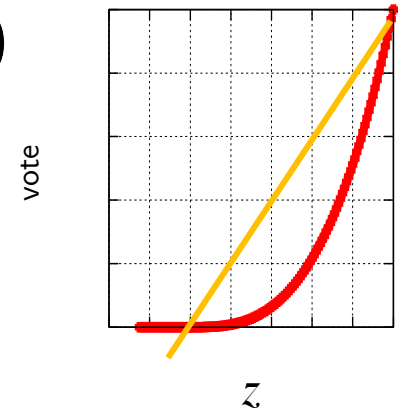
residual vector

- equivalently iterate over common visual words $\mathcal{W}$ between $\mathcal{X}$ and $\mathcal{Y}$

$$S(\mathcal{X}, \mathcal{Y}) \propto \sum_{k \in \mathcal{W}} \sum_{\mathbf{x} \in \mathcal{X}_k} \sum_{\mathbf{y} \in \mathcal{Y}_k} s(\phi(\mathbf{x})^\top \phi(\mathbf{y})), \text{ where } \mathcal{X}_k = \{\mathbf{x} : q(\mathbf{x}) = k\}$$

- non-linear local similarity function (more selective votes)

$$s(z) = \begin{cases} z^\alpha, & \text{if } z > t \\ 0, & \text{otherwise} \end{cases}$$



- only seen as a voting approach
 - no equivalence to global descriptor. **why?**

impact of the local similarity function

- numerical example:

- exponent $\alpha = 1$

- $[0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5] \rightarrow 2.5$

- $[0.7 \ 0.7 \ 0.7 \ 0.2 \ 0.2] \rightarrow 2.5$

- exponent $\alpha = 2$

- $[0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5] \rightarrow 1.25$

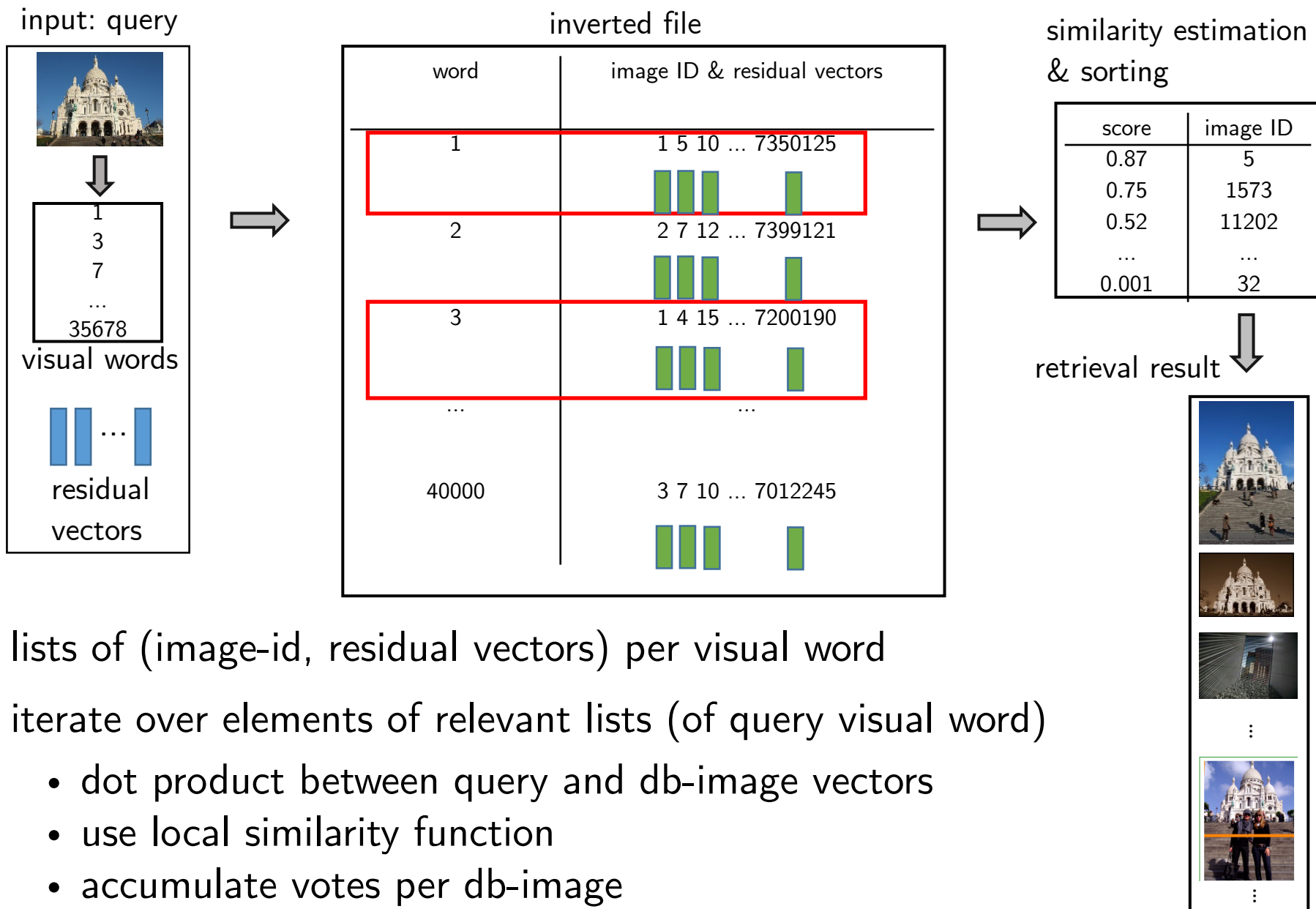
- $[0.7 \ 0.7 \ 0.7 \ 0.2 \ 0.2] \rightarrow 1.55$

- exponent $\alpha = 3$

- $[0.5 \ 0.5 \ 0.5 \ 0.5 \ 0.5] \rightarrow 0.62$

- $[0.7 \ 0.7 \ 0.7 \ 0.2 \ 0.2] \rightarrow 1.05$

SMK – retrieval



- lists of (image-id, residual vectors) per visual word
- iterate over elements of relevant lists (of query visual word)
 - dot product between query and db-image vectors
 - use local similarity function
 - accumulate votes per db-image

settings for identical object retrieval

■ BoW

- very large codebook (eg. 10^6)
- compatible with inverted-file
- lower memory requirements than SMK but less precise
- provides tentative correspondences

■ VLAD

- small codebook (eg. 128)
- dimensionality reduction
- small memory footprint
- efficient search
 - compatible with approximate nearest neighbor search methods

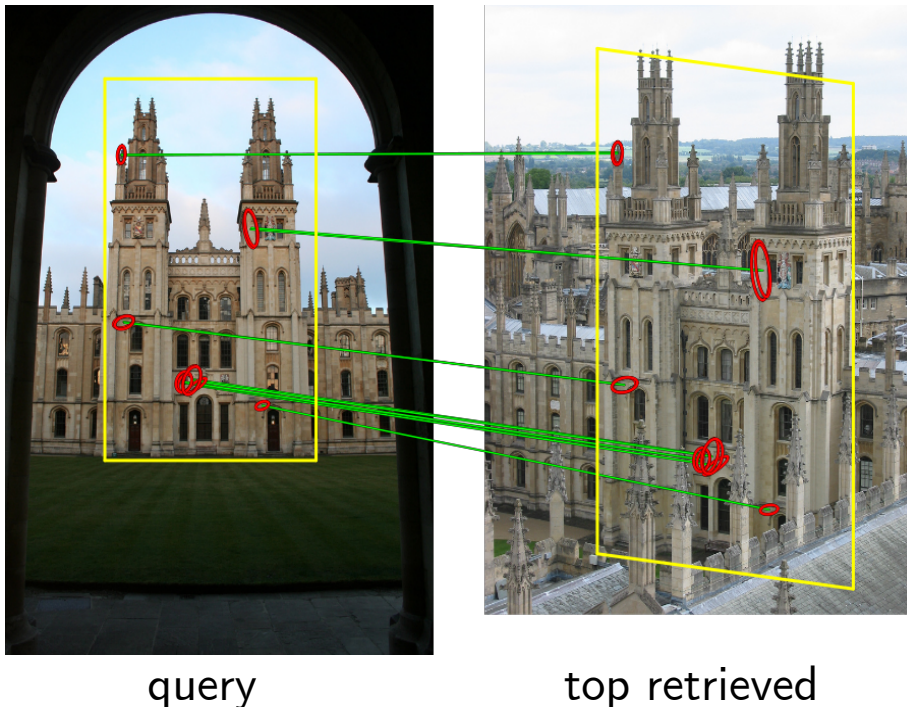
■ SMK

- large codebook (eg. 65k)
- compatible with inverted-file
- memory demanding and slower search than BoW but better performance
- provides tentative correspondences

fast spatial matching

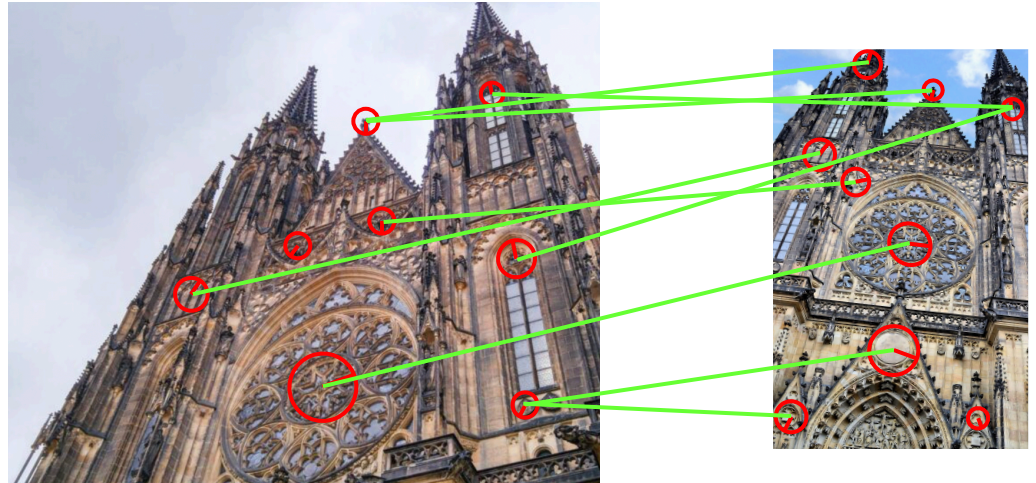
spatial matching and verification

- RANSAC-like approach to find inlier correspondences
 - find the geometric transformation with the largest number of inliers
 - use the number of inliers as image-to-image similarity
- 1st stage of retrieval: rank all images with BoW
- 2nd stage: re-rank top-ranked images according to the number of inliers
 - efficiency is important → method inspired by RANSAC but sped-up

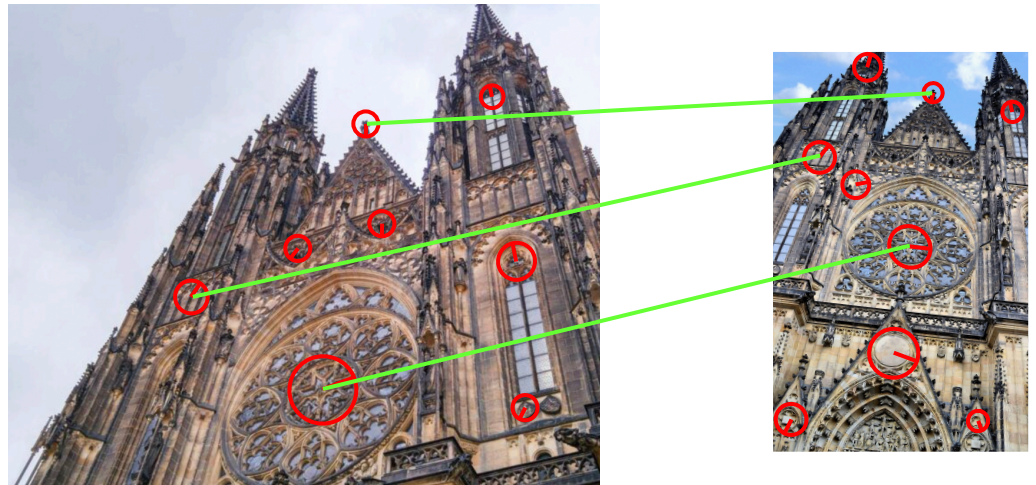


spatial verification: input - output

input:
tentative correspondences
based on visual words



out:
inlier correspondences
also geometric transformation
but that's not what we are after

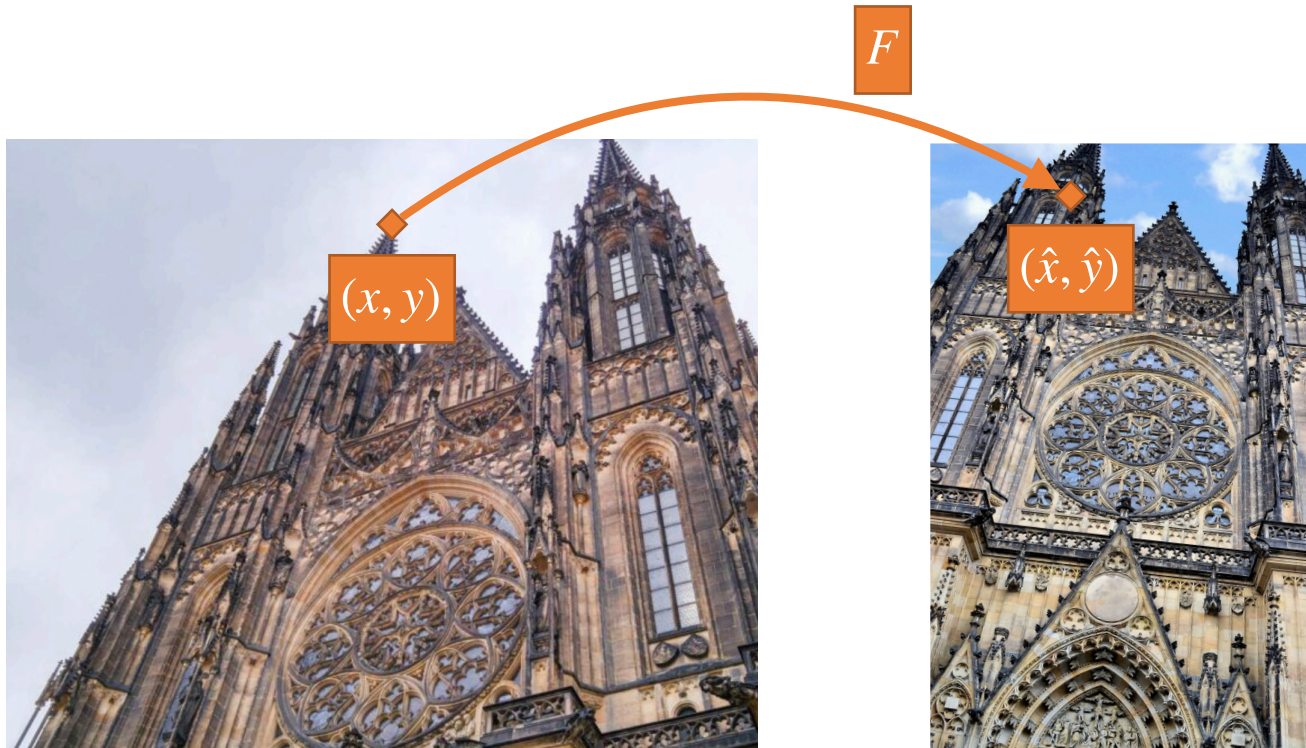


preliminaries: 2D image-to-image transformations

- 2D transformations as linear transformations in homogeneous coordinates

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = F \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- homogeneous coordinates: $[x, y, 1]^\top$
- represent a 2D transformation as a 3x3 matrix F



preliminaries: 2D transformations

- translation in 2D cartesian coordinates

$$\begin{bmatrix} \hat{x} \\ \hat{y} \end{bmatrix} = \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix} + \begin{bmatrix} x \\ y \end{bmatrix}$$

- translation in homogenous coordinates

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & \Delta x \\ 0 & 1 & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- rotation in homogenous coordinates

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- rotation & translation in homogenous coordinates

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & \Delta x \\ \sin\theta & \cos\theta & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & \Delta x \\ 0 & 1 & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

preliminaries: 2D transformations

- Euclidean/rigid transformation (3 DoF) - preserves distances and angles

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & \Delta x \\ \sin\theta & \cos\theta & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- similarity transformation (4 DoF) - preserves angles, not distances

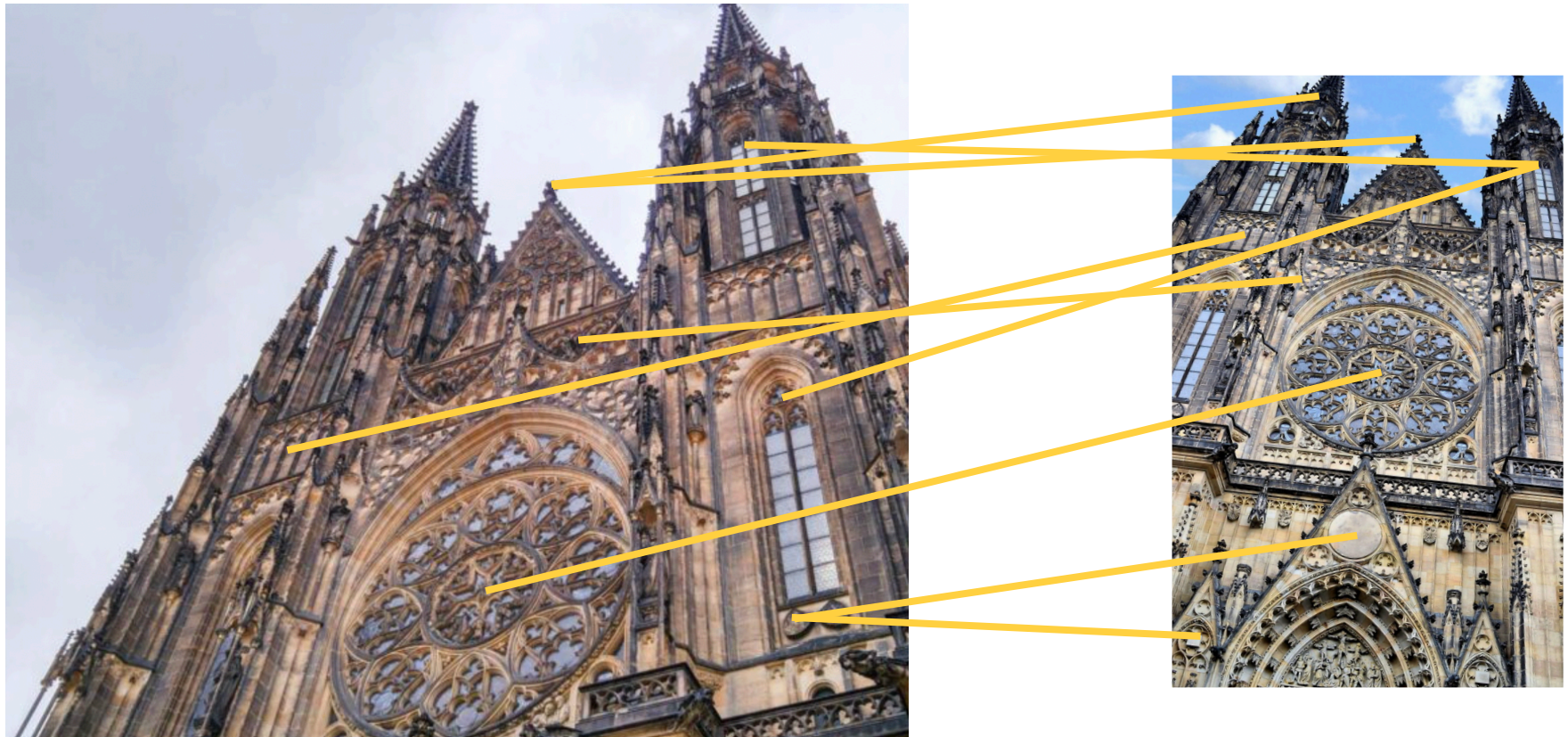
$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} s \cos\theta & -s \sin\theta & \Delta x \\ s \sin\theta & s \cos\theta & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- affine transformation (6 DoF) - preserves parallel lines, not angles/distances

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & \Delta x \\ a_{21} & a_{22} & \Delta y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

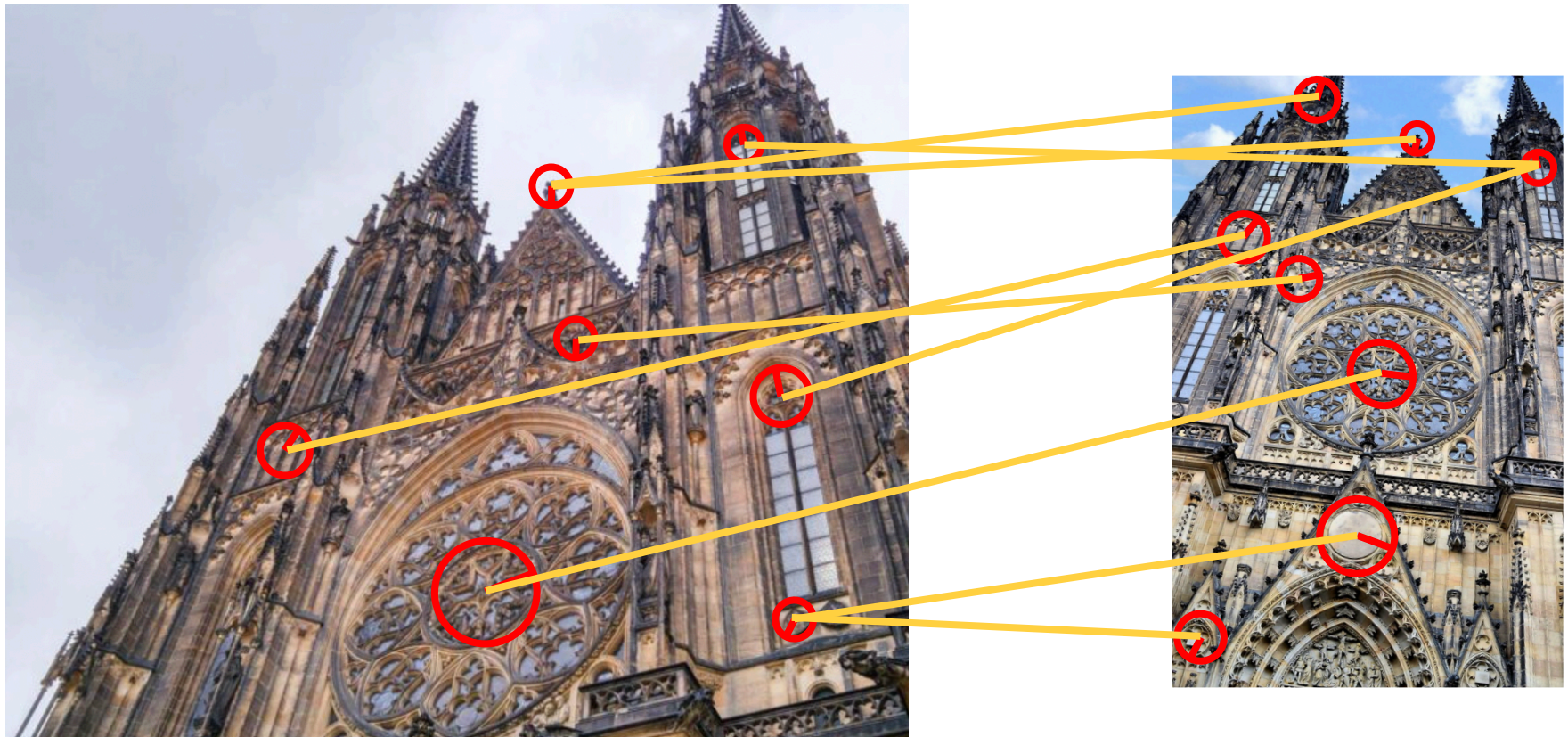
point correspondences vs local feature correspondences

- point correspondences: $(x, y) \leftrightarrow (x', y')$
- local feature correspondences: $(A, x, y) \leftrightarrow (A', x', y')$
 - A represents the shape of the local feature
 - eg. scale and rotation, affine shape



point correspondences vs local feature correspondences

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 - eg. scale and rotation, affine shape



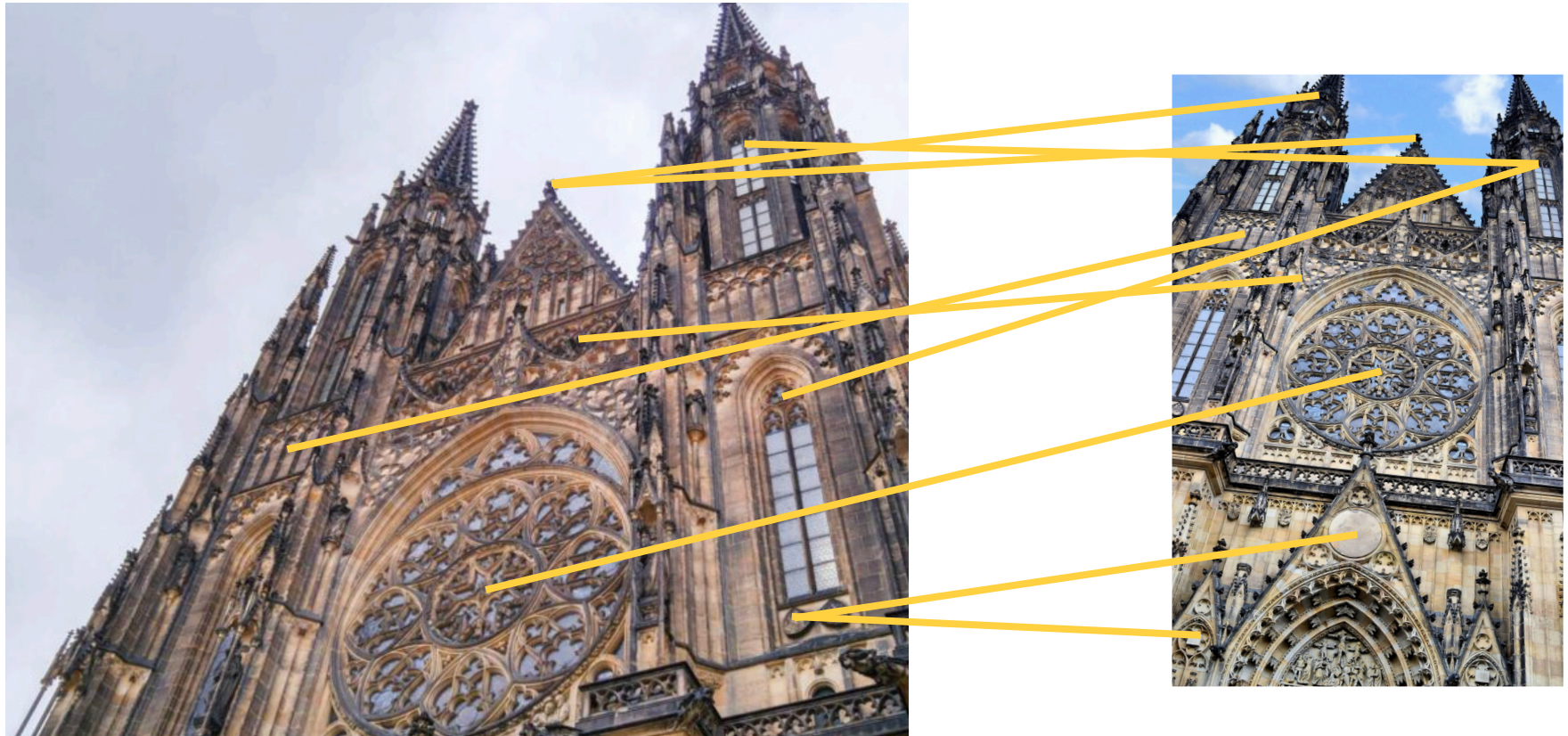
transformation hypothesis

- sample the minimum number of correspondences required to estimate the parameters of the geometric transformation

- one correspondence $\rightarrow$ two equations

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = F \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

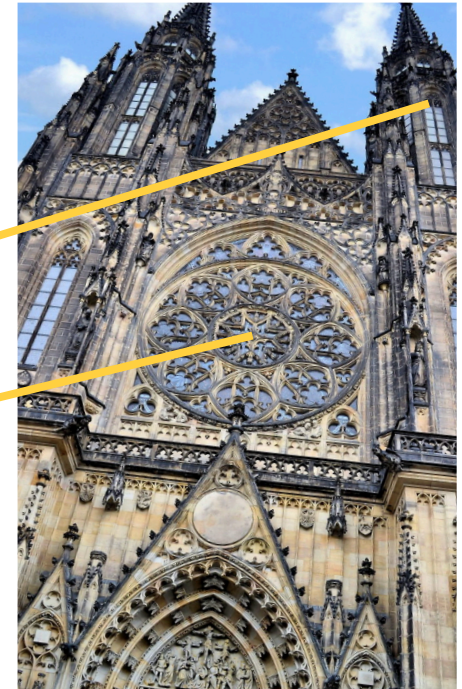
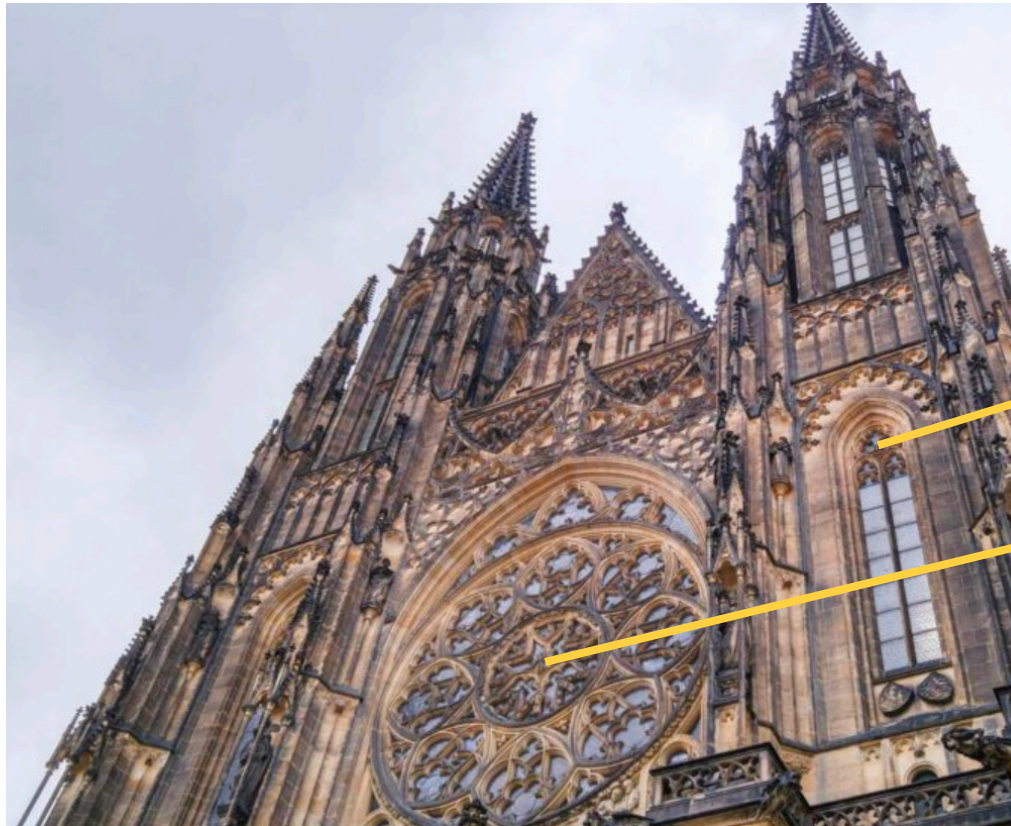
- similarity transformation (4 DoF) $\rightarrow$ 2 correspondences
- affine transformation (6 DoF) $\rightarrow$ 3 correspondences



transformation hypothesis

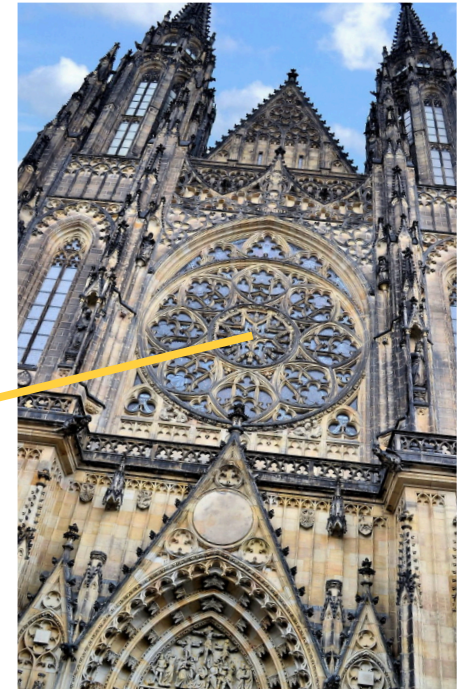
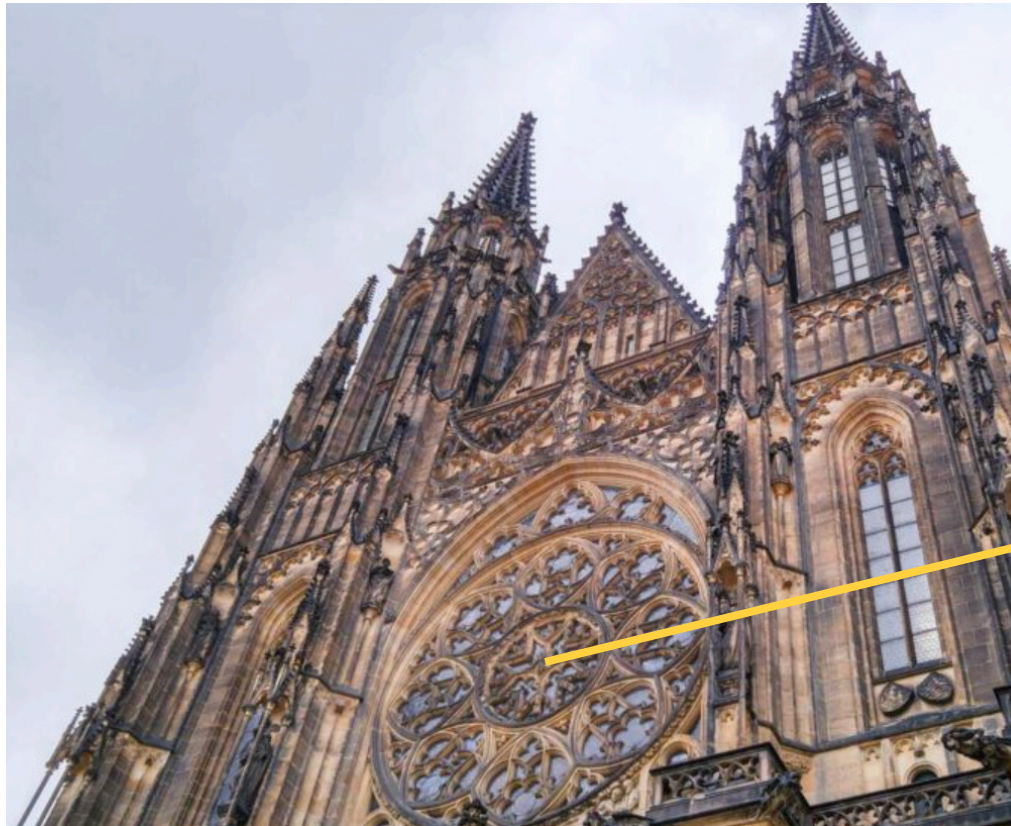
- sample the minimum number of correspondences required to estimate the parameters of the geometric transformation
- one correspondence $\rightarrow$ two equations
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$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ 1 \end{bmatrix} = F \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



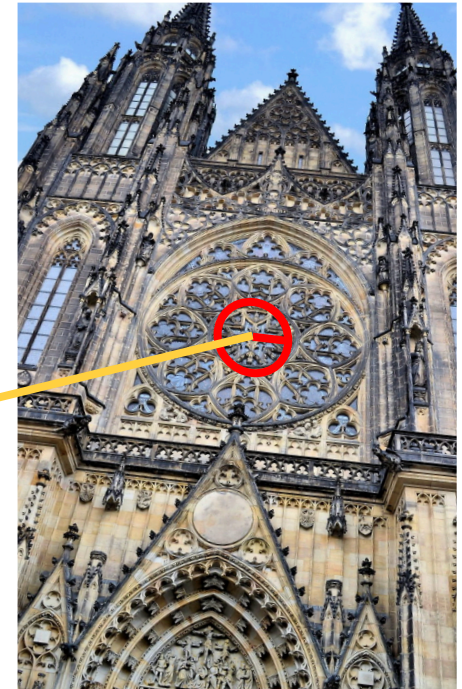
transformation hypothesis from a single correspondence

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features $\rightarrow$ similarity transformation
- affine invariant local features $\rightarrow$ affine transformation



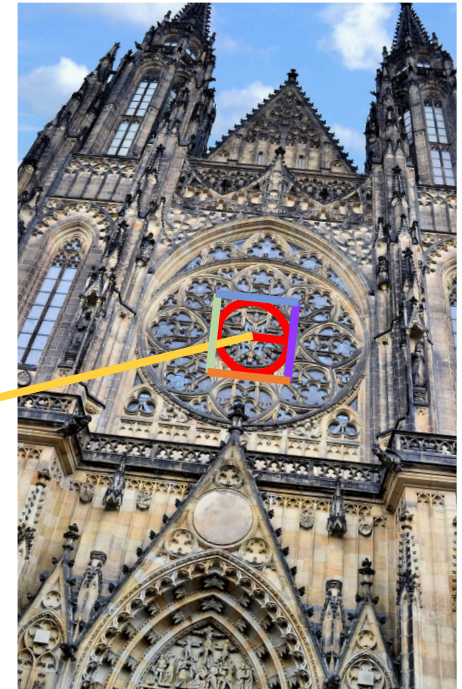
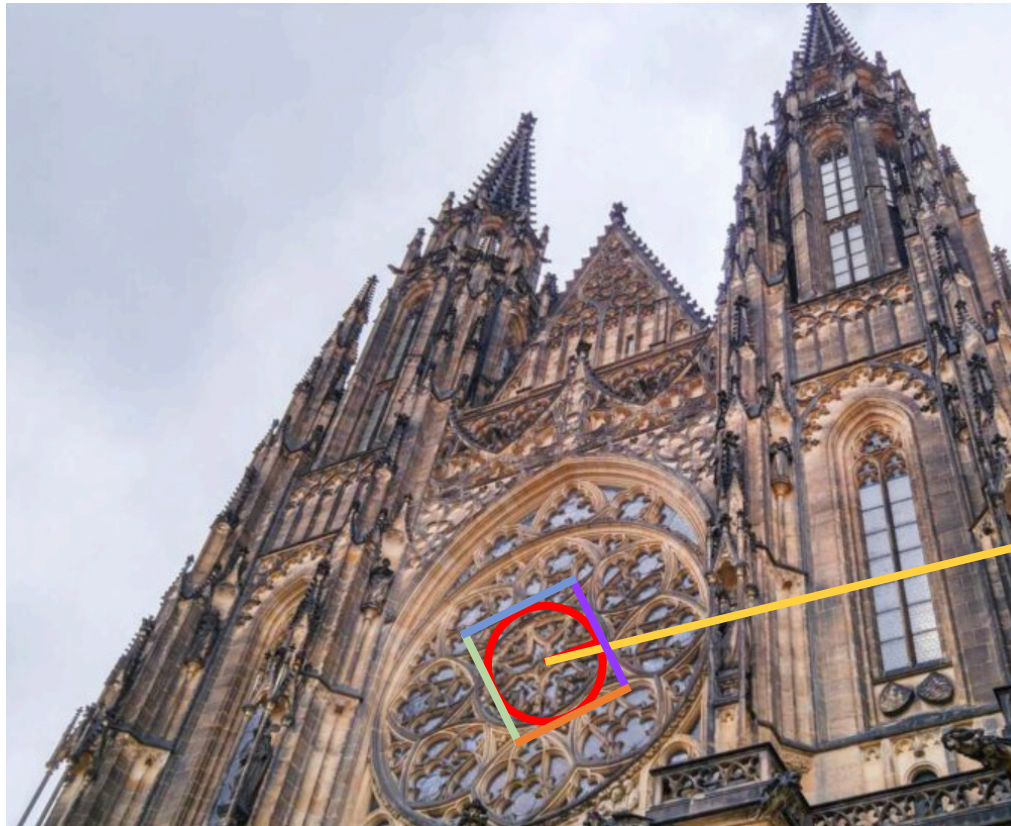
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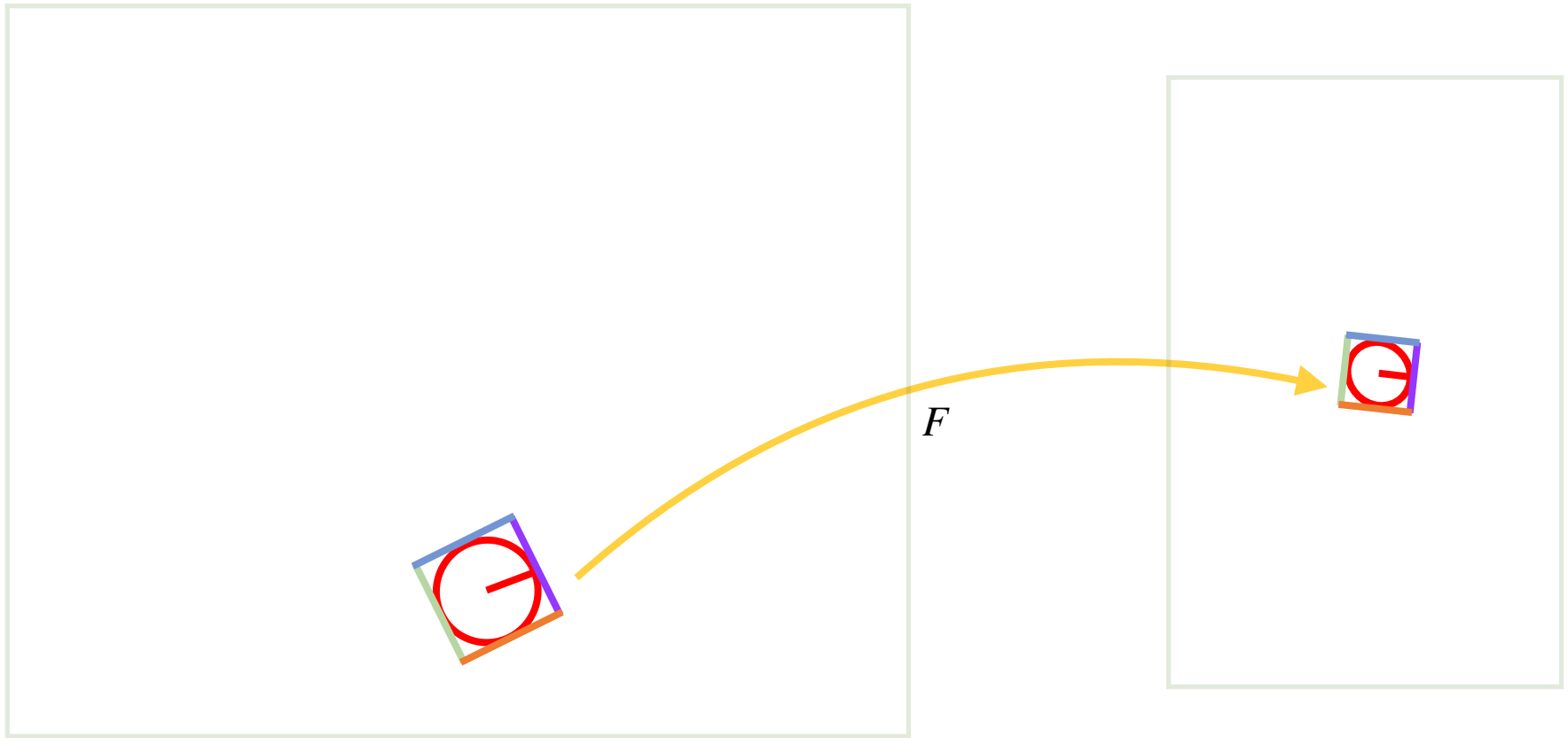
spatial verification

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features $\rightarrow$ similarity transformation
- affine invariant local features $\rightarrow$ affine transformation



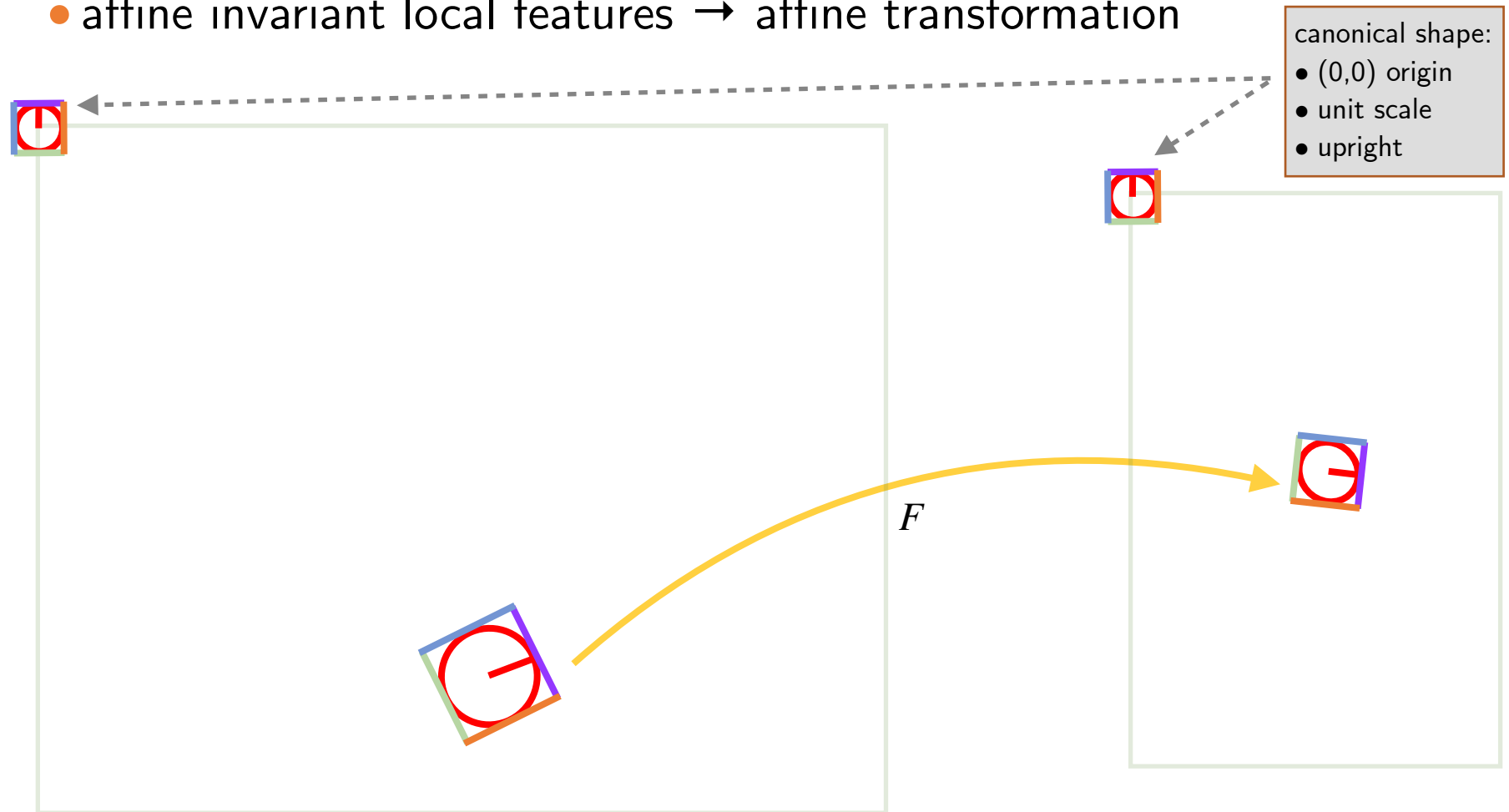
spatial verification

- estimate the transformation hypothesis from a single correspondence
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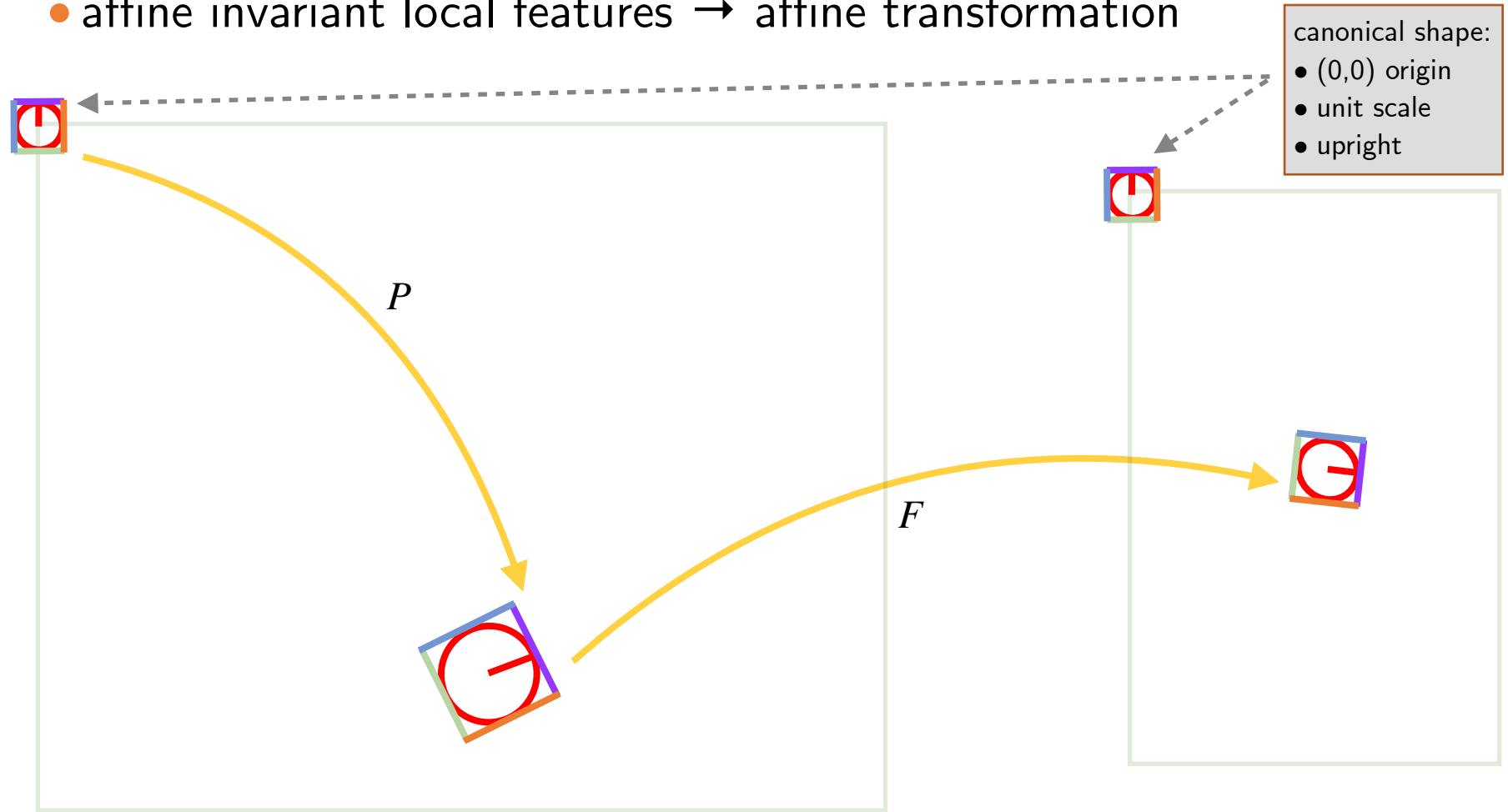
spatial verification

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features $\rightarrow$ similarity transformation
- affine invariant local features $\rightarrow$ affine transformation



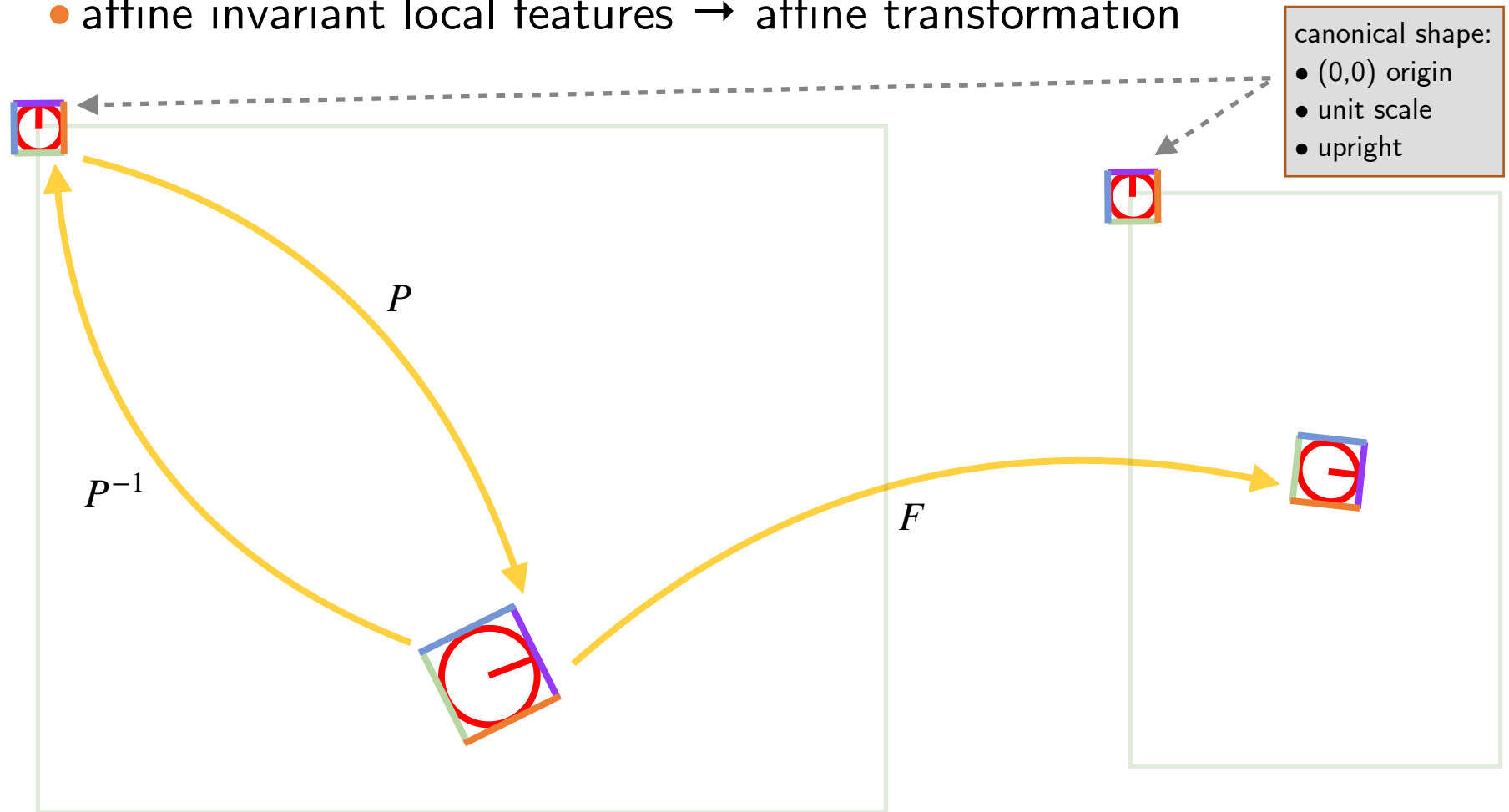
spatial verification

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features → similarity transformation
- affine invariant local features → affine transformation



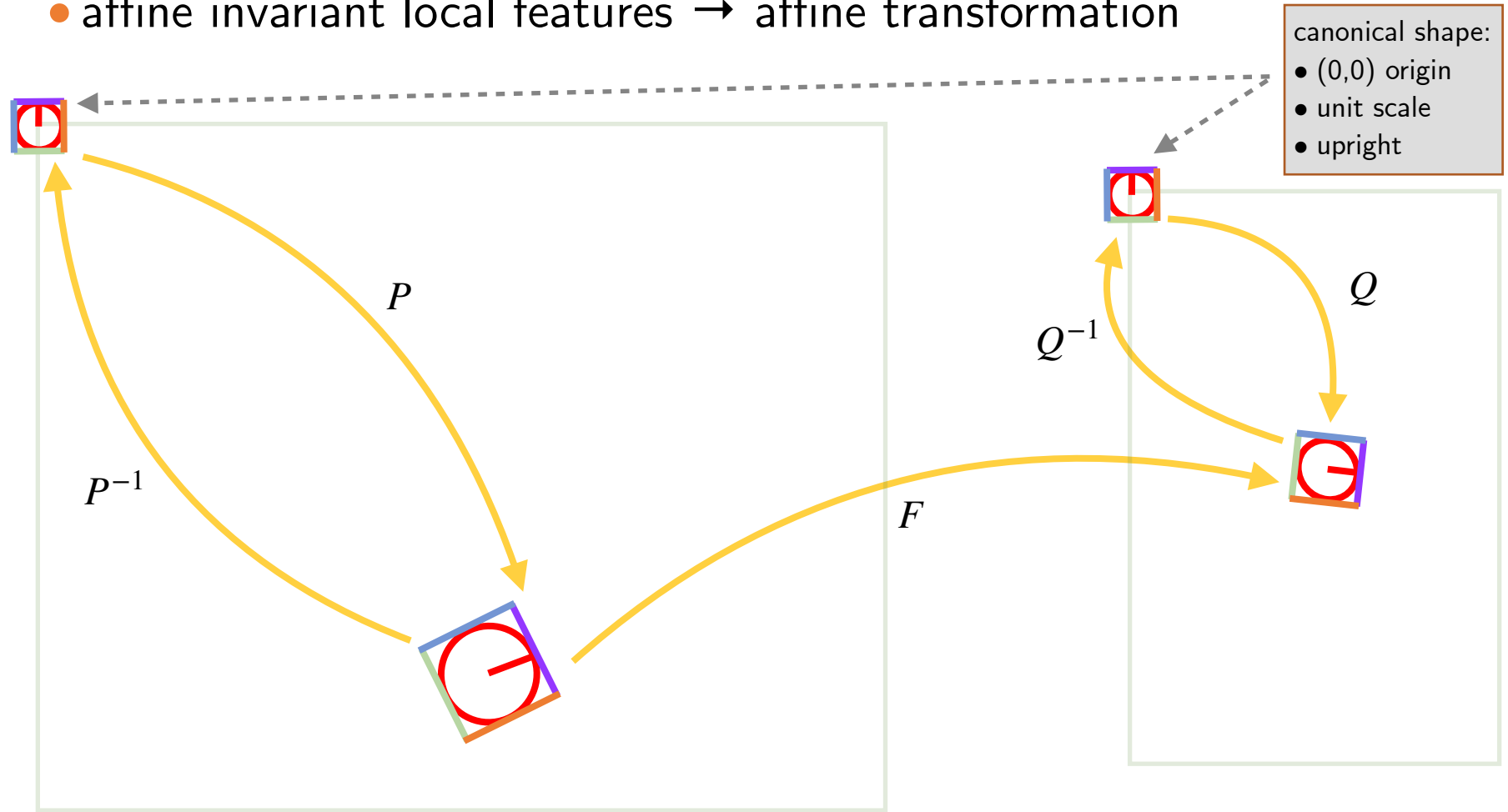
spatial verification

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features $\rightarrow$ similarity transformation
- affine invariant local features $\rightarrow$ affine transformation



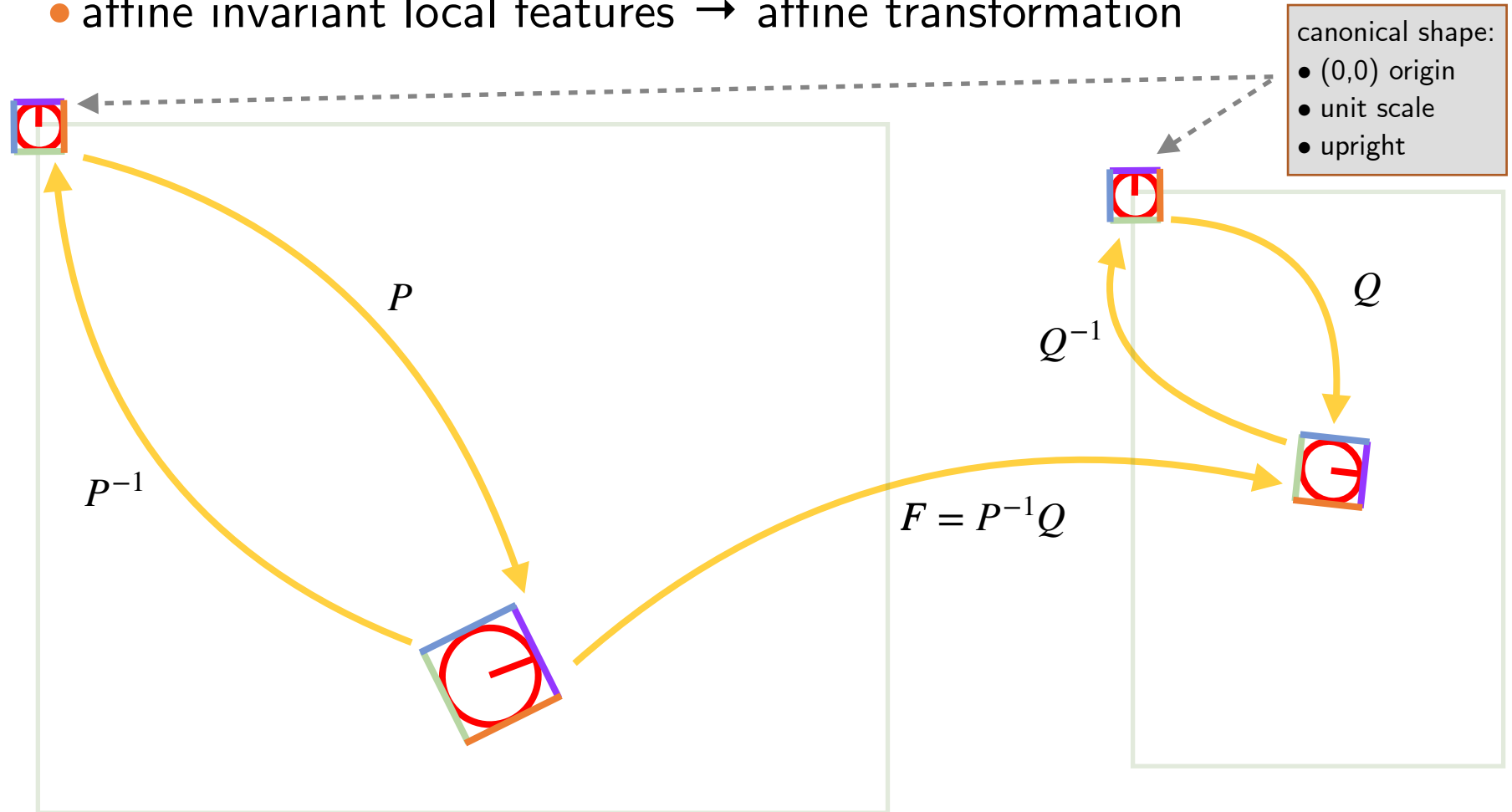
spatial verification

- estimate the transformation hypothesis from a single correspondence
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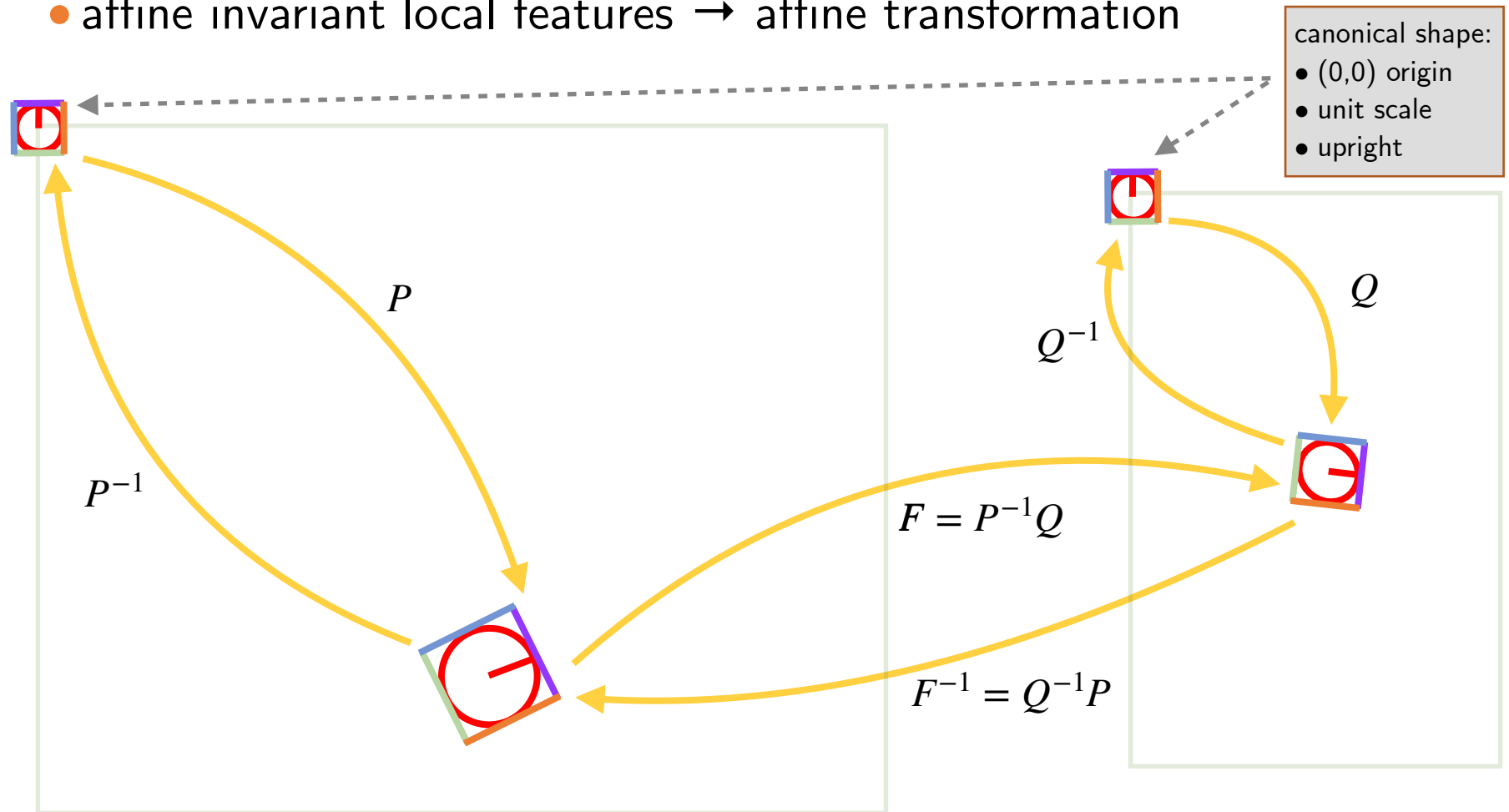
spatial verification

- estimate the transformation hypothesis from a single correspondence
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spatial verification

- estimate the transformation hypothesis from a single correspondence
- scale and rotation invariant local features $\rightarrow$ similarity transformation
- affine invariant local features $\rightarrow$ affine transformation



conventional RANSAC

- correspondence $c_i = (x_i, y_i) \leftrightarrow (x'_i, y'_i)$
- correspondence set $C = \{c_1, c_2, \dots, c_n\}$

conventional RANSAC with point correspondences

- for j in $1 \dots T$ # max number of hypotheses
 - sample a minimal set C_m from C # size depends on DoFs
 - estimate F from C_m # inlier free sample for good estimate
 - for i in $1 \dots n$ # loop over all correspondences
 - $\begin{bmatrix} \hat{x}_i \\ \hat{y}_i \\ 1 \end{bmatrix} = F \begin{bmatrix} x_i \\ y_i \\ 1 \end{bmatrix}$ # transform points from an image to the other
 - $\text{is_inlier} = \text{error}([\hat{x}_i, \hat{y}_i], [x'_i, y'_i]) < \tau$ # error between projected and given point
 - # inlier count, track F with most inliers, early termination, ...

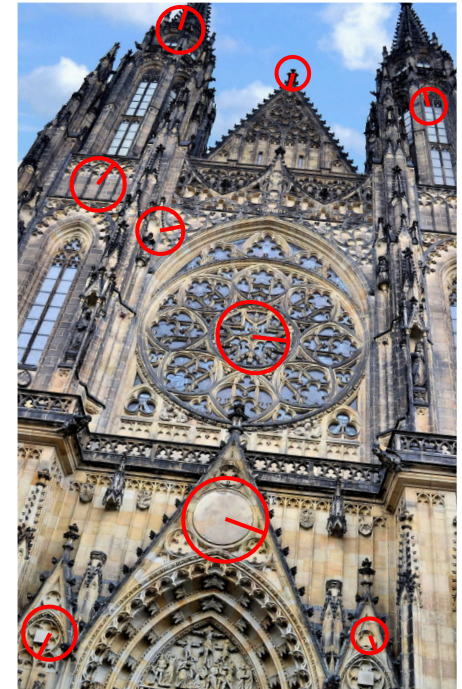
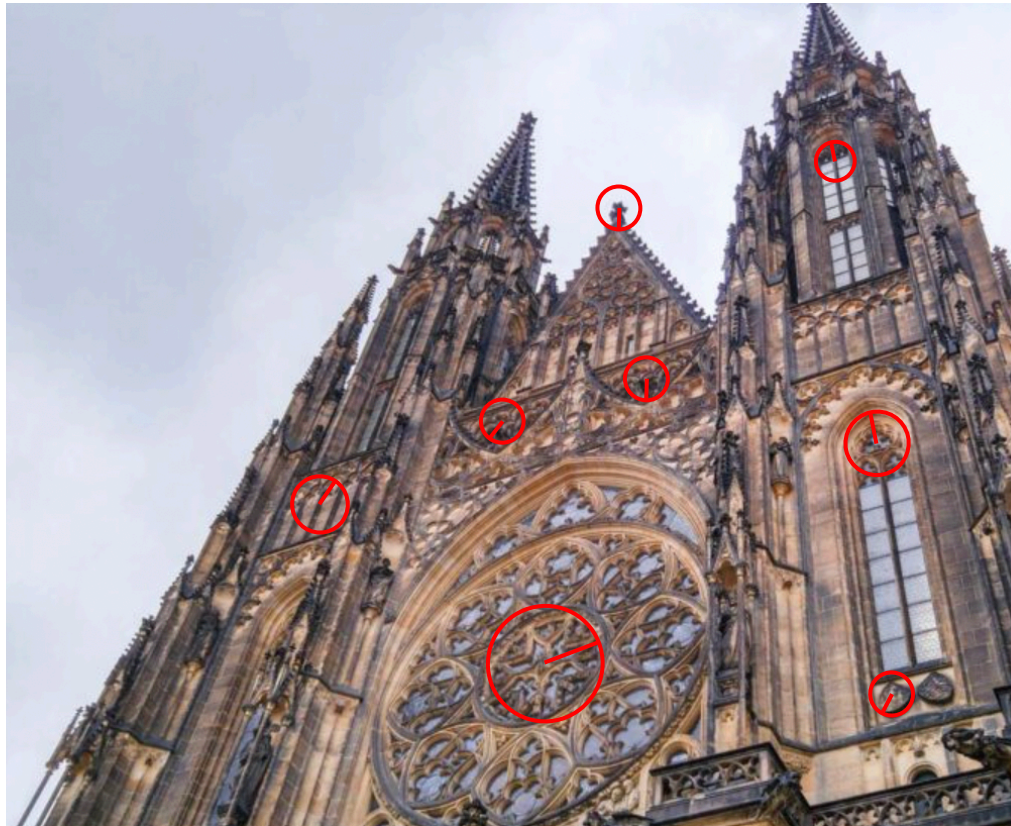
fast spatial matching

- correspondence $c_i = (A_i, x_i, y_i) \leftrightarrow (A'_i, x'_i, y'_i)$
- correspondence set $C = \{c_1, c_2, \dots, c_n\}$

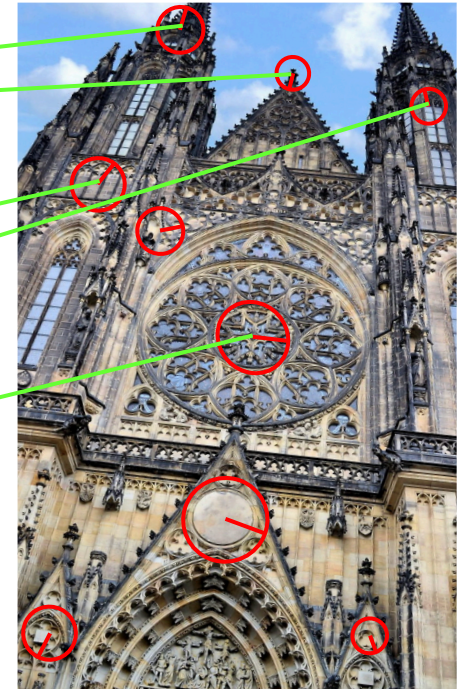
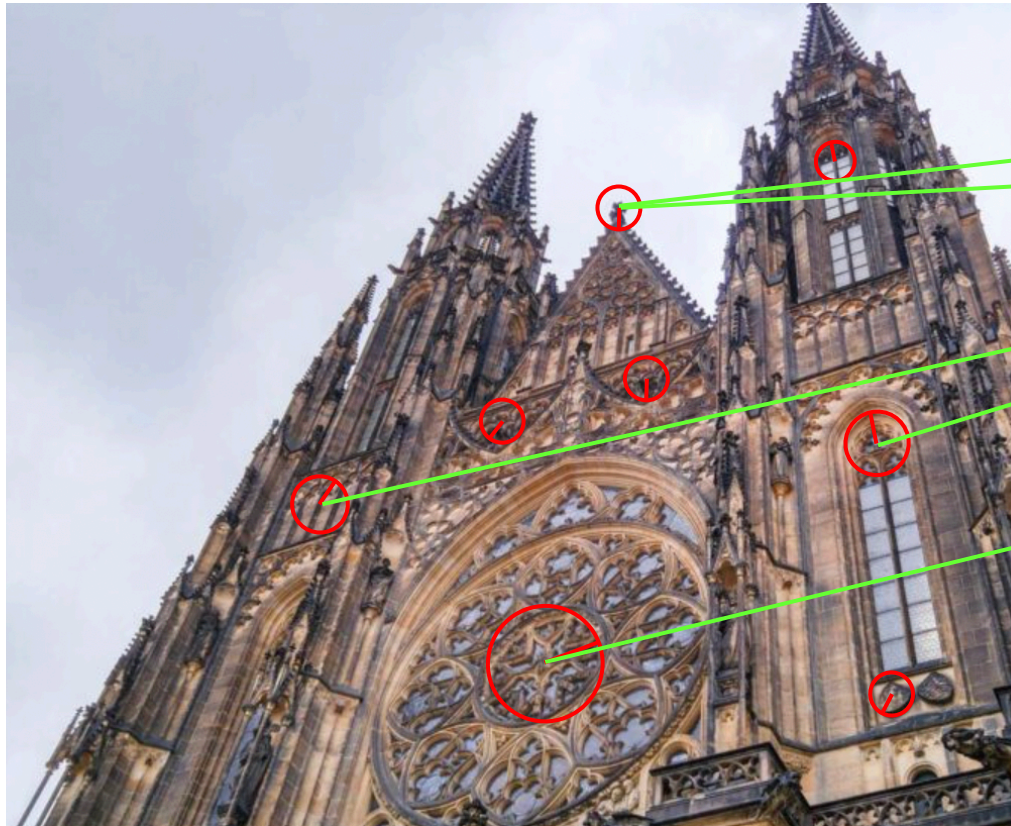
fast spatial matching with local feature correspondences

- for j in $1 \dots n$ # loop over all correspondences
 - estimate F from c_j # single correspondence hypothesis
- for i in $1 \dots n$ # loop over all correspondences no randomness
 - $\begin{bmatrix} \hat{x}_i \\ \hat{y}_i \\ 1 \end{bmatrix} = F \begin{bmatrix} x_i \\ y_i \\ 1 \end{bmatrix}$ # transform points from an image to the other
 - $\text{is_inlier} = \text{error}([\hat{x}_i, \hat{y}_i], [x'_i, y'_i]) < \tau$ # error between projected and corresponding point
 - # inlier count, track F with most inliers, early termination, ...

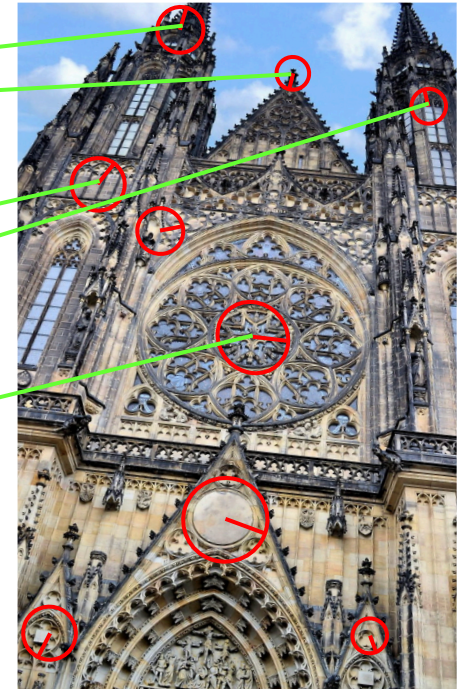
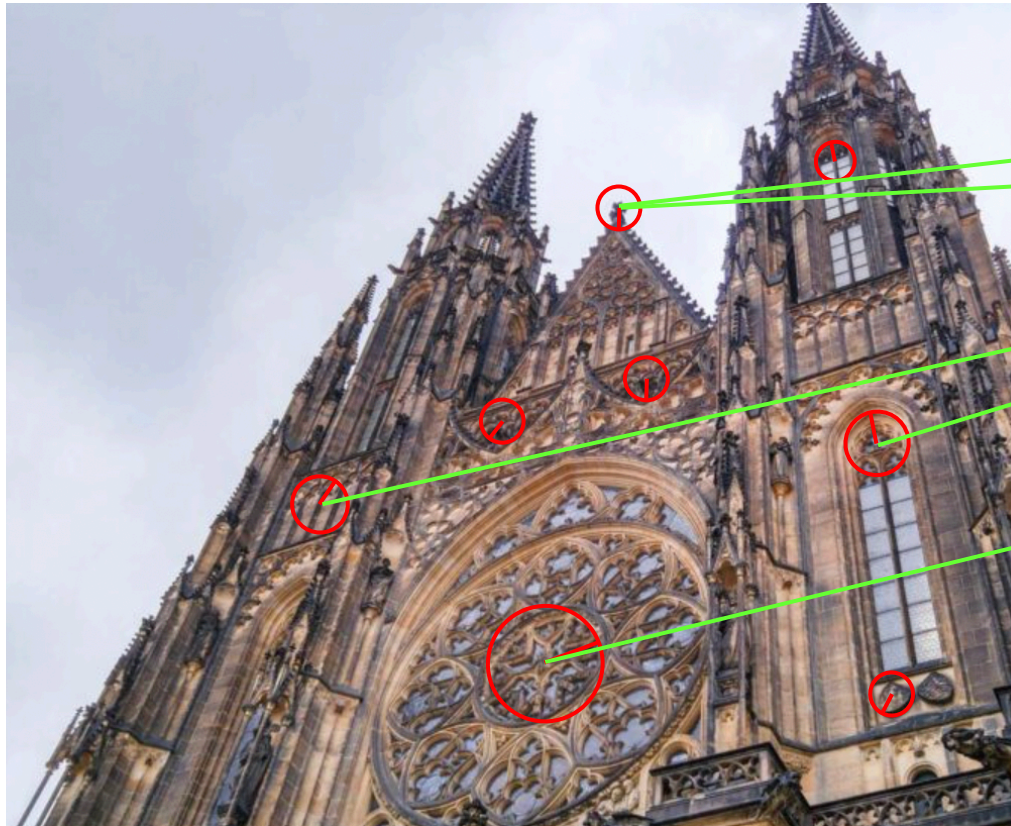
transformation hypothesis verification - inlier counting



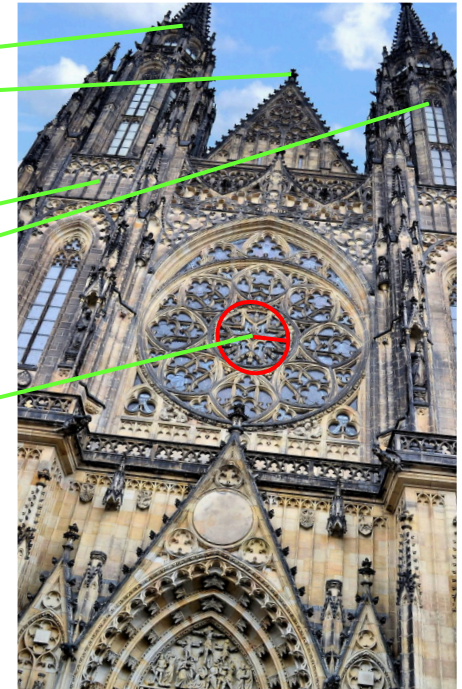
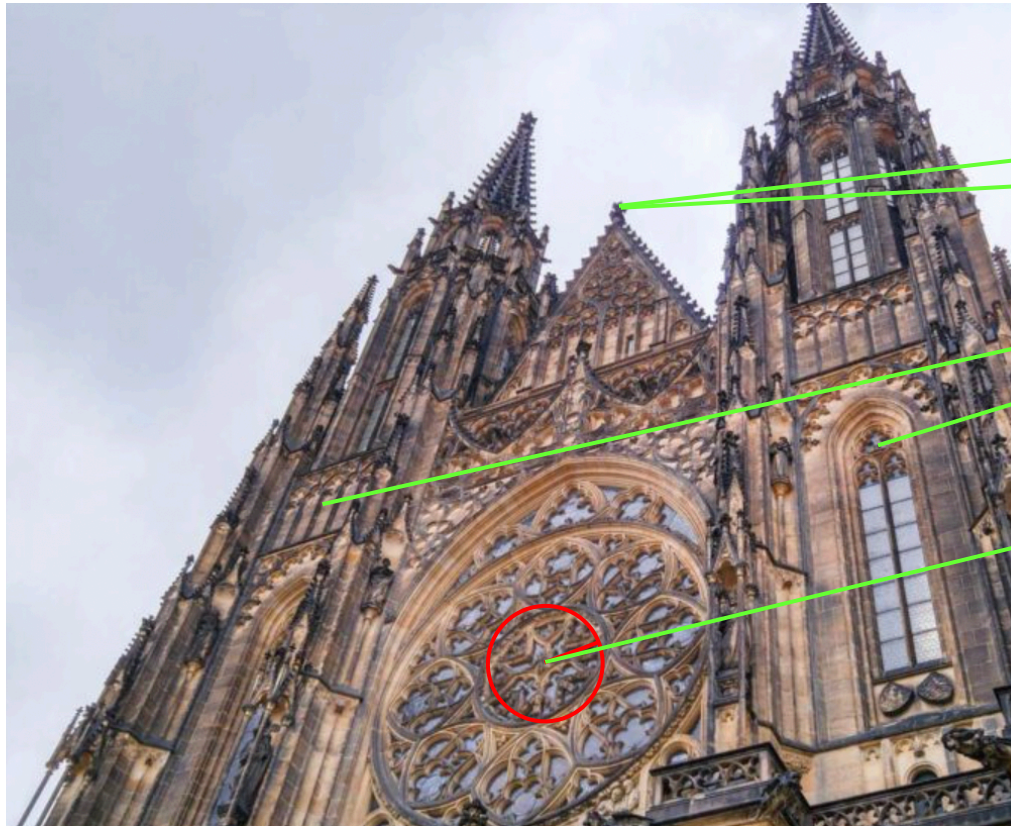
transformation hypothesis verification - inlier counting



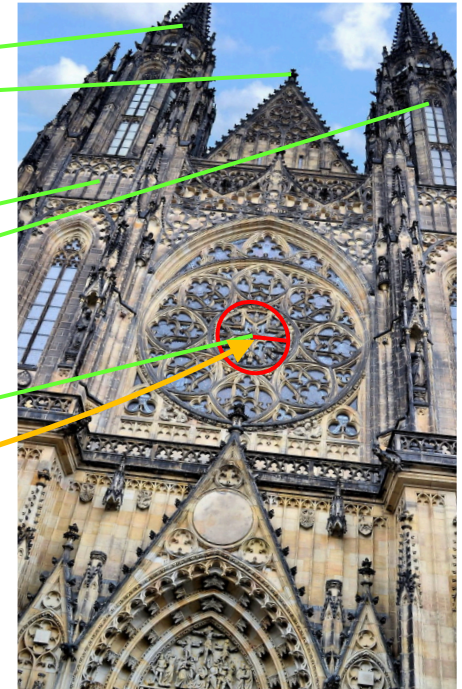
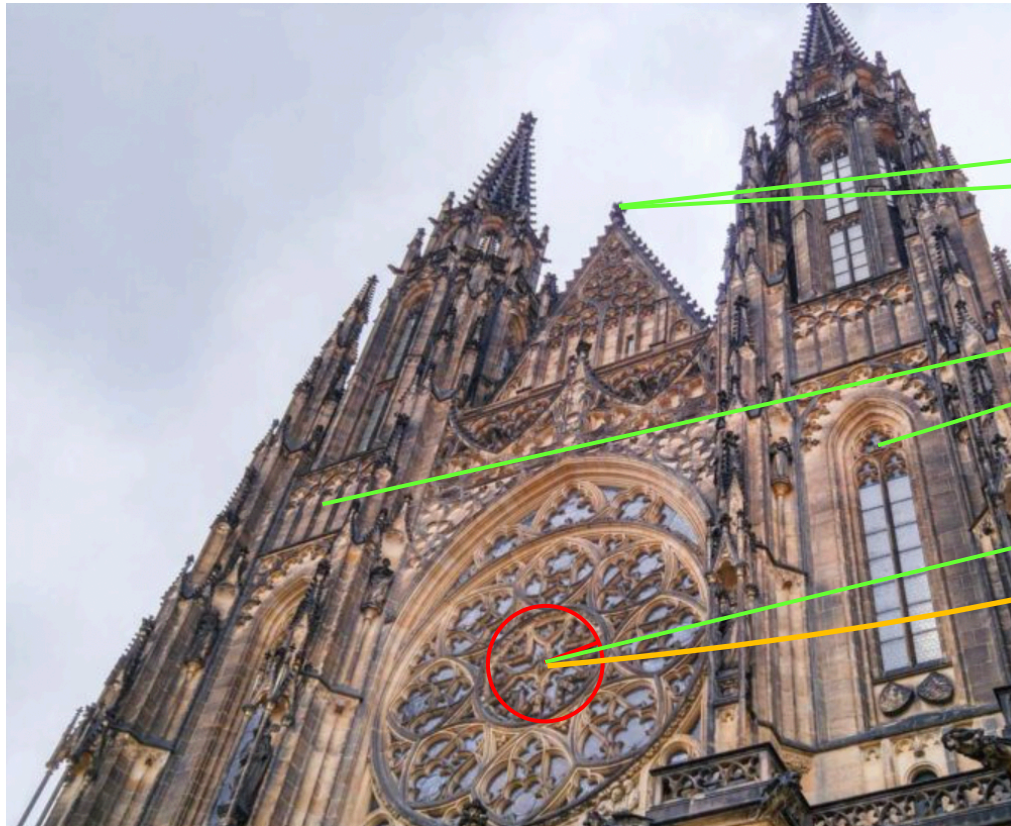
transformation hypothesis verification - inlier counting



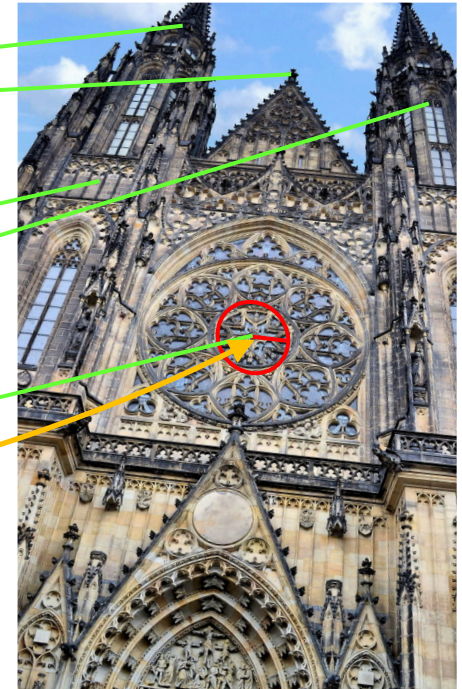
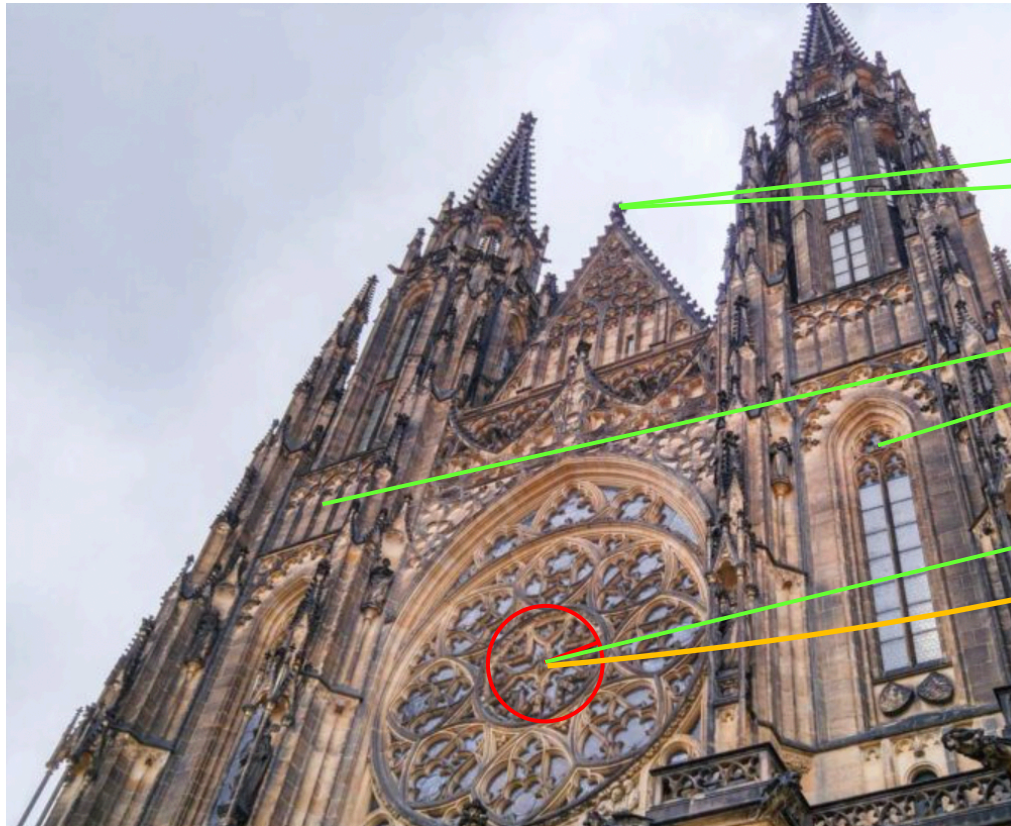
transformation hypothesis verification - inlier counting



transformation hypothesis verification - inlier counting

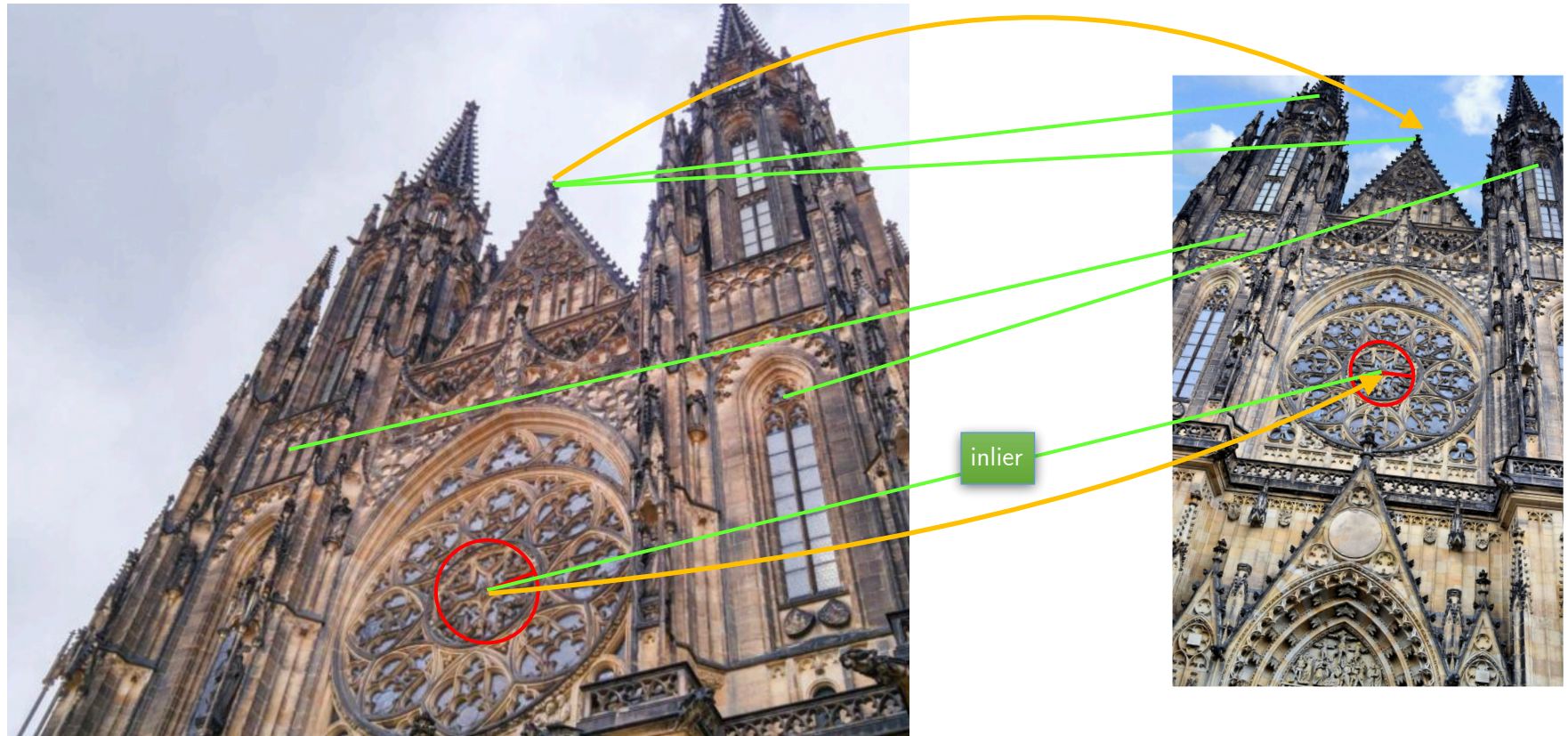


transformation hypothesis verification - inlier counting

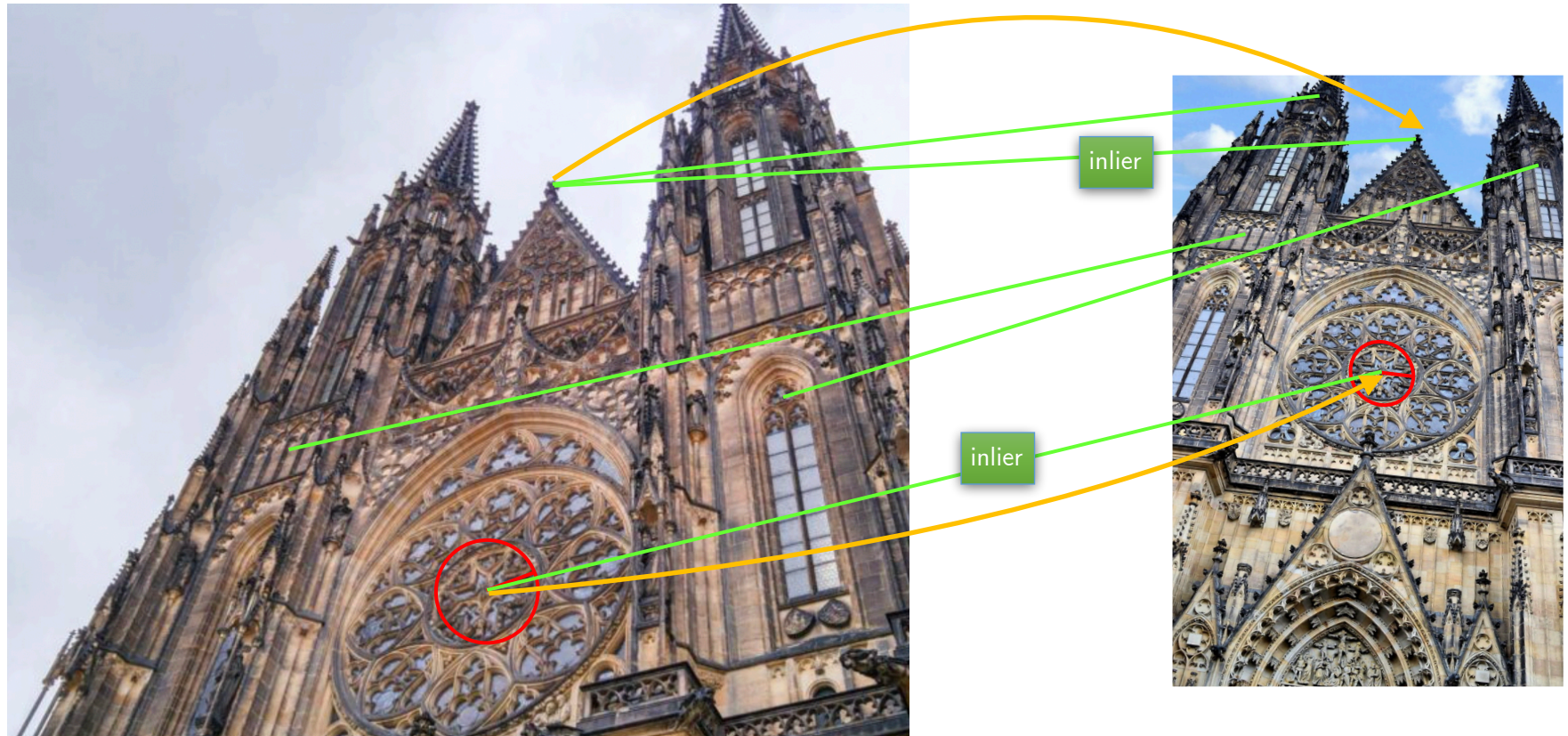


inlier

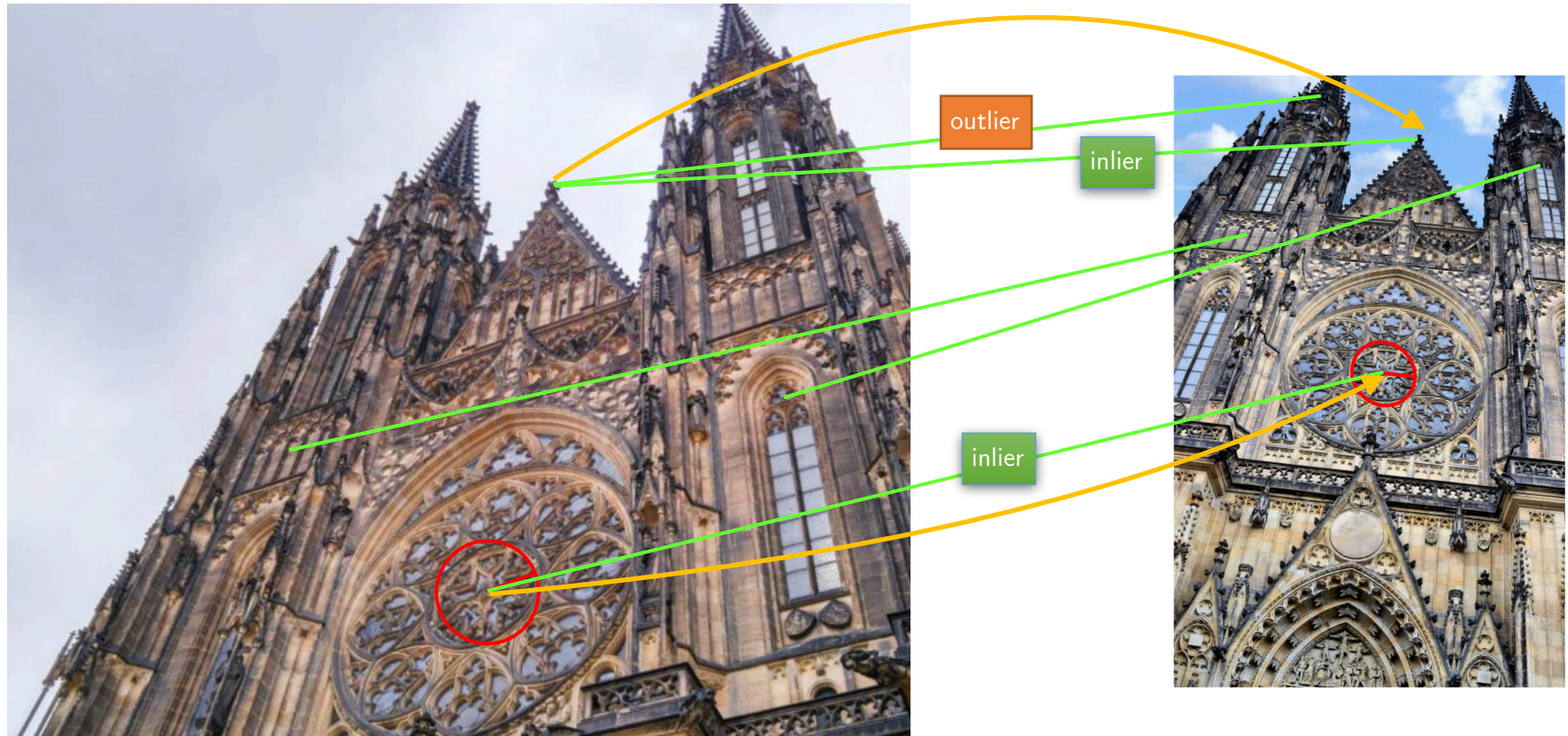
transformation hypothesis verification - inlier counting



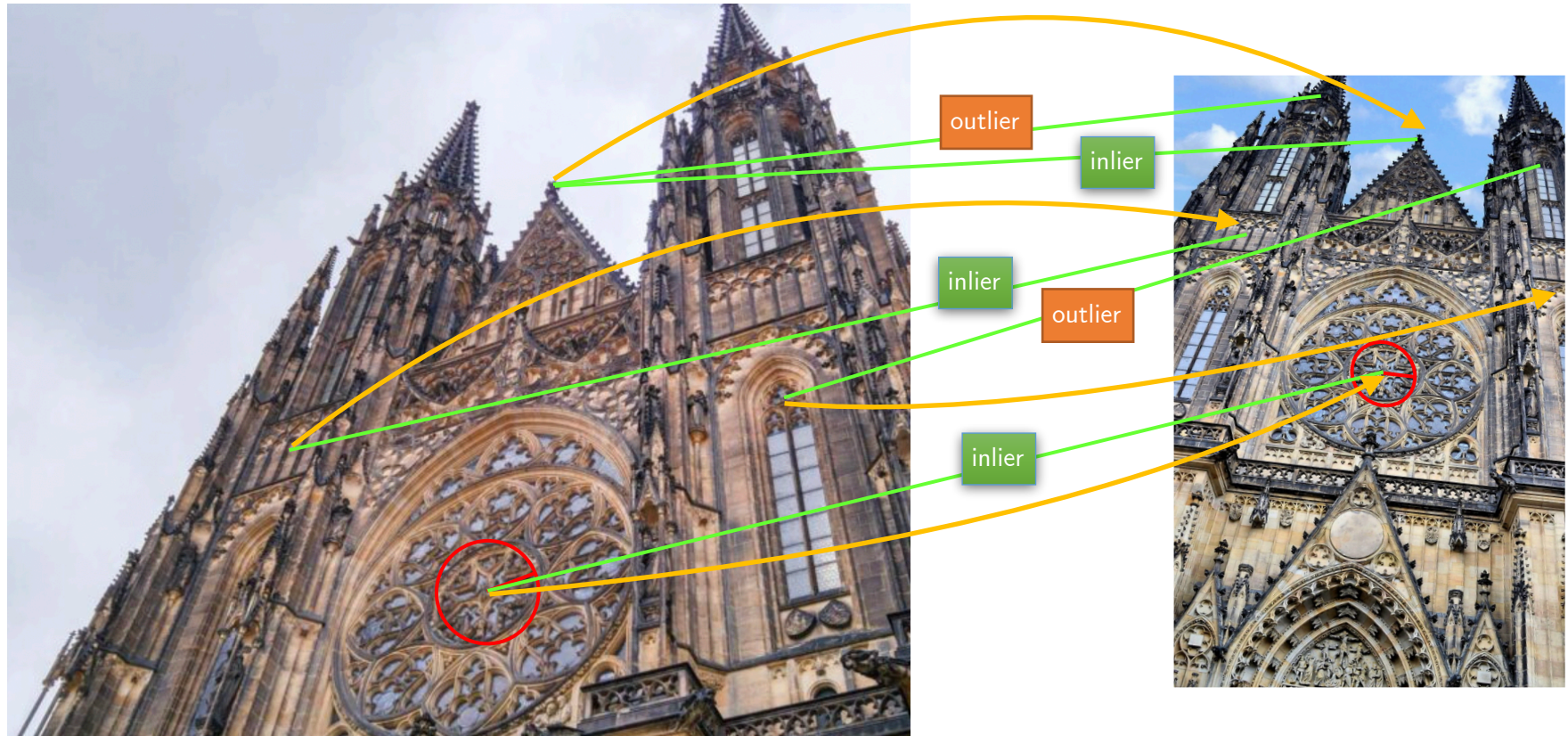
transformation hypothesis verification - inlier counting



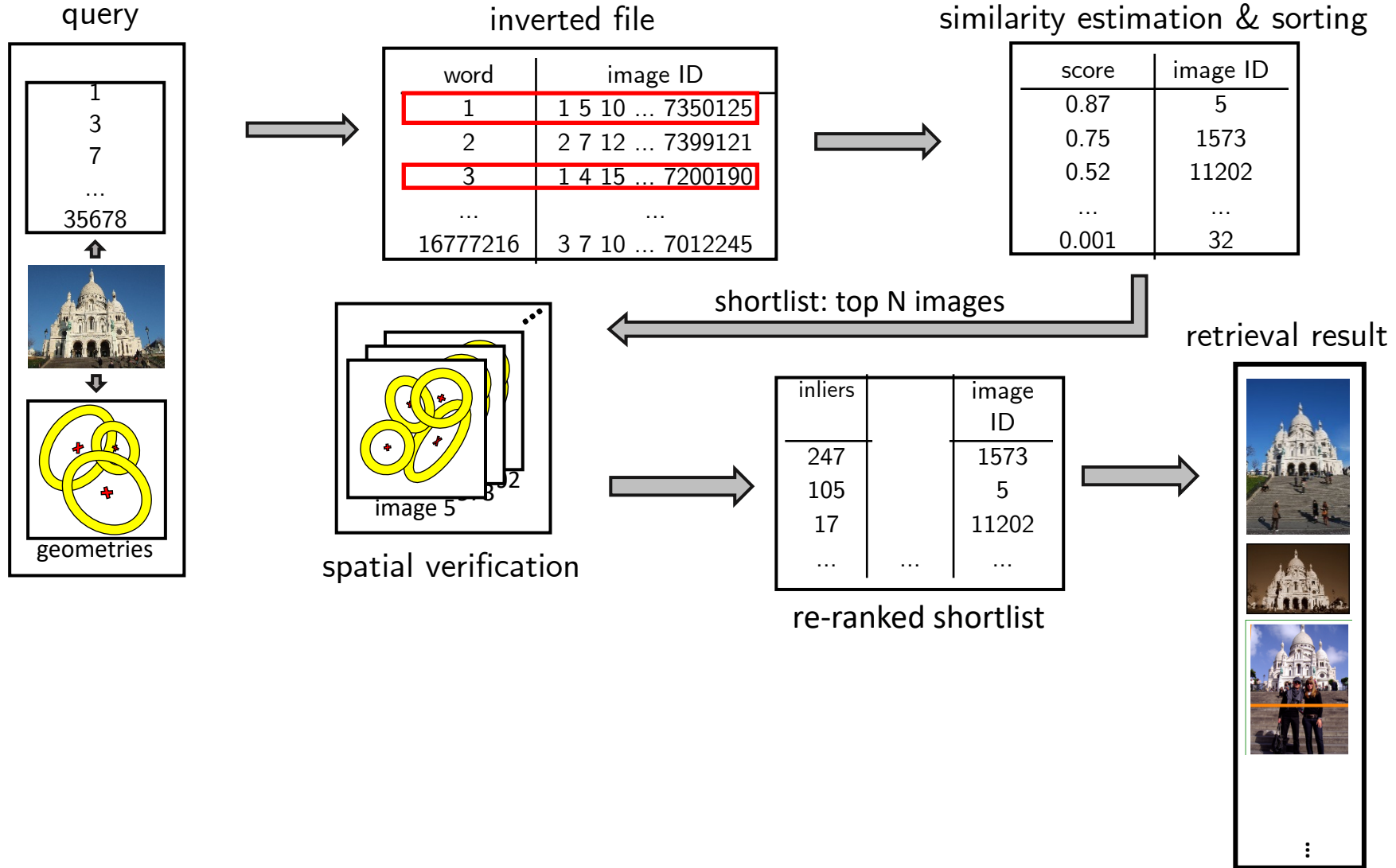
transformation hypothesis verification - inlier counting



transformation hypothesis verification - inlier counting



spatial verification - retrieval



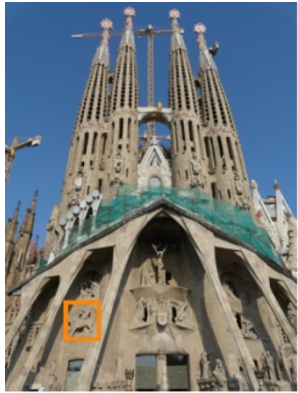
[Philbin et al. CVPR'07]

[Perdoch et al. CVPR'09]

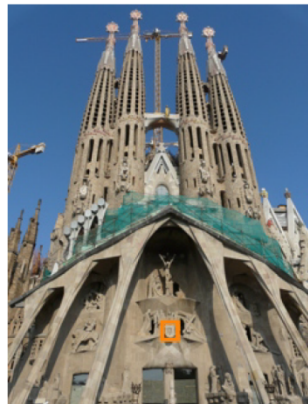
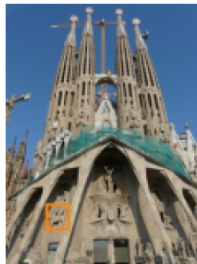
special retrieval tasks

beyond visual similarity retrieval

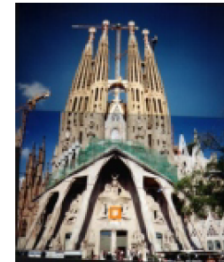
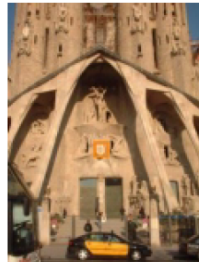
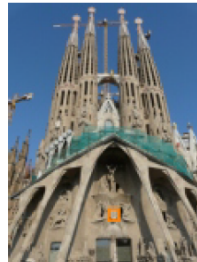
- most similar images: near identical
 - is this what we want?



query 1



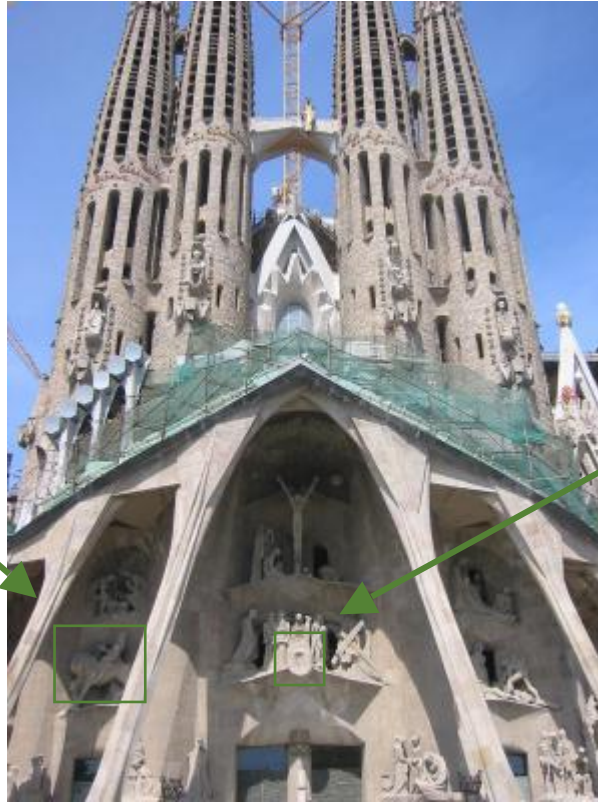
query 2



beyond visual similarity retrieval

what is this?

... and what is that?



let's zoom-in!

image retrieval for zoom-in

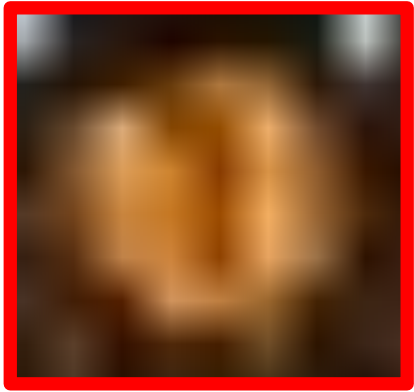


image retrieval for zoom-in



image retrieval for zoom-in

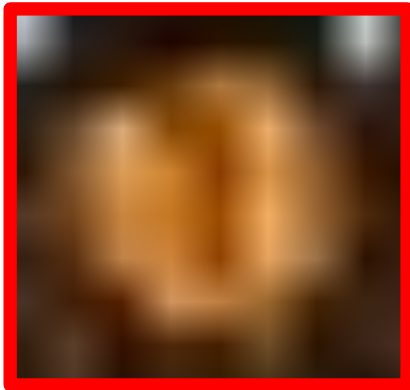


image retrieval for zoom-in

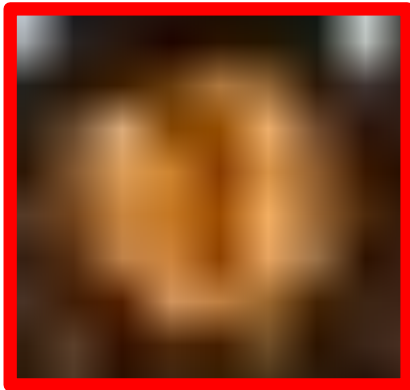
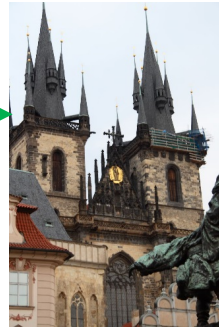


image retrieval for zoom-in

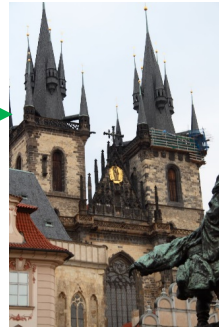
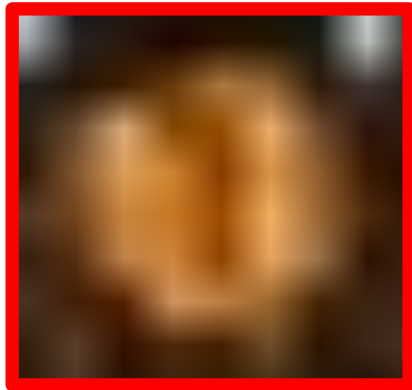


image retrieval for zoom-in

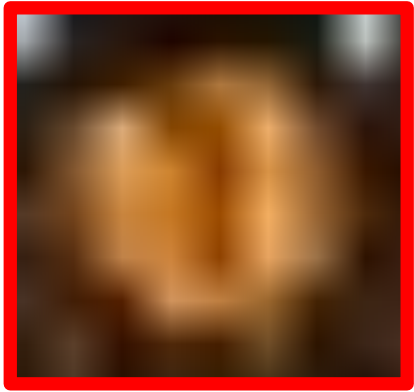


image retrieval for zoom-in

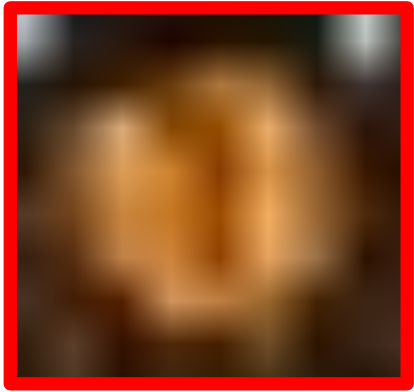
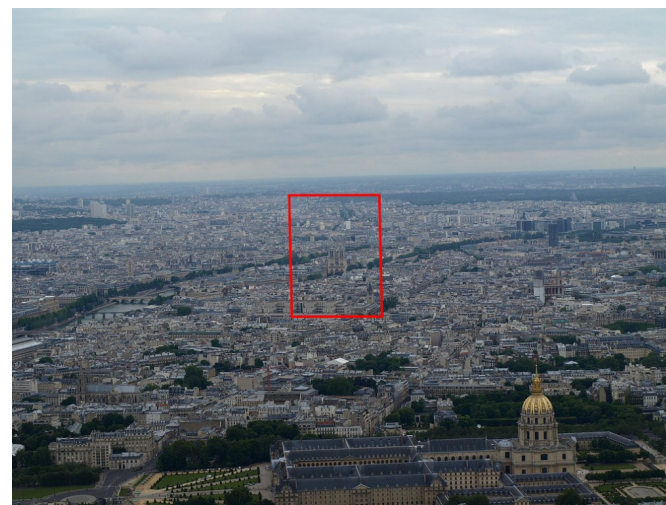
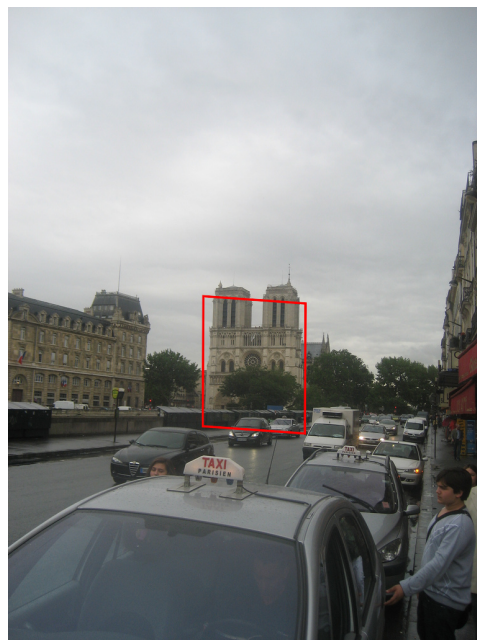
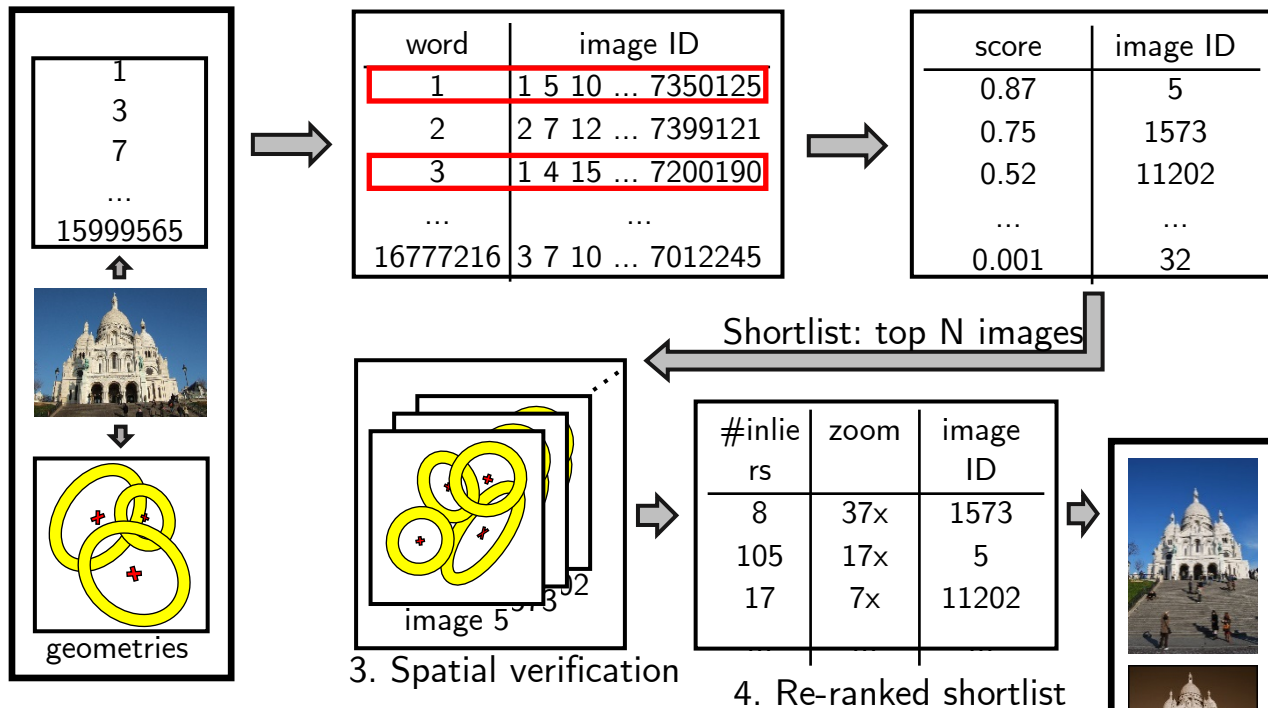


image retrieval for zoom-out



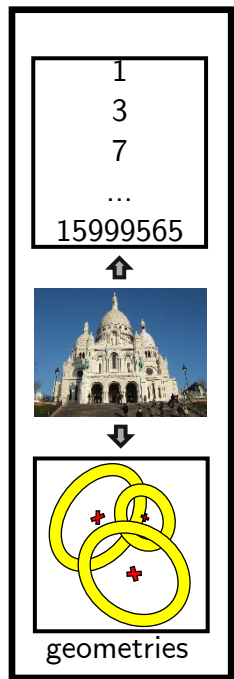
zoom in/out

1. inverted file: posting list per visual word 2. Image ranking



zoom in/out

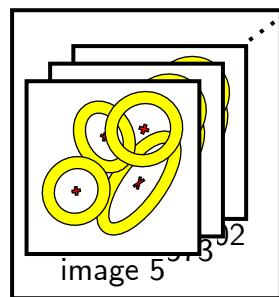
1. inverted file: posting list per visual word 2. Image ranking



word	image ID
1	1 5 10 ... 7350125
2	2 7 12 ... 7399121
3	1 4 15 ... 7200190
...	...
16777216	3 7 10 ... 7012245

score	image ID
0.87	5
0.75	1573
0.52	11202
...	...
0.001	32

Shortlist: top N images



#inliers	zoom	image ID
8	37x	1573
105	17x	5
17	7x	11202

3. Spatial verification

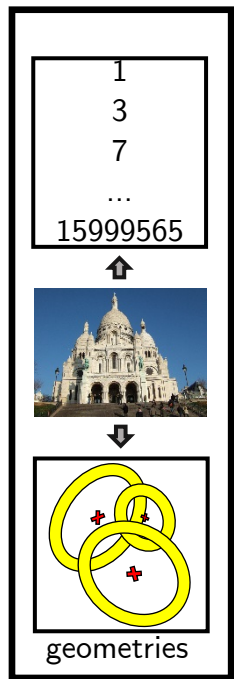
4. Re-ranked shortlist



problem specific ranking function, e.g. maximize scale change

zoom in/out

1. inverted file: posting list per visual word 2. Image ranking

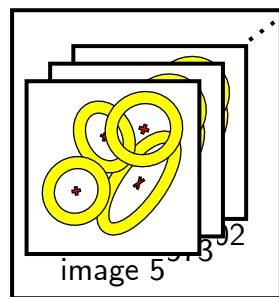


word	image ID
1	1 5 10 ... 7350125
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...	...
16777216	3 7 10 ... 7012245

score	image ID
0.87	5
0.75	1573
0.52	11202
...	...
0.001	32

geometry compressed in inverted file taken into account during scoring

Shortlist: top N images



#inliers	zoom	image ID
8	37x	1573
105	17x	5
17	7x	11202

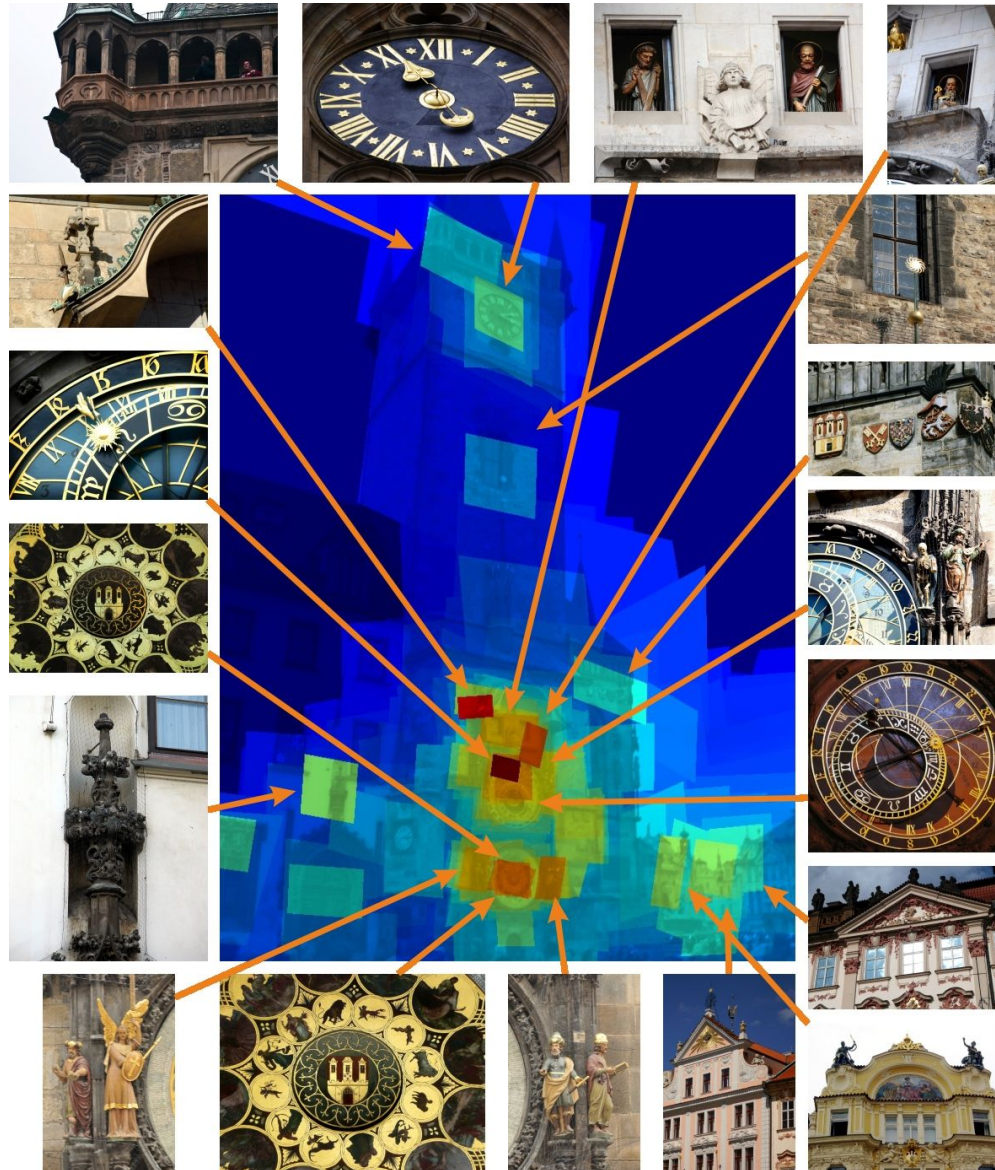
3. Spatial verification

4. Re-ranked shortlist



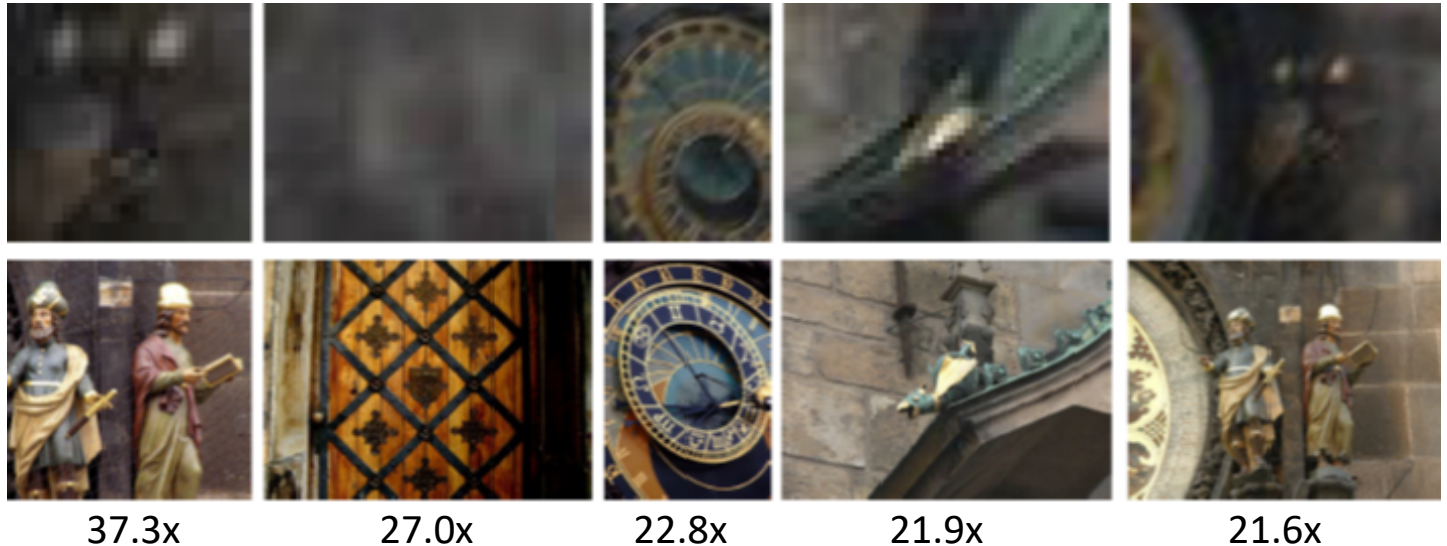
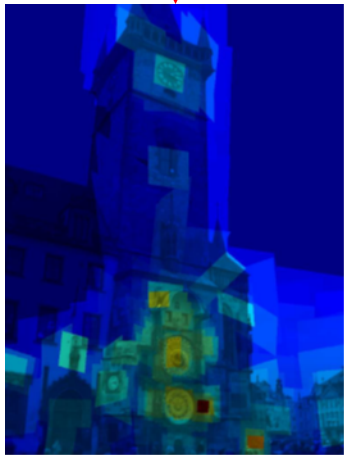
problem specific ranking function, e.g. maximize scale change

what should you not miss?



highest resolution transform

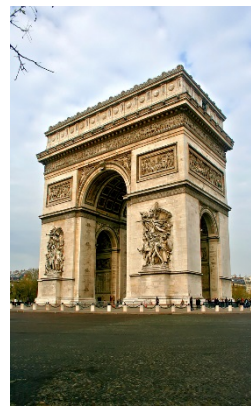
- given a query, for every pixel in the query image:
 - find the database image with the maximum resolution depicting the pixel



retrieval for 3D reconstruction

- visually most similar search
 - many near duplicates
 - details lost
- zoom-in and details search
 - details retrieved
 - transition images to match the details
- zoom-out search
 - viewpoint change
 - more context
- sideways crawl
 - significant viewpoint change
 - more context

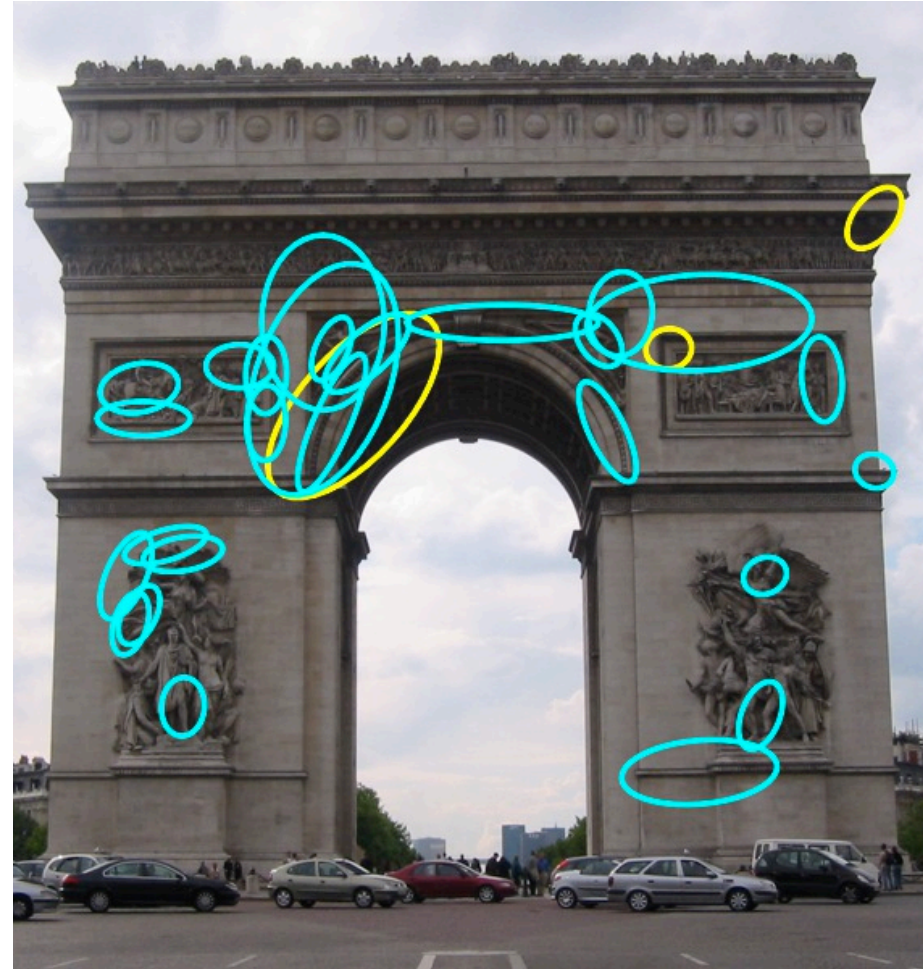
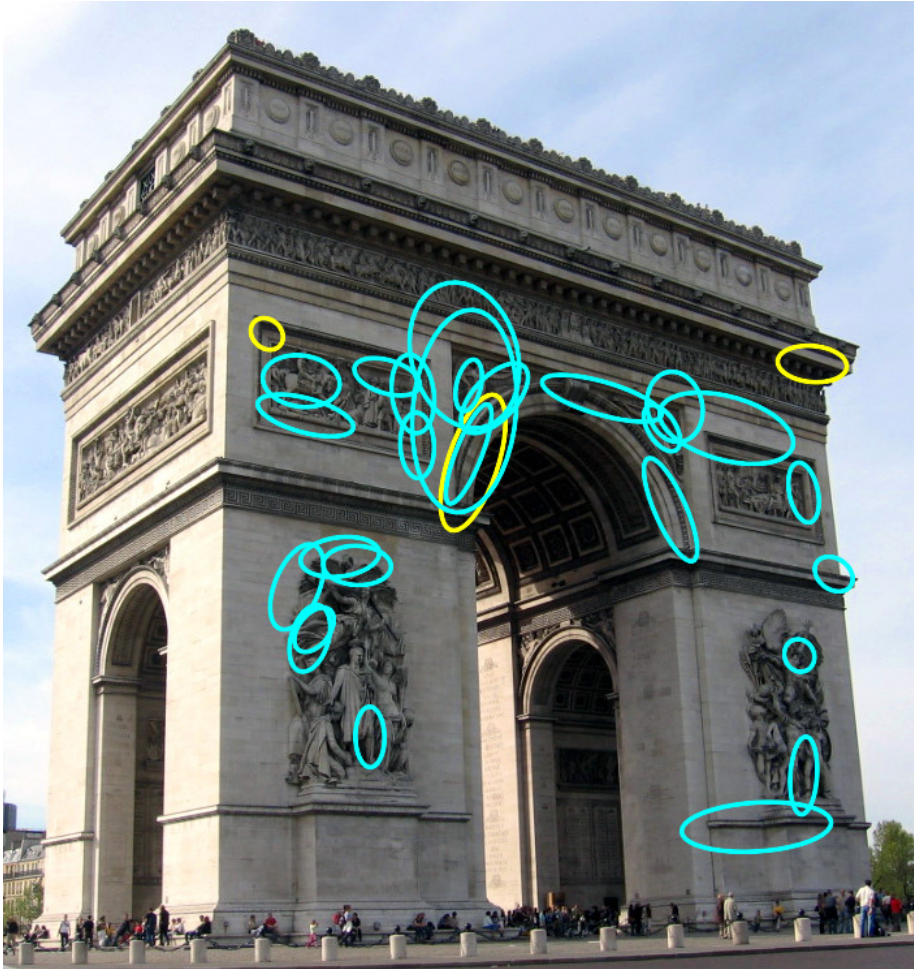
sideways image crawl



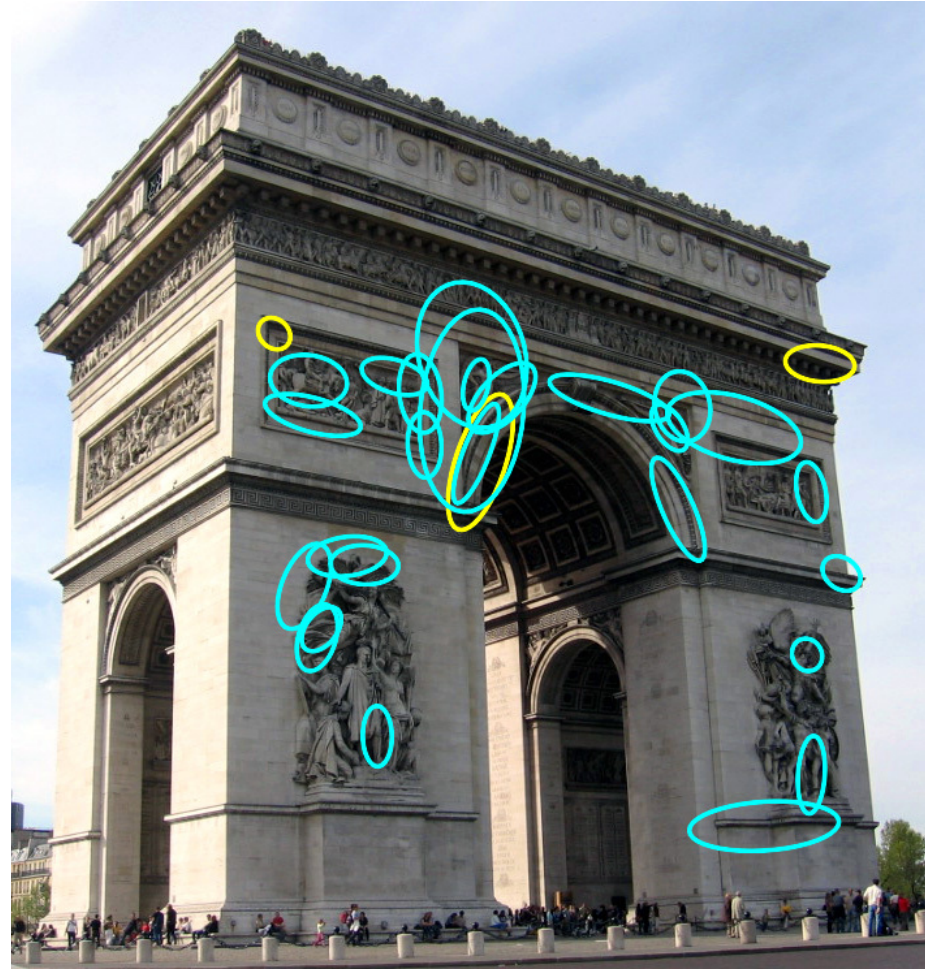
sideways left: step by step



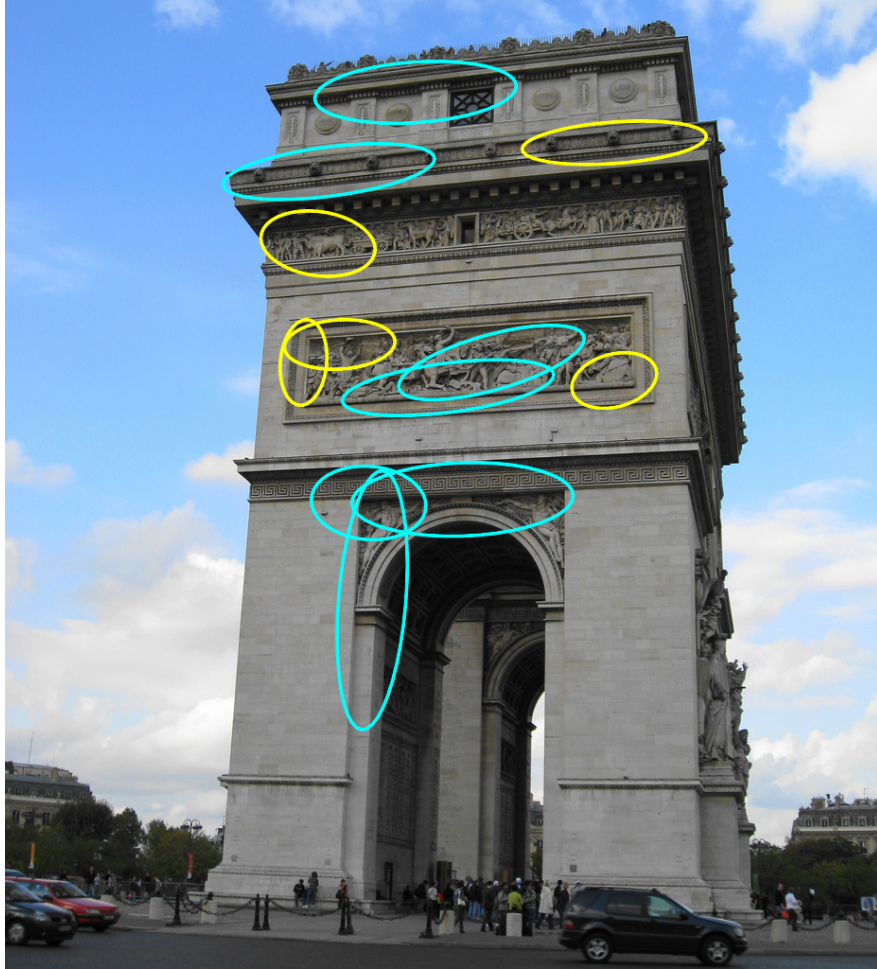
sideways left: step by step



sideways left: step by step



sideways left: step by step



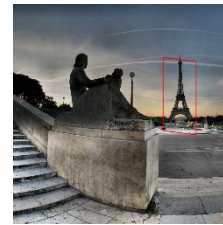
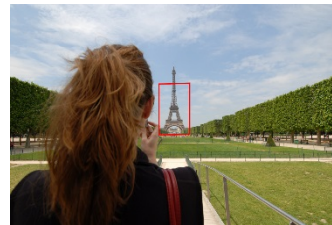
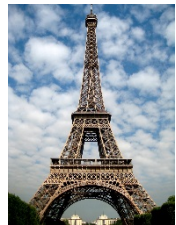
summary



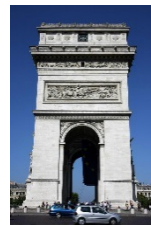
visually most similar



zoom-in / details

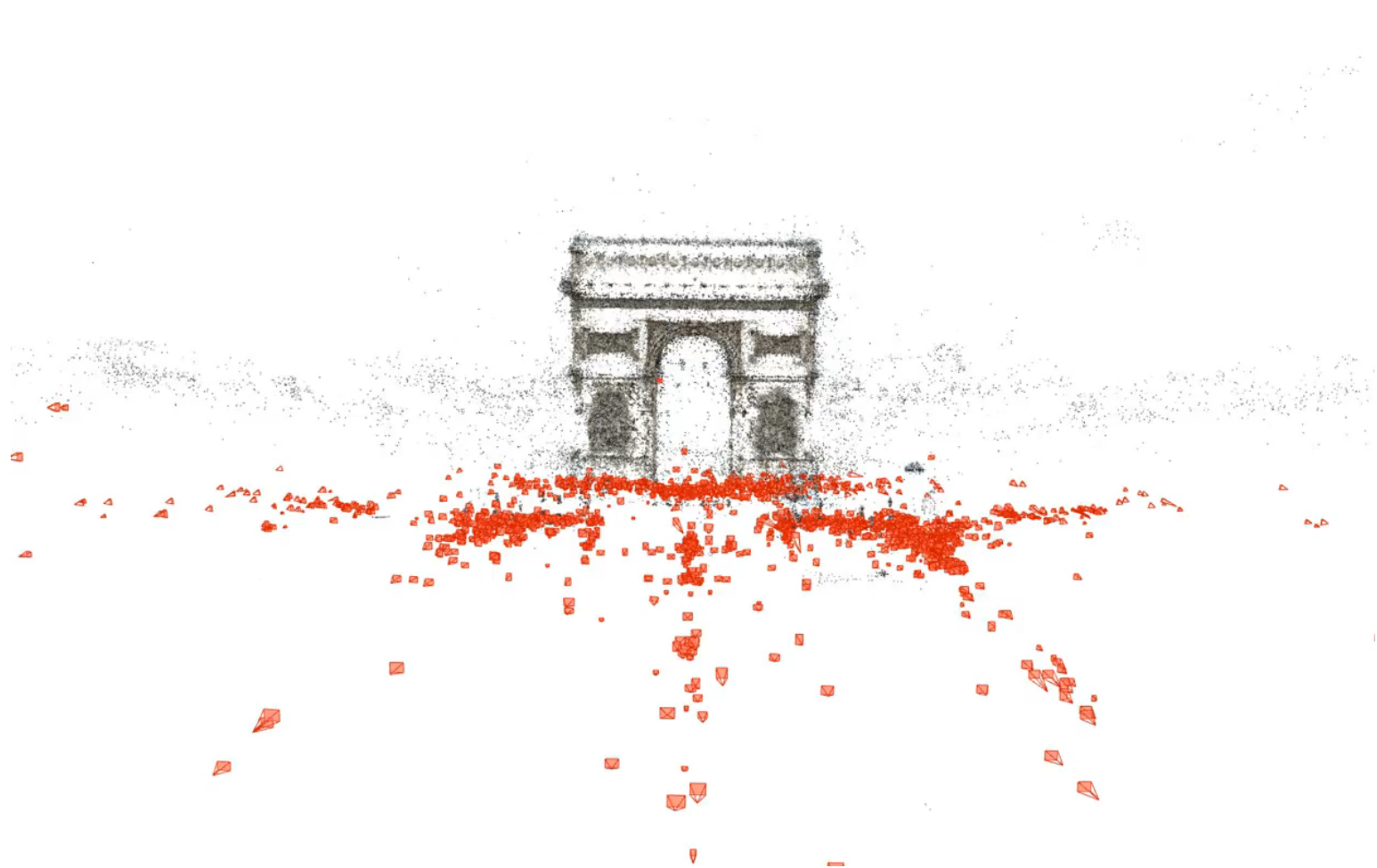


zoom-out

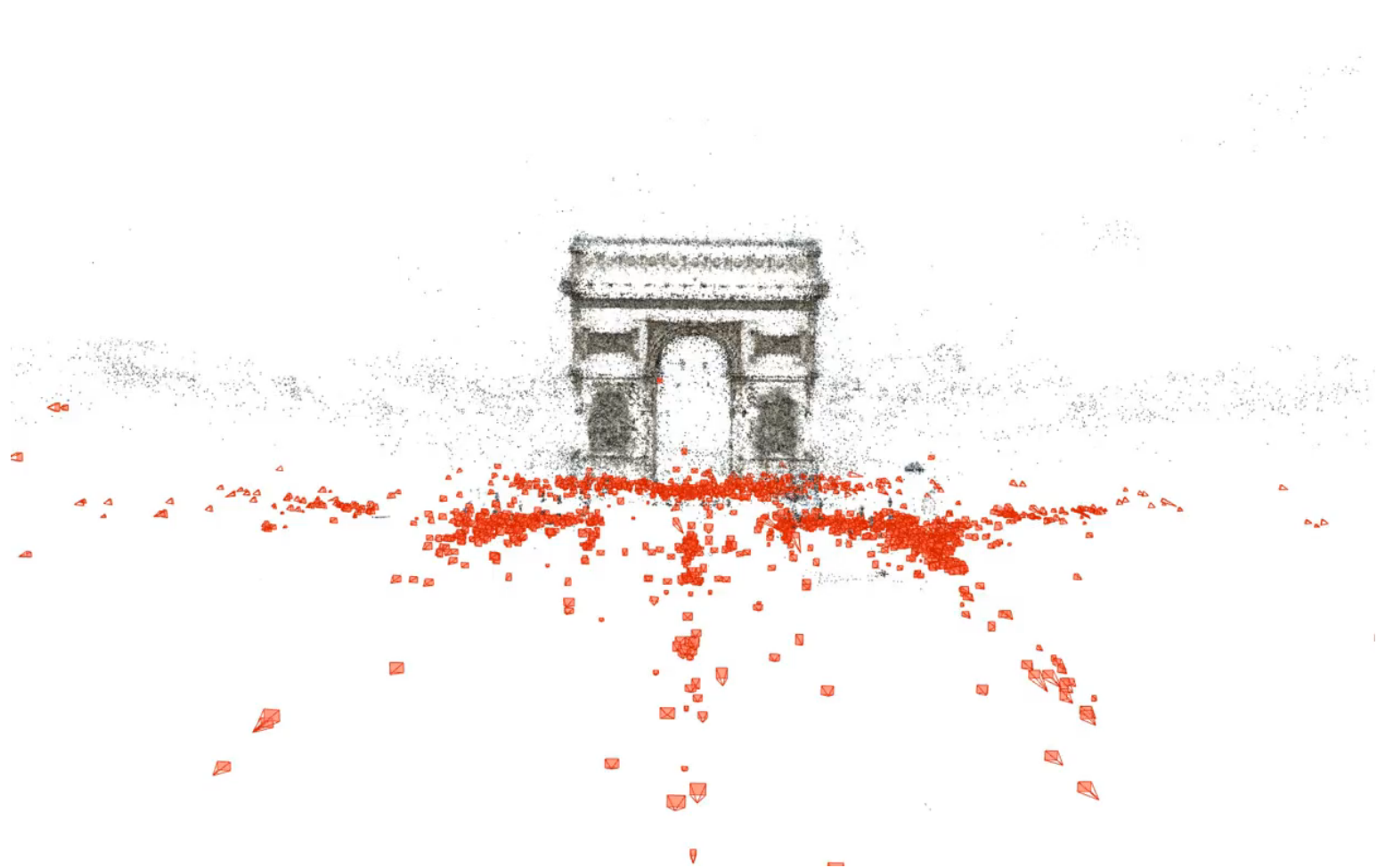


sideways right

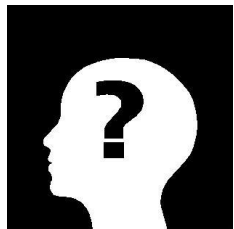
3D reconstruction – from a single image



3D reconstruction – from a single image



questions



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